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FATIGUE CRACK INITIATION IN 2024-T3 ALUMINIUM ALLOY

by

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Submitted to the faculty of the engineering In partial fulfillment of the requirements for the degree of

MASTER OF SCIENCE

MECHANICAL ENGINEERING



Bogazici University February, 1983 THIS THESIS HAS BEEN APPROVED BY:

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ACKNOWLEDGEMENTS

I would like to express my thanks to my thesis advisor Doç. Dr. ÖKTEM VARDAR for his great support throughout this study and to production director of Eskischir Supply and Maintenance Center Eng. Col. Fazil AYDINMAKINA for machining the specimen.

ABSTRACT

In this thesis "Fatigue-crack initiation in 2024-T3 aluminium alloy" was investigated using experimental methods with compact tension specimens having various notch root radius. The root radii are varied from 0.04 to 2.5 mm.

The fatigue-crack initiation tests were conducted on a closedloop servo-controlled fatigue testing machine. The loading was tension to tension and frequencies of fatigue tests were 3 Hz. Initiation of fatigue-crack was detected by means of a microscope.

The effects of notch root radius on the fatigue-crack initiation was evaluated by using linear-elastic-fracture-mechanics theory. The results of experiments are plotted, discussed and compared with the results of the previous studies.

ÖZET

Bu tez çalışmasında, 0.04 mm. den 2.5 mm. ye kadar degişen çenzik radiuslarına sahip (CTS) deney numuneleri ile deneysel yöntemer kullanarak 2024-T3 aluminyum alaşımı malzemede yorulma çatlakarının oluşması incelendi.

orulma çatlağının oluşum deneyleri kapalı devre servo-kontrollu orulma deney makinasında, çekme-çekme yükleme şartlarında, 3 Hz. orulma test frekansında yapıldı. Yorulma çatlağının oluşması bir ikroskop vasıtasıyla gözlendi.

Lineer-elastik-kirilma-mekanigi teorisi kullanılarak çentik dibi adiusların, yorulma çatlaklarının oluşması üzerindeki etkileri inelendi.

eney sonuçları grafik halinde gösterilerek bu konu üzerindeki daha nceki çalışmalarla karşılaştırılarak mukayese edildi.

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 $\Delta K_{I} / \sqrt{\rho} E$ and Ni data

LIST OF SYMBOLS

A	Material constant
a	Crack length
a/W	Crack length-the width of specimen ratio
B	Thickness of specimen
C	Material constant
da/dN	Crack growth rate
E	Young's modulus
K ^N f	Fatigue notch factor by Neuber
K ^P f	Elasto-plastic fatigue notch factor
К _Т	Stress intensity factor for mode-I
K _T c	Fracture taughness for mode-I
K _m	Elastic stress concentration factor
$\Delta \bar{K}_{th}$	Stress intensity range threshold at which the crack
	growth rate is apperently zero.
ΔK	Stress intensity factor range for mode-I
N i	Number of cycles for fatigue-crack initiation
P	Applied load
ΔP	Applied load fluctuation
∆ U nem	Nominal stress fluctuation
∆umax	Maximum stress fluctuation
P	Notch root radius

CHAPTER - I

INTRODUCTION

The field of fracture mechanics has become the primary approach for controlling brittle fracture and fatigue failures in structures. Brittle fracture of large structures caused large damages in the past.

In 1950's two Commet airerafts failed catastrophically while at high altitudes.An exhaustive investigation indicated that the failures initiated from very small fatigue-cracks originating from rivet holes near openings in the fuselage.

Numerous other failures of aircraft landing gear and rocket motor cases have occured from undetected defects or from subcritical crack growth by fatigue. The failure of F - 111 aircrafts were attributed to brittle fractures of members with preexisting flaws.

Metal fatigue was encountered as a general problem when engineers were faced with difficulties such as failure of railway carriage axles or partial failure of aircraft parts under repeated loads.

It should be considered how fracture mechanics can be used to prevent brittle fracture and fatigue failures of engineering structures. The fatigue life of structural components is determined by the sum of the elapsed cycles required to initiate a fatiguecrack and to propagate the crack from subcritical dimensions. Consequently, the fatigue life of structural component may be considered to be composed of three continous stages.

1- Fatigue-crack initiation

2- Fatigue-crack propagation

3- Fatigue fracture

Many studies of fatigue-crack initiation stage at the notch root have proved the great importance of this stage in predicting the fatigue life of structures. They are either for completly elastic [1,2,4] or simplified elasto-plastic analysis [5,6]. Many investigators have studied the other stages 1,7

1.1- FATIGUE-CRACK PROPAGATION

The fatigue-crack propagation behavior under constant amplitude load fluctuations for metals can be divided into three regions which can be observed in figure-1.1

Region-I exhibits a "Fatigue-threshold" cyclic stress intensity factor fluctuation, ΔK_{th} , below which cracks do not propagate under cyclic-stress fluctuations.

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Region-II, represents the fatigue-crack propagation behavior above ΔK_{th} , which can be represented by

$$\frac{da}{dN} = c (\Delta K)^{m}$$

(1.1)

Where, <u>da</u> = Fatigue-crack growth rate. dN

(c) and (m) are constants.

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N : Number of cycles.

 ΔK : Stress-intensity factor fluctuation,

 ΔK can be calculated by,

$$\Delta K = f(g) \ O \ Va \tag{1.2}$$

f(g) is a parameter that depends on the specimen and crack geometry.

Number of cycle for fatigue-crack propagation can be predicted by,

$$\int_{N} dN = \int_{a_{o}} \frac{da}{C(\Delta K)^{m}} \qquad (1.3)$$

In region-III, the fatigue-crack growth per cycle is higher than predicted for region-II. The rate of fatigue-crack growth increases. This increase occurs at a constant value of cracktip displacement, δ_{τ} , and at a corresponding stress-intensity factor value, K_{τ} , given by,

$$\delta_{T} = \frac{K_{T}}{E O_{ys}}$$

(1.4)

K_T : Stress-concentration factor value corresponding to onset of accelaration infatigue-crack growth rates.
E : Young's modulus

J. : Yield strength

Acceleration of fatigue-crack-growth rates that determines the transition from region-II to region-III appears to be caused by the superposition of a ductile-tear mechanism. Ductile tear occurs when the strain at the tip of the crack reaches a critical value.Thus, the fatigue-rate transition from region-II to region-III depends on K_{max} and stress ratio, R.

