# A BIOSEQUENCE BASED DYNAMIC RIDE-MATCHING ALGORITHM THAT TAKES INTO ACCOUNT SOCIAL FACTORS 

by<br>Ömer Faruk Aydın<br>B.S., Civil Engineering, Boğaziçi University, 2011<br>M.S., Civil Engineering, Boğaziçi University, 2013

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# A BIOSEQUENCE BASED DYNAMIC RIDE-MATCHING ALGORITHM THAT TAKES INTO ACCOUNT SOCIAL FACTORS 

APPROVED BY:

# Assoc. Prof. Ilgın Gökaşar <br> (Thesis Supervisor) <br> Assist. Prof. Mustafa Gökçe Baydoğan 

Assist. Prof. Mehtap Işık

Assist. Prof. Gürkan Günay

Assist. Prof. Ahmet Yıldız

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#### Abstract

\section*{A BIOSEQUENCE BASED DYNAMIC RIDE-MATCHING ALGORITHM THAT TAKES INTO ACCOUNT SOCIAL FACTORS}

Increasing traffic congestion and advancements in technology have fostered the growth of alternative transportation modes such as dynamic ride-sharing. Smartphone technologies enable dynamic ride-sharing, which aims to establish ride matches between people with similar routes and schedules at short notice. Many automated matching methods are designed to improve system performance, such as minimizing process time, minimizing total system cost or maximizing total distance savings; however, the results may not provide the maximum benefits for the participants. In this dissertation, an attempt is made to develop an algorithm to optimize matches when considering participants' gender, age, employment status and social tendencies. A biosequence algorithm, namely the Needleman-Wunsch algorithm, is used to quantify the similarity of participants' itineraries. A stated preference survey was conducted among 604 students and members of staff at Turkish-German University in 2018. An extensive simulation study was then performed by utilizing the survey data to compare the performance of the proposed algorithm with that of traditional bipartite and optimization algorithms. The simulation results indicate that when compared to the traditional bipartite and optimization algorithms, the proposed algorithm significantly increases performance in terms of computation times and the potential success rate of the matches. A sensitivity analysis for the proposed algorithm is also performed.


## ÖZET

# SOSYAL FAKTÖRLERİ DİKKATE ALAN BİYOLOJİK DİziLíM hizalamasina dayali bír dĩnamik yolculuk eşleştirme algoritmasi 


#### Abstract

Artan trafik sıkışıklı̆̆ 1 ve teknolojideki gelişmeler dinamik yolculuk paylaşımı gibi alternatif yöntemlerin gelişmesine yol açmıştır. Akıllı telefon teknolojileri benzer rota ve zamanda seyahat edecek insanları kısa zaman zarfında eşleştirmeyi amaçlayan dinamik yolculuk paylaşımını mümkün kılmaktadır. Birçok otomatik eşleştirme algoritması işlem süresini, sistem maliyetini veya toplam mesafeyi en aza indirgemek gibi sistem performansını geliştirmek üzere tasarlanmıştır, ancak sonuçlar katılımcılar için en iyi faydayı sağlamayabilir. Bu tezde, katılımcıların cinsiyet, yaş, çalı̧̧ma durumu ve sosyalleşme isteklerini baz alan bir algoritma geliştirilmiştir. Katılımcıların rotaları arasında mevcut benzerlikleri bulmak için Needleman-Wunsch isimli bir biyodizilim algoritması kullanılmıştır. 2018 yılında Türk-Alman Üniversitesi'nde toplam 604 öğrenci ve personelle belirli tercih anketi yapılmıştır. Önerilen algoritmanın performansını geleneksel bipartit ve optimizasyon algoritmaları ile karşılaştırmak için anket verileri kullanılarak kapsamlı bir benzetim çalışması yapılmıştır. Simülasyon çalışasının sonuçları, önerilen algoritmanın geleneksel bipartit model ve optimizasyon algoritmalarına kıyasla işlem sürelerinde ve eşleşmelerin potansiyel başarı oranlarında önemli oranda artış sağladığını göstermiştir. Önerilen algoritmanın hassasiyet analizi de yapılmıştır.