Equation-1.4 is used to calculate the stress-intensity factor value corresponding to the onset of fatigue-rate transition, $K_{\rm T}$ (or $\Delta K_{\rm T}$) which also corresponds to the point of transition from region-II to region-III in materials that have high fracture taughness.Acceleration of the rate of fatigue-crack growth occurs at a stress -intensity-factor value slightly below the criticalstress-intensity factor, $K_{\rm Ic}$.

1.2- FATIGUE FRACTURE

Fatigue fraçture occurs when the stress-intensity factor, K, reaches to a critical value, K_c , with increasing the fatigue crack length. Critical-stress-intensity factor, K_c , also depends on the specimen thickness.

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Figure-1.2

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The critical-stress-intensity factor, K_c , for a particular structural material, decreases with increasing specimen thickness. In figure-1.2 which shows that the minimum toughness of particular material, K_{Ic} , is reached when the thickness of the specimen is large enough so that the state of stress is plane strain. As the thickness of the specimen is decreased, even though the metallurgical characteristic of the material are not changed the stress-intensity factor increases and plane-stress, K_c , behavior exits.

CHAPTER - II

APPLICATION OF LINEAR ELASTIC FRACTURE MECHANICS (L.E.F.M) TO FATIGUE - CRACK INITIATION

Linear-elastic-fracture-mechanics technology is based on an analytical procedure that relates the stress-field magnitude and distribution in the vicinity of a crack-tip to the nominal stress applied to the structure, to size, shape and orientation of a crack and to the material properties.

2.1- THE ELASTIC-STRESS FIELD IN THE VICINITY OF A CRACK-TIP Figure-2.1 represents σ_x and σ_y components of the elastic-stress field in the vicinity of a crack-tip in a body subjected to tensile stresses normal to the plane of the crack.



The elastic-stress field in the vicinity of a sharp crack is presented by following equations.For MODE-I deformation, in plane-strain,

Where, the stress components and the coordinates (r) and (Θ) are presented in figure-2.1 .K_I is the stress-intensity factor by the help of which the magnitude of the elastic-stress field can be described.

2.2- THE ELASTIC-STRESS FIELD IN THE VICINITY OF SHARP

ELLIPTICAL OR HYPERBOLIC NOTCHES

The elastic-stress field in the vicinity of sharp elliptical or hyperbolic notches in a body subjected to tensile stresses normal to the plane of notch is presented by the following equation.



Figure-2.2

$$\begin{aligned}
\overline{U_{x}} &= \frac{K_{1}}{\sqrt{2\pi r}} \cos \frac{\Theta}{2} \left[1 - \sin \frac{\Theta}{2} \sin \frac{3\Theta}{2} \right] - \frac{K_{1}}{\sqrt{2\pi r}} \cdot \frac{P}{2r} \cos \frac{3\Theta}{2} \\
\overline{U_{\gamma}} &= \frac{K_{1}}{\sqrt{2\pi r}} \cos \frac{\Theta}{2} \left[1 + \sin \frac{\Theta}{2} \sin \frac{3\Theta}{2} \right] + \frac{K_{1}}{\sqrt{2\pi r}} \cdot \frac{P}{2r} \cos \frac{3\Theta}{2} \\
\frac{K_{1}}{\sqrt{2\pi r}} \sin \frac{\Theta}{2} \cos \frac{\Theta}{2} - \frac{K_{1}}{\sqrt{2\pi r}} \cdot \frac{P}{2r} \sin \frac{3\Theta}{2} \\
\end{bmatrix}$$

(2.4

Where, the coordinates (r) and (Θ), (ρ) are defined in figure-2.2

The first term in equation-2.2 defines the magnitude and distribution of the stress-field in the vicinity of a sharp crack. In this equation, K_{I} , is the stress-intensity factor. The second term in this equations represents influence of a blunt-tip radius on this stress field.

At point (B), in figure-2.2, for $\theta=0$; $r=\rho/2$

Equation-2.2 becomes,

$$\begin{cases} \sigma_{x} \\ \sigma_{y} \\ \tau_{xy} \end{cases} = \frac{K_{1}}{\sqrt{\pi\rho}} \begin{cases} 0 \\ 2 \\ 0 \end{cases}$$
(2.3)

$$\Delta \sigma_{\max} = \frac{2 \Delta K_1}{\sqrt{\pi \rho}}$$
(2.4)

Where, ΔK , is the stress-intensity factor fluctuation. Although equation-2.4 is considered exact only when (ρ) approaches zero. Wilson and Gabrialse [8] showed by using finite element analysis of blunt notches in compact tension specimens that this relationship is accurate to within 10 % for notch root radii up to 0.180 in.

2.3- EFFECT OF STRESS CONCENTRATION ON FATIGUE-CRACK

INITIATION

The effect of geometrical discontinuty in a loaded structural component is to intensify the magnitude of the nominal stress in the vicinity of the discontinuity. The localized stresses may cause the metal in that neighborhood to undergo plastic deformation. Because the nominal stresses in most structures are elastic the zone of plastically deformed metal in the vicinity of stress concentrations is surrounded by an elastic stress field. To predict the effect of stress concentrations on the fatigue behavior of structures, the fatigue behavior of the localized plastic zones has been simulated by testing smooth specimens under strain-controlled conditions.

A better simulation of the effects of stress concentrations on the fatigue behavior of structures is obtained by testing notched specimens under stress-controlled conditions because the applied stress can be more directly related to the struc-

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tural loading. The number of load fluctuations required to initiate a fatigue-crack in the vicinity of a notch tip is related to $\Delta K_1 / \sqrt{\rho}$, which in turn is related to the maximum alternating stress in the vicinity of the notch tip.

In the linear-elastic-fracture-mechanics theory, fatiguecracks do not initiate in structural components when the body configuration, the notch geometry and nominal stress fluctuations are such that the magnitude of the parameter $\Delta K_1 / \sqrt{\rho}$, is less than a given value, which is called threshold value. In general, the value of this fatigue-crack initiation threshold, $(\Delta K_1 / \sqrt{\rho})_{th}$, increases with increasing yield strength or tensile strength of the material.

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CHAPTER-III

PREVIOUS WORK

PEARSON (1) investigated the effect of notch depth and root radius on fatigue-crack initiation and propagation in half inch thick specimens aluminium alloys.

He used three-point bending specimens. The test specimen dimensions were 1 in.x 1/2 in. extruded bar B.S specification 1 65. The specimen were fatigued in bending machine. Loading was tension to tension. The cyclic load speed was 1500 cycles per minute and subsequent crack propagation is measized using the electrical resistance method.

He expressed that, for the same value of $\Delta K_1/\sqrt{\rho}$ the notches with low values of K_T have short initiation times. While the law,

$$N_{i} = C \left[\frac{\Delta K_{i}}{\sqrt{\rho}} \right]^{-5}$$
(3.1)

give a rough approximation, it does not exactly represent the results. In log N_i v.s $\log(\Delta K_1 / \sqrt{\rho})$ graph for a single notch depth and root radius, the test results lie on a straight line of slope 5 When log N_i versus $\log(\Delta K_1 / \sqrt{\rho})$ is plotted, it is seen that for the same root radius and a single notch depth, the overall scatter is grater than obtained Jack and Price [2].

The other approach was related to the fatigue stress concentration factor (K $_{\rm P}$) which was defined

Stress to produce failure in a given number of cycles in unnotched test pieces.

Net section stress to produce failure in same number of cycles in notched test pieces.

For fatigue-crack initiation, K_{fi} was defined as the ratio of the stress producing failure in unnotched test pieces in a given number of cycles to the stress initiating the crack in the same number of cycles in notched pieces.

The test results showed that the value of K_T/K_{fi} was almost constant for $\rho \ge 0.01$ in. and equal to 1.35 so that crack initiation can be represented by the equation,

For L 65 aluminium alloy;

K_f =

for $\rho \ge 0.01$ in.

 $\overline{V_{NSi}} = \frac{1.35}{K_{T}} \overline{V_{f}}$

(3-2)

Where; v_{NSi} = Net section stress to initiate a crack 0.005 in. long in N cycles. v_f = Failure stress for unnotched test pieces in N cycles.

It should be noted that there is a size effect in fatigue results for notched.specimens.

A.R.JACK and A.T.PRICE [2] investigated the initiation of fatigue-cracks from notches in mild steel plates. They used single-edge notched specimens of mild steel in their experimental work.

Test were carried out at room temperature on a testing machine of 10 000 lb. capacity. All tests were carried out at 20 cpm under zero to tension or tension to tension conditions. The major variables investigated were notch depth (a) and

roet radius (ρ). Three types of specimens were tested in experimental work and they had different width (w) and thickness (B). Tests were carried out at stress amplitudes in the range 1000 lbf/in² to 3500 lbf/in² measured on the gross section, under conditions producing failure in less than about 2x10⁵ cycles. Crack initiation was detected by using electrical potential drop of about 1mV over 1 in. of uncracked specimens.

They showed that number of cycles to initiate a fatiguecrack was proportional to the range of stress-intensity factor

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 (ΔK) for sharp notches which have $\rho \leq 0.010$ in. the test data was analysed by plotting N_i against the stress-intensity factor range.It was noted that the slope of this line was (4) and N_i was proportional to $(\Delta K)^{-4}$

i.e.

$$N_i \propto (\Delta K)^4$$
 (3.3)

within the ranges studied, there was no effect of width or thickness.

Test on specimens having notch root radiiograter than 0.010 in. showed that N_i increasing with increasing root radius.At particular values of (a) and (Γ), the relationship indicated was

$$N_i \propto \sqrt{\rho}$$
 (3.4)

If the relationship is analysed clearly, for the notch root radius values which are grater than critical notch root radius (0.010 in.), it can be noted that the number of cycle to initiate a fatigue-crack is a function of $\Delta K/\sqrt{\rho}$. Y.H.KIM, T.MURA and M.E.FINE [3] investigated fatiguecrack initiation and microcrack growth in 4140 steel in three conditions, as-quenched, tempered at 400°C and tempered at 600°C. Specimens 90x20x3.2 mm size were machined from 3.5 mm thick plates. The specimens were austenitized in Argon for one hour at 1000°C and then oil-quenched and with two different tempering conditions were investigated, one hour at 400°C or 650°C in vacum.

Single-edge notched specimens were used in the experimental study. The specimens have a crack 1 mm long (a) and with 0.22 mm radius of curvature (ρ). Only one notch geometry was investigated

All fatigue tests were conducted on a closed-loop electrohydraulic MTS machine of 90 KN capacity at room temperature using 30 Hz. test frequency.Fatigue-crack initiation was detecte by a metallurgical microscope.

They indicated the results for crack initiation in the 4140 steel samples for each of three conditions in the graphs. They defined N_{ii} as the number of cycles to initiation 3 μ m crack and N_{if} as the number of cycles to form a crack extending across the full lateral dimensions of the notch i.e 3.2 mm.

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For as-quenched 4140 steel, very few cracks formed near the notch edges.Furthermore, once the crack initiated, it grew rapidly to the fatal crack and N_{if} was not much grater than N_{ii}

For 650°C tempered samples approximately 100 fatiguecracks formed near the edges of notch and these grew very zero slowly or not at all.

For 400 and 650°C tempered specimens N_{if} was considerably larger than N_{ii} . They suggested that the N_{ii}/N_{if} ratio could be approximately 0.1 and microcracks grew most rapidly in asquenched specimens and least rapidly in 650°C tempered specimens at the same $\Delta K / \sqrt{\rho}$.

In as-quenched specimens, fatigue-cracks initiated at grain boundaries but in the 400 and 650°C tempered specimens, they initiated at intrusions-extrusions.