## TABLE OF CONTENTS

ACKNOWLEDGEMENTS ..... iii
ABSTRACT ..... iv
ÖZET ..... V
LIST OF FIGURES ..... viii
LIST OF TABLES ..... xi
LIST OF SYMBOLS ..... xiii
LIST OF ACRONYMS/ABBREVIATIONS ..... XV

1. INTRODUCTION AND BACKGROUND ..... 1
1.1. Motivation ..... 1
1.2. History of Ride-Sharing ..... 3
1.3. Studies on Ride-Matching Algorithms ..... 4
1.3.1. Solution Approaches ..... 4
1.3.2. Objective Functions ..... 5
1.3.3. Parameters ..... 7
1.3.4. Assumptions ..... 10
1.3.5. Summary and Discussion on Ride-Matching Algorithms ..... 12
1.4. Motivation behind Utilizing Needleman-Wunsch Algorithm ..... 15
1.5. Contributions ..... 18
1.6. Organization of This Dissertation ..... 19
2. PROBLEM DEFINITION ..... 20
2.1. Feasible Match ..... 21
2.2. Matching Algorithm ..... 22
3. SOLUTION APPROACH ..... 25
3.1. Time Feasibility ..... 25
3.2. Route Feasibility and the Needleman-Wunsch Algorithm ..... 26
3.3. Joint Socialness Score (JSS) ..... 29
3.4. Matching Process ..... 30
4. DATA COLLECTION AND ANALYSIS ..... 34
4.1. Turkish-German University ..... 34
4.2. Survey Data ..... 35
5. SIMULATION STUDY ..... 40
5.1. Application of Other Matching Algorithms ..... 40
5.1.1. Traditional Weighted Bipartite Matching Algorithm ..... 40
5.1.2. The Optimization Algorithm with Social Parameters ..... 43
5.2. Performance of the Ride-matching Algorithms ..... 46
5.3. Quality of Matches ..... 48
6. SENSITIVITY ANALYSIS ..... 50
6.1. Regression Analysis ..... 50
6.2. Regression Analysis of Parameters ..... 51
6.2.1. Analysis for Ratio of Matched Riders ..... 52
6.2.2. Analysis for Computation Time ..... 59
6.2.3. Analysis for Average JSSs of Matched Pairs ..... 65
7. CONCLUSION \& DISCUSSIONS ..... 71
7.1. Summary of the Contributions ..... 71
7.2. Conclusions and Discussions ..... 72
7.3. Limitations of the Study ..... 74
7.4. Recommendations ..... 74
REFERENCES ..... 76
APPENDIX A: CAMPUS TRANSPORTATION SURVEY ..... 83
APPENDIX B: COMPUTATIONAL RESULTS ..... 85