The experimental results for the threshold values of $\Delta K/\sqrt{\rho}$ were compared to the $\Delta K/\sqrt{\rho} |_{=} 26x(\sigma_{ys})^{2}$ which was BARSOM's new correlation. The agreement with the new BARSOM formula was much better than with the old formula which was $\Delta K/\sqrt{\rho} |_{=} 9.5x(\sigma_{ys})$ The experimental results are plotted in $\log[\Delta K/\sqrt{\rho} - \Delta K/\sqrt{\rho} |_{th}]$

v.s.log.N_{if} graph.The data fit reasonably well to straight line. They suggested that the crack initiation data for 4140 stee were fit to the emprical equation.

$$N_{if} \simeq (\Delta K / \sqrt{\rho} - \Delta K \sqrt{\rho} |_{th}) \qquad (3.5)$$

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J.M.BARSOM and R.C.MCNICOL [4] investigated effect of stress concentration on fatigue-crack initiation in HY-130 steel.

They used double-edge-notched specimens which were 20 in. long 6 in. wide, and 0.125 in. thick. Notch tip radii were changed from 0.008 in. to 0.375 in. The polished, unnotched specimens, that were tested, had 10 in. radius.

All specimens were tested at room temperature in 50 kip on MTS.The frequency of stress fluctuation was 120 to 600 cpm. Fatigue-crack initiation was detected optically with a stereozoom microscope.The specimens were tested over a range of fluctuating stress and number of cycles required to initiate a 0.01 in. crack was recorded.The variation of notch acuity covered the range from fatigue-cracked specimens to polished, unnotched specimens and fatigue-crack initiation data were obtained in the range 10³ to 10⁶ cycles.The data were analyzed by using linearelastic-fracture-mechanics concepts and theory of stress conceptration in notched specimens.

Their results showed that the number of elapsed load cycles required to initiate a fatigue-crack in notched specimens is related to the ratio of the fluctuation of stress intensity factor ΔK_{I} to the square root of the notch tip radius (ρ). Fatigue-crack initiation life can also be expressed in terms of the fluctuation of the maximum stress at the notch tip (ΔG_{max}) because $\Delta K_{I}/V\rho$ can be related to (ΔG_{max}).

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Fatigue-crack initiation threshold was investigated in HY-130 stell by BARSOM and McNICOL. The data indicated that fatiguecracks did not initiate in steel structural components when the body configuration, the notch geometry and nominal-stress fluctuations were such that the magnitude of the parameter $\Delta K_{l}/\sqrt{\rho}$ was less than a given characteristic value of steel. In general, the value of this fatigue-crack initiation threshold $(\Delta K_{l}/\sqrt{\rho})_{th}$ increased with increasing yield strength or tensile strength of the steel.

They showed that fatigue-crack initiation threshold at $\Delta K_1 / \sqrt{\rho} = 85 \, \text{Ksiwas}$ reasonably applicable to notches having a stress-concentration factor value, K_t , that ranged from 17.2 for the specimen with ρ =0.008 in. to 2.9 in. for the specimens with ρ =0.375 in.

They suggested that the fatigue-crack initiation threshold in martensitic steels of various yield strengths tested under zero to tension load fluctuation can be predicted by the equation.

$$\frac{\Delta K_{I}}{\sqrt{\rho}} = 0.6$$

(3.6)

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The use of this relationship to predict the fatigue-crack initiation threshold in various metal alloys may require normalizing the relationship with respect to Young's modulus, E, or some power of E.

The test data showed that, in the finite-initiation life region, the number of elapsed cycles required to initiate a fatigue crack at the tip of a notch, N_i, is related to the parameter $\Delta K_{I} / \sqrt{\rho}$ by the equation

$$V_{i} = \beta \frac{1}{\left(\Delta K_{I} / \sqrt{\rho}\right)^{n}}$$
(3.7)

Where, β is a constant and the value of exponent,(n),decreases.

The data also showed that at a constant value of the parameter, $(\Delta K_I / \sqrt{\rho})$, the number of cycles required to initiate a fatigue-crack in the region of finite cyclic life, increased as the notch-tip radius increased.

A.BAUS, H.P.LIEURADE, G.SANZ, and M.TURCHON [5] investigated fatigue-crack initiation at the root of a notch. The specimen material was two kinds of high-strength steels (AFNOR 35 NCD 16 and 35 NCD 4). They used compact tension specimen, 15 mm thick, having various notch root radii between 0.003 in. and 0.04 in. All crack initiation testing was conducted on a servo-hydraulic fatigue machine of \pm 100 KN under tension to tension loading conditions and at a frequency of 20 Hz.In order to detect fatigue-crack initiation in the center of the specimen, they used two methods which were compliance measurement and potential drop method.

They showed that for the same notch root radius, the test points lie on a straight line. If the number of cycles to initiate a fatigue-crack is to be kept constant a higher load amplitude must be applied to the specimen for increasing the stress intensity fluctuating as the notch root radius increases. When the $N_i v \cdot s \Delta K_i / \sqrt{\rho}$ diagram was plotted, it was noted that the points still lie on straight lines at constant notch root radius, but corresponding $\Delta K_i / \sqrt{\rho}$ levels decreases as the root radius(ρ) increases.

Another approach of elastic analysis is fatigue notch factor (K_{f}) which is characteristic of both the mechanical notch and material. K_{f} is defined as the ratio of the fatigue limits of unnotched specimens and a notched specimen, during tests of the same type.

It was not possible to carry out a comparison with tests on unnotched specimens when the notched ones were compact. Thus they used Neuber's emprical formula to define the notch factor which was,

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$$K_{f}^{N} = 1 + \frac{K_{T} - 1}{1 + \sqrt{A/\rho}}$$
 (3.8)

Where, K_{T} , is the stress concentration factor and A is a material constant.

Knowing K_f, it was possible to calculate the amplitude of the maximum stress at the notch root by the formula,

$$\Delta \overline{O}_{max}^{N} = K_{f}^{N} \times \Delta \overline{O}_{nom}$$
(3.9)

In elasto-plastic analysis of stress concentration, the modified Neuber rule was a powerful means of expressing notch root stress-strain behavior.

$$K_{f}^{2} = K_{\sigma} \times K_{\epsilon}$$
(3.10)
$$K_{\sigma} = \frac{\Delta \overline{U}}{\Delta \overline{U_{nom}}}$$
(3.11)

$$K_{\epsilon} = \frac{\Delta \epsilon}{\Delta \epsilon_{\text{nom}}}$$
(3.12)

and;

$$K_{f^{\star}} \Delta \overline{U_{nom}} = \sqrt{E.\Delta \overline{U}.\Delta \varepsilon}$$
 (3.13)

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After each initiation test, it is verified that for a given material and given value of K the ratio $\sqrt{E.\Delta S.\Delta E}/\Delta E_{nom}$ remained constant whatever the value of N with only a small scatter in the values around an average value which they call EP K_f .Knowing the values of K_f^{EP} for each material and each notch configuration, they presented the test results relating K_f^{EP} $\propto \Delta G_{nom}$ and N_i in a graph.

 K_{f}^{N} , the fatigue notch factor and K_{f}^{EP} , elasto-plastic initiation parameter which can be calculated from the Manson-Coffin curve and cyclic stress-strain curve of the material.They suggested that these parameters did not yield the same accuracy for the calculation of the number of cycles N_{i} .The K_{f}^{EP} approach showed that there exists a good correlation between fatiguecrack initiation when $N_{i} < 10^{5}$ cycles and materials low-cycle fatigue behavior.

They were in good agreement with BARSOM who suggested that the elastic $\left(\Delta K / \sqrt{\rho}\right)_{th}$ approach was very helpful when $N_i > 10^6$ cycles. $\left(\Delta K / \sqrt{\rho}\right)_{th}$ defines a threshold value under which no crack occurs.

K.SAANOUNI and C.BATHIAS [6] studied on the fatigue-crack initiation in the vicinity of notches of the 316 austenitic; stainless steel.They used 28 notched compact tension specimens with two different widths, various notch depth (a) and root radii (ρ).

Crack-initiation testings were conducted on hydraulic fatigue test machine. The loading condition was tension to tension and frequencies vary between 0.1 and 5 cps. in air enviroment and room temperature. Fatigue-crack initiation was detected by three different monitoring techniques.

One procedure involved electrical potential variation with time. The second procedure involves crack opening displacement variation versus time and third one, the use of scaled microscope mounted at both polished sides of compact tension specimens. Their test results showed that for the same N_i , ΔG_{nom} increas-

ed when notch root radius increased. The real stress amplitude at the notch tip $\Delta \widehat{\sigma}_{max}$ was

$$\Delta \mathcal{G}_{\max} = K_{T} \Delta \mathcal{G}_{\operatorname{nom}} = \frac{2}{\sqrt{\pi}} \frac{\Delta K}{\sqrt{\rho}}$$
(3.14)

For both parameters $(\Delta K/\sqrt{\rho} \text{ and } K_T \Delta G_{\text{nom}})$ it is assumed that initiation was an elastic phenomenon neglecting the plasticity deformation at tip of the notch. They defined a critical value for notch root radius (ρ_c) below which the number of cycles N_i was independent of $\frac{G \min}{G \max}$. The critical notch root radius was found to be 0.25 mm.

Although the nominal stress range may be elastic, there is always a plastic zone which caused by the localized stresses at

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the notch root. Therefore the elasto-plastic analysis was used to predict the number of cycles to initiate a fatigue-crack. A function of damage is defined as, ($\sqrt{E.\Delta 0.\Delta E}$)

$$K_{\mathbf{J}} = K_{\mathbf{T}} \times K_{\mathbf{E}}$$
 (3.15)

$$K_{c} = \frac{\Delta G_{nom}}{\Delta G}$$
(3.16)

$$K_{\epsilon} = \frac{\Delta \epsilon_{\text{nom}}}{\Delta \epsilon}$$
(3.17)

 K_{f} is introduced instead of K_{T} in the above relation and if the nominal stress range ΔG_{nom} is limited within elastic range and

$$\Delta \epsilon_{nom} = \frac{\Delta \overline{\epsilon}_{nom}}{E}$$
(3.18)

thus,

$$K_{f} \star \Delta G_{nom} = \sqrt{E.\Delta G.\Delta \varepsilon} \qquad (3.19)$$

where both ΔG^- and ΔE were calculated using the cyclic atress-strain curve and Manson-Coffin one for each N_i.

The variation of damage function versus N_i showed that all the test results, lie on one unique line for two types of specimens and all notch root radii.

This could be expressed as;

$$N_{i} = \left[\Psi / \sqrt{E.\Delta G.\Delta E} \right]$$
(3.20)

Where, (Ψ) and (\propto) are material constants. In equation-3.9 $\Delta \xi = \Delta \xi_e + \Delta \xi_p$ in which the plastic deformation is not neglected. In using $K_f \cdot \Delta G_{nom}$ one most also take into account the plastic deformation. But ΔG_{nom} is calculated by neglecting this fact. So the only parameter that can take into consideration for plasticity is the fatigue notch factor K_f , called K_f^p . The Neuber relation,

$$K_{f} = 1 + \frac{K_{f} - 1}{1 + \sqrt{A/p}}$$
 (3.21)

Where A is defined by Neuber to be a material constant which represents the distance from notch tip after which there is no more stress gradient.

$$A = \left[(K_{r} - K_{f}) / (K_{f} - 1) \right]^{2} x \rho$$
 (3.22)

In constant amplitude test with different values of ΔK (or ΔP), for the same notch geometry, they showed that the function (A) depended not only on the material but also on K which generated the plastic zone size.