## LIST OF FIGURES

Figure 1.1. Crude Oil Prices in last 30 years ..... 2
Figure 1.2. Occupancy Rates in Passenger Transport ..... 2
Figure 1.3. Time and space complexities of the Needleman-Wunsch (blue), Smith and Waterman (green) and Hirschberg (yellow). (A) Time complexities in miliseconds, (B) space complexities in bytes [1]. . . 18
Figure 2.1. Ride-sharing Schema for a Driver and several Riders. ..... 20
Figure 2.2. An Illustrative Graph with a Driver and four Riders ..... 22
Figure 3.1. Announcement Status Updating Algorithm. ..... 26
Figure 3.2. The Needleman-Wunsch Algorithm after the Generation of the S Matrix. ..... 28
Figure 3.3. The Needleman-Wunsch Algorithm after the Generation of the M Matrix. ..... 28
Figure 3.4. Needleman-Wunsch Algorithm to Check Route Feasibility. ..... 29
Figure 3.5. The Proposed Matching Process. ..... 32
Figure 3.6. Flowchart of the Proposed Matching Process. ..... 33
Figure 4.1. Location of the TAU Campus in Beykoz, Istanbul. ..... 34
Figure 4.2. Map of Istanbul and Meeting Points for Ride-Sharing. ..... 39
Figure 5.1. Weighted Bipartite Matching Algorithm. ..... 41
Figure 5.2. Flowchart of the Weighted Bipartite Ride-matching Algorithm. ..... 42
Figure 5.3. Optimization with Social Factors Algorithm. ..... 44
Figure 5.4. Flowchart of the Optimization Ride-matching Algorithm. ..... 45
Figure 6.1. Ratio of Matched Riders versus Number of Riders by Capacities of Drivers ..... 56
Figure 6.2. Ratio of Matched Riders versus Number of Riders by Rider Count. ..... 56
Figure 6.3. Ratio of Matched Riders versus Number of Drivers by Different Capacities. ..... 57
Figure 6.4. Ratio of Matched Riders versus Number of Matched Drivers by Rider Count. ..... 57
Figure 6.5. Ratio of Matched Riders versus Number of Matched Riders Reject- ing First Match. ..... 58
Figure 6.6. Ratio of Matched Riders versus JSS Limit. ..... 58
Figure 6.7. Computation Time versus Number of Riders by Capacities of Drivers. ..... 62
Figure 6.8. Computation Time versus Number of Riders by Rider Count. ..... 62
Figure 6.9. Computation Time versus Number of Drivers by Different Capacities. ..... 63
Figure 6.10. Computation Time versus Number of Matched Drivers by Rider Count. ..... 63
Figure 6.11. Computation Time versus Number of Matched Riders Rejecting First Match. ..... 64
Figure 6.12. Computation Time versus JSS Limit ..... 64
Figure 6.13. Average JSSs of Matched Pairs versus Number of Riders by Ca- pacities of Drivers. ..... 68
Figure 6.14. Average JSSs of Matched Pairs versus Number of Riders by Rider Count. ..... 68
Figure 6.15. Average JSSs of Matched Pairs versus Number of Drivers by Dif- ferent Capacities. ..... 69
Figure 6.16. Average JSSs of Matched Pairs versus Number of Matched Drivers by Rider Count. ..... 69
Figure 6.17. Average JSSs of Matched Pairs versus Number of Matched Riders Rejecting First Match. ..... 70
Figure 6.18. Average JSSs of Matched Pairs versus JSS Limit. ..... 70
Figure A.1. Campus Transportation Survey, Page 1. ..... 83
Figure A.2. Campus Transportation Survey, Page 2 ..... 84

## LIST OF TABLES

Table 1.1. Objective functions used in the literature ..... 7
Table 1.2. Parameters used in some ride-matching algorithms in the literature. ..... 10
Table 1.3. Assumptions made in the literature. ..... 12
Table 1.4. Some sequence matching algorithms and their characteristics [1,2]. ..... 16
Table 2.1. An illustrative example of the computation of the JSS ..... 23
Table 4.1. Descriptive results of the survey. ..... 35
Table 4.2. Social factors and related survey questions. ..... 36
Table 4.3. The average weights of the social parameters for the students. ..... 36
Table 4.4. The average weights of the social parameters for the faculty staff. ..... 37
Table 4.5. The average weights of the social parameters for the administrative staff. ..... 37
Table 4.6. The average weights of the social parameters for the other staff. . . ..... 37
Table 4.7. The average weights of the social parameters for all participants. ..... 38
Table 5.1. Performance of the ride-matching algorithms. ..... 47
Table 5.2. Quality of the matches. ..... 49
Table 6.1. Model summary of the regression for ratio of matched riders. ..... 53
Table 6.2. ANOVA of the regression for ratio of matched riders ..... 53
Table 6.3. Coefficients of the regression for ratio of matched riders. ..... 54
Table 6.4. Model summary of the regression for computation times. ..... 59
Table 6.5. ANOVA of the regression for computation times. ..... 59
Table 6.6. Coefficients of the regression for computation times ..... 60
Table 6.7. Model summary of the regression for average JSSs of matched pairs. ..... 65
Table 6.8. ANOVA of the regression for average JSSs of matched pairs. ..... 66
Table 6.9. Coefficients of the regression for average JSSs of matched pairs ..... 67
Table B.1. Coefficients of the regression for average JSSs of matched pairs ..... 86

## LIST OF SYMBOLS

| $a_{s}$ | Age of the participant $s$ |
| :--- | :--- |
| $c_{d}$ | Capacity (number of empty seats) of the vehicle of driver $d$ |
| $d$ | Driver |
| $d_{k l}$ | Distance from location $k$ to $l$ |
| $d_{l d_{i}}$ | Distance from location $l$ to $d$ |
| $d_{o_{i} d_{i}}$ | Distance from location $o$ to $d$ |
| $d_{o_{i} k}$ | Distance from location $o$ to $k$ |
| $d_{s}$ | Destination location of trip announcement $s$ |
| $D$ | Set of drivers |
| $e_{s}$ | Earliest departure time of trip announcement $s$ |
| $f$ | Flexibility in time |
| $g_{s}$ | Gender of the participant $s$ |
| $k_{r}$ | Rider Count of $r$ i.e. number of riders who want to travel |
| $l_{s}$ | with $r$ including $r$ |
| $M$ | Latest departure time of trip announcement $s$ |
| $n_{d}$ | Set of meeting points |
| $o_{s}$ | Route of driver $d$ |
| $P$ | Origin location of trip announcement $s$ |
| $r$ | Set of participants |
| $R$ | Rider |
| $T_{o d}$ | Set of riders |
| $T_{o d}^{E D}$ | Trip announcement |
| $T_{a}^{L D}$ | Eatiest departure time with origin $o$ and destination $d$ |
| $x_{a}^{r d}$ | Variable i.e. 1 if ages of $r$ and $d$ are same, 0 otherwise |


| $x_{g}^{\text {rd }}$ | Variable i.e. 1 if genders of $r$ and $d$ are same, 0 otherwise |
| :---: | :---: |
| $x_{w}^{r d}$ | Variable i.e. 1 if employment status of $r$ and $d$ are same, 0 otherwise |
| $x_{\sigma}^{\text {rd }}$ | Variable i.e. 1 if social tendency of $r$ and $d$ are same, 0 otherwise |
| $X_{\text {cod }}$ | Capacity of each driver's vehicle |
| $X_{j s s}$ | Joint social score limit |
| $X_{n o r}$ | Number of riders |
| $X_{\text {nod }}$ | Number of drivers |
| $X_{n r j}$ | Number of riders who reject first match |
| $X_{r c}$ | Rider count |
| $Y_{\text {com }}$ | Computation time |
| $Y_{j s s}$ | Average joint social scores of matches |
| $Y_{\text {romr }}$ | Ratio of matched riders |
| $\sigma_{s}$ | Socialness i.e. willingness to meet new people of participant |
|  | $s$ |
| $\sigma_{(i, j, k, l)}$ | Travel distance saving by rider $j$ is served by driver $i$ from |
|  | location $k$ to $l$ |
| $\gamma_{a}$ | Weight of the age |
| $\gamma_{g}$ | Weight of the gender |
| $\gamma_{w}$ | Weight of the employment status |
| $\gamma_{\sigma}$ | Weight of the socialness |
| $\gamma^{r d}$ | Joint socialness score of rider $r$ and driver $d$ |

# LIST OF ACRONYMS/ABBREVIATIONS 

| ANOVA | Analysis of Variance |
| :--- | :--- |
| JSS | Joint Socialness Score |
| LCS | Longest Common Subsequence |
| TAU | Turkish-German University |

## 1. INTRODUCTION AND BACKGROUND

### 1.1. Motivation

Every day traffic congestion worsens and the rate of global warming accelerates. These factors have negative impacts on economics and social life of the regions which suffer from them. Therefore, policy makers seek certain strategies for these factors in congestion management and reduction perspective.

There are some existing strategies in congestion management perspective in the literature, such as constructing new highways, maintaining current transportation infrastructure, utilizing current highway capacities, reducing the private car use by developing some methods, implementing Intelligent Transportation Systems (ITS) and integrating bicycle into existing transportation network and so forth [3-8]. However, each strategy comes with both benefits and costs. To evaluate the impact of each given strategy and decision, benefit/cost analysis is commonly used in the literature. In this methodology, the benefits and costs of these strategies are calculated by considering some evaluation models, such as subjective scorings, life cycle cost analysis and so forth $[9,10]$. Hence, the results can be used for the most appropriate decisions for benefits of the society. This dissertation mainly focuses on a methodology for the reduction in private car use.