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$$A=\Psi (material, r_y)$$
(3.23)

Monotonic plastic zone is, where the material is monotonically plastically deformed, its size is;

$$\Gamma_{ym} = \frac{1}{6\pi} \left[K_{max} / G_{y} \right]^{2} \quad \text{if} \quad \Delta G_{nom} \ge G_{y}$$
(3.24)

Cyclic plastic zone is where the material is deformed plastically in a reversible manner, its size is;

$$\Gamma_{yc} = \frac{1}{6\pi} \left[\Delta K / 2G_{y} \right]^{2} \quad \text{if} \quad \Delta G_{nom} < G_{y}$$
(3.25)

To define the fuction Ψ , they plot the values of A calculated using equation-313 versus (r_y) and they found,

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$$A=0.02 \exp(1.87\sqrt{r_y})$$
 (3.26)

Introducing Neuber relation, they obtained

$$K_{f}^{P} = 1 + \left[(K_{t-1}^{*})/(1 + (0.02 \exp(1.87 \sqrt{F_{y}}))/\rho)^{1/2} \right]$$
(3.27)

Where Kt is the theoretical elastic stress concentration factor calculated from the critical notch root radius.

Plotting the relation between $K_{1}^{P} \propto \Delta \overline{V_{nom}}$ and N_{i} , it was suggested that to predict the number of cycles to initiate a fatiguecrack, the below formula could be used

$$N_{i} = \left[\dot{A} / (\kappa_{f}^{P} \Delta \overline{u_{nom}}) \right]$$
(3.28)

Where,A' and & were constant for 316 austenitic stainless steel.

The test results showed that the localized material element in the tip of the notch, is plastically deformed and crack initiation needs to be studied by an elasto-plastic analysis. Although the analysis based on function of damage (\sqrt{E} . ΔC . ΔC) gave better results in prediction of N_i. The real values of ΔC and ΔE are obtained by experimental techniques. On the other hand, the analysis based on elasto-plastic fatigue notch factor K_{f}^{P} was more advantageous for simple prediction of N_{j}^{\bullet} . The function of A' needs to be well defined in the elastoplastic analysis.

CHAPTER - IV

EXPERIMENTAL WORK

4.1- MATERIAL PROPERTIES

The material used throughout this experimental study was 2024-T3 type of Aluminium alloy, with the chemical composition and mechanical properties as below [14]

CORE	Fe	Cu	Mn	Mg	Zn	Ti	Va	Zi	Silicon
°/ <i>o</i>	0.5	5.8 _ 6.8	0.2_ 04	0 .0 2	0.1	002_0.01	0.05	0.10	0.5

ASTM number	: B 209	
Goverment number	: QQ – A – 250	
Typical uses	:Aircraft structures, rivets, hard ware	
	truck wheels, screw-machine products e.	t.c.
Density	: at 68°F (20°C) 2.77 kg/cm ³ 0.100 lb	/in ³
Liquidus temp.	: 1180°F (638°C)	
Solidus temp.	: 935 [°] F (502 [°] C)	

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Thermal expansion	micro-in/in/ ^O C
-76 to +68°F (-60 to +20°C)	21.4
68 to 212°F (20 to 100°C)	22.8
68 to 392°F (20 to 200°C)	23.9
68 to 572°F (20 to 300°C)	24.7

Specific heat at 212°F (100°C)	: 0.23 cal/g.
Thermal conductivity at 77°F	: 0.29 cal/cm/cm/°C/sec.
Electrical conductivity	: 30 % IACS
Electrical resistivity at 68°F	: 5.75 microhm-cm
Rockwell hardness	: 83-87 RH(B)
Brinell hardness	: 120 (500 kg load 100 mm ball
T3 Heat treatment :Solution h	neat treated and then cold
worked by	2) attaning ononation

Mechanical properties of 2024-T3 Aluminium alloy plate:Ultimate tensile strength: \overline{U}_{ult} =64000 lb/in² =45 kg/mm²Tensile yield strength: \overline{U}_{TYS} =42000 lb/in² =29.5 kg/mm²Compressive yield strength: \overline{U}_{CYS} =45000 lb/in² =31.6 kg/mm²Critical stress intensity factor : Kc =40000 lb/in^{3/2} = 140 kg/mm²Elongation: 18 %Modulus of elasticity: 10.6x10⁶ lb/in² = 0.75x10⁶ kg/ctFatigue limit: 17-20 kg/mm²

4.2-THE SPECIMEN PREPARATION

The specimen have been prepared in the department of Jet motor of Eskischir Supply and Maintenance Center before going on with testing on electro-hydraulic closed loop (MTS 812) fatigue testing machine.

Fatigue-crack initiation tests are performed with the compact tension specimen which is single-edge notched and pin loaded in tension. The geometry of the compact tension specimen and notch are shown in figure-4.1



Figure-4.1

0.04≤ *9* ≤2 mm



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In this study, Dimensions are chosen such as;

W = 45 mm a = 21 mm H = 55 mm B = 10 mm F = 22.5 mm \$\alphi\$ = 10 mm

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The specimen were cut the notch being in the rolling direction of 15 mm thickness Aluminium alloy plate and marked. The pin holes, root radii and notches were machined using a sharp milling cutter. The notch radii vary from 0.04 mm to 2.5 mm; the notches were cleaned and polished by shoot peening.

4.3-EXPERIMENTAL PROCEDURE FOR FATIGUE-CRACK INITIATION

Crack initiation tests were conducted on electro-hydraulic closed loop (MTS 812) fatigue testing machine with a maximum capacity of 10 tons, under sinusoidal tension to tension loading condition at constant amplitudes for all tests.

The test frequencies are 3 Hz. and the conditions are standert with embient room temperature.Fatigue-crack initiation is detected by means of a Gaertner Travelling Microscope (10 X) The microscope is mounted such that one can look directly into

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the notch root (figure-4.2) and scan the notch root across the thickness (B) for incipient crack growth.



Figure-4.2

Each test is terminated when fatigue-crack initiation is observed at the notch root on the microscope and the number of cycles is recorded. The applied load selected from 40 kg to 650 kg for different specimens having different notch root radius The applied load monitored through a digital voltmeter. The number of load cycles is counted by the MTS fatigue testing machine.