Studies show that there is a significant shift from public transport towards the private vehicles despite rising fuel prices in EU-15 countries [11]. In Figure 1.1, it can be seen that especially after the year 2000, the crude oil prices has increased significantly.

While most vehicles can transport up to four passengers, the average passenger per vehicle ratio or private car occupancy rate in Europe was approximately 1.45 in 2015 (in Germany, 1.42; in the Netherlands, 1.38; and, in the UK, 1.58) [13]. Despite of low occupancy rates per vehicles, this value has continued decreasing as seen in Figure 1.2. Ride-sharing may have great potential in reducing traffic congestion.


Figure 1.1. Crude oil prices in last 30 years [12].


Figure 1.2. Occupancy rates in passenger transport [13].

Increase in number of private vehicles and decrease in occupancy rates of private vehicles led to increase in number of studies aiming to increase occupancy rates of private vehicles such as ride-sharing studies. Ride-sharing can be defined as matching riders, who have no vehicle, with the drivers, who have empty seats on their vehicles and have similar routes and time schedules. The applications of ride-sharing began during World War II and have continued to date.

### 1.2. History of Ride-Sharing

The history of ride-sharing goes back to the 1940s but the increasing use of smartphone devices and mobile applications has made ride-sharing more appealing [14-16]. The evolution of ride-sharing can be examined in five eras:

- The appearance of ride-sharing can be traced back to the 1940s, when it was done to conserve resources during World War II. At the time, the U.S. Office of Civilian Defense created a program called the "Car Sharing Club Exchange and Self-Dispatching System" to match riders and drivers via a bulletin board at their workplaces.
- The second era of ride-sharing occurred between the late 1960s and 1980, during the energy crisis.
- The third era of ride-sharing occurred in the 1980s and 1990s, when attempts at meeting transport demand focused on mitigating traffic congestion and improving air quality. However, there still existed a need for methods by which to match commuters at short notice.
- Later, the fourth era had come, in which ride-sharing systems focused on encouraging ride-sharing among commuters with the most reliable trip records. This era utilized the Internet for online matching and traveler information services.
- The fifth, current, era of ride-sharing includes the use of software packages, realtime services, financial incentives and social networking platforms [17]. This has resulted in a dramatic increase in dynamic ride-sharing studies in recent decades $[3,18]$.

Although advancement in technology in recent decades made building an advanced ride-sharing system possible, to-date critical mass for ride-sharing has not been achieved. There are many reasons for this fact, but automated ride-matching, which optimally matches riders and drivers in real-time, plays a key role to achieve critical mass in ride-sharing [3].

### 1.3. Studies on Ride-Matching Algorithms

Dynamic ride-sharing requires an automated matching system. This automated matching system brings riders and drivers with similar travel patterns and schedules together at very short notice. Dynamic ride-sharing systems are very complicated and require a great deal of attention of the researchers. Therefore, the success of a ridesharing system depends on successful implementation of ride-matching [18]. In the literature, a number of studies on ride-sharing systems have identified the characteristics of ride-matching problems and proposed solution methodologies [3, 19]. In this section, several dynamic ride-matching algorithms in the literature are outlined and their advantages, disadvantages and importance are discussed.

### 1.3.1. Solution Approaches

There are many ride-matching algorithms in the literature, which are created based on optimization approach. To overcome present challenges, operation research community addressed this problem by building different ride-sharing models. Dynamic ride-matching includes many parameters, rendering the problem non-deterministic polynomial-time hard (NP-hard) [20-22]. Therefore, many solutions to the ride-matching problem that have been proposed in the literature use heuristics or meta-heuristics [14, 20-28]. Although heuristic and meta-heuristic methods offer feasible processing times, they may not find the best possible matches. To be able to offer feasible solution approaches, some parameters such as social characteristics of the users and/or some transportation modes, such as multiple rider or multi-hop, are omitted in these problems. There are some algorithms in the literature, which considers these parameters and modes, but most of these studies did not consider computation times. As a
result, there is still need for ride-matching algorithms, which are compatible with the real-life situations and that can be solved at reasonably short notice.