4.4- RESULT AND DISCUSSION OF FATIGUE-CRACK INITIATION TEST

All of the fatigue-crack initiation test results are sumerized in table - 1

Maximum alternating stress can be calculated by equation- ΔK_{I} is the stress-intensity fluctuation which is obtained for compact tension specimen as [8]

$$\Delta K_{I} = \frac{\Delta P}{B\sqrt{W}} f(a/W)$$
 (4.1)

 $f(a/W) = 29.6(a/W)^{1/2} - 185.5(a/W)^{3/2} + 655.7(a/W)^{5/2} - 1017(a/W)^{7/2} + 638.9(a/W)^{9/2}$

Where;

△P : Applied load

B : Thickness of the specimen

W : Width of the specimen

a : Crack length

Nominal stress fluctuation is calculated by the equation-For compact tension specimen [6]

It is given as;

$$\Delta \overline{I}_{nom} = \frac{\Delta P}{B(W-a)} \begin{bmatrix} 1 + \frac{3(W+a)}{(W-a)} \end{bmatrix}$$
(4.2)

The fatigue-crack initiation behavior of the specimen is presented in figure-5.1 , in terms of the number of cycles for fatigue-crack initiation, N_i , versus the nominal stress fluctuation, $\Delta \overline{\Omega_{nom}}$.

The data presented in figure-5.1 for ρ =1.5 mm, show that the number of cycles to initiate a fatigue-crack in the low-cycle region, which is defined $N_i \leq 5 \times 10^4$ cycles, can be calculated by

$$N_{i} = A \left(\Delta \overline{U_{nom}} \right)^{-1}$$
(4.3)

Where,	for p=1.5 mm	n=1.88	$A=6.5 \times 10^6$
	0=0.5 mm	n=1.72	A=8.1x105

The increase of values of (n) and (A), for different notch root radius, show that the number of cycles required initiate a fatigue-crack, (N_i) , can not only be related to the (ΔK_I) but also related to the notch tip radius. Barsom and McNicol [4] show that, for HY-130 steel, n=2 for fatigue-crack increase to n=8 for unnotched specimen.

The data presented in figure-5.2 indicated that the number of cycles required to initiate a fatigue-crack at the tip of the notch, N_i, is related to the parameter ($\Delta K_I / \sqrt{\rho}$). This relation is defined by the equation-

$$N_{i} = \beta \frac{1}{\left[\frac{\Delta K_{I}}{\sqrt{\rho}}\right]^{k}}$$

(4.4)

Where, (θ) and (k) are constants, for constant notch root radius, the value of (β) can not be predicted in limited fatiguecrack initiation test data. When a small scatter band is plotted for the overall fatigue-crack initiation test data, the value of (β) is varied from $(6.16)*10^8$ to $(3.16)*10^9$. The value of exponent (k) is equal to 2.7

It can be noted that $\Delta K_1 / \sqrt{\rho}$ increases as N_1 increases in figure-5.2 .Pearson [1], Jack and Price [2], Barsom and McNicol [4] gave the same relation (4.4) for fatigue-crack initiation.

Pearson suggested that the value exponent (k) was 5 for aluminium alloy, the value of (k) was 4 for mild steel, obtained by Jack and Price. However, Barsom and McNicol [4] show that the value of exponent (k) is related to the notch root radius (ρ).

If the value of $\Delta K_1 / \sqrt{\rho}$ is equal or lower than 22 kg/mm² for 2024-T3 Aluminium alloy, the number of cycles required to initiate a fatigue-crack, N₁, is grater than 4×10^5 cycles.

In the case of crack-propagation, data of different materials may be combined by normalizing with the elastic modulus (E). The same approach may be tried on initiation data. Hence the value of $\Delta K_{I} / \sqrt{\rho}$ is normalized by the elastic modulus (E) and entered in table-2. When the log $\Delta K_{I} / \sqrt{\rho}$ E v.s log N₁ is plotted, it can be seen that the test points of 2024-T3 Aluminium alloy and steel lie on the straight lines in figure-5.3

The slope of lines are;

k = 3.7	for	Jack and Price
k = 4	for	Barsom and McNico
k = 6.2	for	Vardar
k = 2.7	for	2024 - T3
k = 4.82	for	Pearson .

In this study, the test results are in good agreement with Barsom and McNicol, Jack and Price, Pearson. In the low-cycle region, the value of $\Delta K_{I} / \sqrt{\rho} \in I$ is grater than the 3×10^{-3} for steel and aluminium alloy.

An experimental fatigue notch factor which characteristic of both the mechanical notch and material. It is called Kr and defined as the ratio of the fatigue limits of unnotched specimen and a notched specimen during tests of the same type.As it is not possible to carry out a comparison with tests on unnotched specimens when the notched ones are compact tension specimen. This coefficient is determined by means of an emprical formula which is given by Neuber.

$$K_{f}^{N} = 1 + \frac{K_{T} - 1}{1 + \sqrt{A/\rho}}$$

$$\frac{1/2}{A} = (24/G_{ult})^{3} in.^{1/2}$$
(4.6)

(4.6)

Where, A is a material constant. Heywood [1] says that for aluminium alloy,
$$A = 0.07$$
 mm.

Knowing K_{f}^{N} , it is possible to calculate in each case the amplitude of the maximum alternating stress at the notch root by the formula,

$$\Delta \overline{\mathcal{G}}_{max} = K_f^N \times \Delta \overline{\mathcal{G}}_{nom}$$
 (4.7)

In elastic analysis, the parameter K_T, which is defined elastic stress concentration factor, is possible to write as [5]

$$K_{\rm T} = \frac{1}{\Delta G_{\rm nom}} \times \frac{2\Delta K_{\rm I}}{\sqrt{\pi \rho}}$$
(4.8)

The values of K_{τ} and K_{f}^{N} are calculated for each specimen and entered in table - 1

In figure-5.4 log $K_f^N \times \Delta \widehat{U}_{nom}$ v.s log N_i is plotted. It can be shown that the number of cycles required to initiate a fatigue-crack is related to $K_f^N \times \Delta \widehat{U}_{nom}$ in log-scale.

Pearson suggested that N_i could be related to $K_{f^x}^N \Delta \mathcal{T}_{nom}$ linearly in log-scales for L 65 aluminium alloy.

CHAPTER - V

CONCLUSION

There are two different points of view on fatigue-crack initiation of the materials under cyclic-loading. One of them elastic-approach the other one is elasto-plastic approach.

In this study, the elastic approach was used and the fatigue-crack initiation was investigated by using linear-elastic-fracture-mechanic (LEFM) concepts and theory of stress-concentration in notched speci men.

The number of cycle required to start a fatigue-crack in the low-ccycle region, which is defined $N_i \leq 5 \times 10^4$ cycles, can be calculated by equation-5.1

 $N_i = A \left(\Delta \overline{v_n}_{om} \right)^{-n}$

(5.1)

The stress intensity factor fluctuation ΔK_{i} have been calculated from the equation-4.1 for compact tension specimen. The test results are good^Aagreement with Barsom-McNicol,Pearson and Jack-Price.It can be deduced that the number of load cycles required to initiate a fatigue-crack is related to the ratio of the stress-intensity-factor fluctuation to the square root of the notch root radius.This relation is defined by the below formula.

$$N_{i} = \beta \frac{1}{\left[\frac{\Delta K_{i}}{\sqrt{\rho}}\right]^{k}}$$
(5.2)

Where, the value of exponent (k) is equal to 2.7 Fatigue-crack initiation can be expressed in terms of the maximum stress fluctuation $\Delta \overline{V}_{max}$ at the notch tip, because $\Delta K_{\rm r} / \sqrt{\rho}$ is related to $\Delta \overline{V}_{max}$.

For 2024 - T3 aluminium alloy, if the value of $\Delta K_{I}/\sqrt{\rho}$ is equal or less than 22 kg/mm², the number of cycles required to initiate a fatigue-crack is more than 4×10^{5} cycles. This criterion can be defined as a threshold value for the notched structural components because the fatigue limit of 2024 - T3 aluminium alloy 17 - 20 kg/mm² is based on 10 cycles.

Normalizing the equation of $(\Delta K_1 / \sqrt{\rho}) = 22 \text{ kg/mm}^2$ we get;

$$\frac{\Delta K_{I}}{\sqrt{v_{s}}\sqrt{\rho}} = 0.74$$

(5.3)

Fatigue-crack initiation threshold in aluminium alloys of various yield strengths can be predicted by using equation-Barsom and McNicol suggested that threshold value of $\Delta K_1/\Gamma_{ys}\sqrt{\rho}$ were 0.6 for various steels.

When the $\log \Delta K_1 / E \sqrt{\rho}$ v.s log N_1 is plotted for steels and aluminium alloys, it can be seen that the test results lie on the different straight lines for different materials and there is not any test point below $\Delta K_1 / E \sqrt{\rho} = 3 \times 10^{-3}$ in lowcycle region.

If the notch factor is known K_{f} , fatigue-crack initiation life can be predicted in terms of the maximum alternating stress at the notch tip in elastic analysis. It is difficult to define the material constant (A'). (ΔC) and ($\Delta \epsilon$) which are calculated using finite element methods or by using the cyclic stress-strain curve and Manson-Coffin one for each N_{i} in elasto-plastic analysis. K_{f} and K_{f}^{P} parameters do not yield same accurcy for the prediction of the number of cycles N_{i} in terms of the parameter $\Delta K_{i}/\sqrt{\rho}$.

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TABLE _ I

							-			
CIMEN No.	ROOT RADIUS	LOAD ΔP (kg)	ΔK _{13/2} (kg/mm ²)	ΔΚ _J /V ρ (kg/mm ²)	ΔG_{max}^{N} kg/mm ²	Δσ _{max} kg/mm ²	∆ G _{nom} kg/mm ²	κ _t	κ ^N f	N. i (cycles)
2	<u> ମ</u> . ୦୨	160	18.88	84.44	46.40	95.28	5.6	17.014	8.34	11930
3	0.05	150	17.68	79.07	46.1	89.92	5.25 ·	16.99	8.78	18 800
4	0.04	126	14.85	74.28	38.58	83-82	4.41	19	8.75	11750
8	0.5	350	41.3	58.40	51.3	65.9	12.25	5.38	4.187	10710
9	0.5	120	14.5	20	17.57	22.58	4.2	5.37	4.185	140510+
10	0.5	450	53.1	75.10	53.39	67.61	15.75	4.29	3.39	8600
12	1	450	53.1	53.1	50.62	59.91	15.75	3.8	3.214	27750
13	1.5	250	29.5	24.09	23.89	27.18	8.75	3.106	2.731	400000 ++
14	1.5	500	59	48.18	47.79	54.36	17.5	3.106	2.731	27600
15	1.5	40	47.2	38.53	38.23	43.38	14	3.106	2.731	45450
18	2	600	70.8	50.06	50.88	56.49	21	2.69	2. 423	19450
19	2	450	53.1	37.55	38.16	42.37	15.75	2.69	2.423	178910
21	2.5	600	70.8	44.77	46.26	50.52	21	2.405	2.203	39750

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	∆K,/Vg	Δκ/εν9	Ni
	120	5.7 103	30 000
PARCON	132	6.3 10 ³	.20000
And	160	7.6 10 ³	10 000
MCNICOL	108	8.57 เ0 ³	5500
	208	9.9 10 ³	3000
	47.1	2.24 10 ³	81750
JACK	73.84	3.52 10 ³	46486
And	97.04	4.62 103	8720
	123	5.86 10 ³	5000
	154.7	7.36 10 ³	2000
	143	6.80 103	157 000
	165	7.85 103	52 000
	165	7.85 10	57 000
	165	7-85 lo ³	65000
VARDAR	208	9.9 10 ³	13000
	208	9.9 10 ³	14:000
	208	9.9 10 ³	20130
	208	9.9 (0 ⁻³	14 000
	42.7	3.85 10	³ 10 ⁶
	50	4.55 10	3 98000
	54.9	6.3 10	3 11 300
PEARSON	67.6	7.35 10	3 10250
	95.5	8.78 10	3 6400

TABLE-II









FIGURE-5.4

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