To maximize system benefits, a previous study has proposed a novel approach to solve the ride-matching problem by modeling it using a traditional maximum-weight bipartite matching algorithm [15]. This algorithm is based on a single rider-single driver match. It is demonstrated that the weighted bipartite matching algorithm can be used for ride-matching; however, this algorithm requires long processing times because it calculates distance savings for each rider-driver pair to determine distance savings. The algorithm also omits multiple riders-single driver matches and ignores individual preferences to simplify the problem. Rolling horizon approach is introduced to force the matching algorithm to postpone finalization of the previously found matches until a deadline specified by the users. This technique aims to increase the number of matches [15]. The rolling horizon would not encourage people to be included in ridesharing systems; even should users specify a deadline for their travel request, they do not like to wait long [29]. This algorithm is extended by adding meeting points to increase the number of matches [30]. The algorithm allows multiple riders-single driver matches if the riders are waiting at the same location.

### 1.3.2. Objective Functions

Ride-sharing offers many advantages to the participants such as decreasing their travel time and cost. Ride-sharing also causes important system-wide benefits such as increase in occupancy rates in private vehicles and decrease in use of private vehicles. Many studies in the literature have employed one of the following objectives to solve ride-matching problems:

- Maximizing total distance savings [15, 31-33]. Total distance savings represent the difference in vehicle-miles driven by all participants when they drive alone and when they share ride. This objective is important because it is directly related to the objective of reducing air pollution. It is also directly proportional to the objective function of minimizing travel cost.
- Minimizing total travel time [34]. Total travel time defines the sum of travel times of the ride-sharing participants while travelling from their origin to destination locations. This is also related to the air pollution because vehicle emission is not only related to travelled distance but also vehicle speeds.
- Minimizing total travel cost [35,36]. Total travel cost is the sum of the travel costs of all ride-sharing participants. Ride-sharing allows its participants to share their travel costs. This is an important parameter that can be an incentive for riders and drivers to be included in a ride-sharing system. Additionally, this would encourage private ride-share providers to build ride-sharing systems because they can make profit by taking a commission from each match they create.
- Maximizing number of matches [35-37]. This objective is used to increase number of satisfied participants. More satisfied participants may attract even more participants into a ride-sharing system, so this is an important indicator to achieve critical mass.
- Minimizing total waiting and delay time [28]. Total waiting and delay time is one of the reason people don't want to be included in a ride-sharing system. Therefore, this objective function aims to increase participation rate by minimizing participant inconvenience.

Most of the objective functions used in the literature focused mainly on systemwide benefits, whereas, potential participants in real-life wish to maximize individual benefits. This is an important challenge to overcome in order to apply the ride-matching algorithms in real-life. For example, a driver may want to be matched with a rider at the same gender even if another rider is better for maximizing distance savings or minimizing system-wide travel cost. To the best of writer's knowledge, social parameters are used in ride-matching algorithm as constraints [38], but they are not used in objective functions. In Table 1.1, objective functions used in some ride-matching algorithms in the literature are presented.

Table 1.1. Objective functions used in the literature.

| Reference | Objective function |
| :--- | :--- |
| Agatz et al. (2011) [15] | Maximizing total travel distance savings |
| Cheikh and Hammadi (2016) [28] | Minimizing total waiting and delay times |
| Ghoseiri et al. (2011) [38] | Maximizing total number of matches |
| Masoud and Jayakrishnan (2017) [14] | Maximizing total number of matches |
| Najmi et al. (2017) [23] | Maximizing total number of matches |
| Stiglic et al. (2015) [30] | Maximizing total number of matches |
| Wang et al. $(2017)[39]$ | Maximizing total travel distance savings |

### 1.3.3. Parameters

Many parameters were used in ride-matching algorithms to present real-life instances. There were some parameters naturally used in all algorithms. Announcement time of a ride-sharing request, origin and destination locations, earliest departure time, latest arrival time or latest departure time are some examples to these parameters. On the other hand, there are parameters, which are only used in some of the algorithms. A literature review on use of these parameters are demonstrated in Table 1.2. Some examples to these parameters are as follows:

- Joint rider. In many ride-matching algorithms, it is assumed that a driver is matched with a rider at a time, while, in some other algorithms, multiple riders who wish to travel together can be matched with a driver. This parameter may decrease safety concerns of many participants [3]. This parameter can be used in different ways.
(i) Stiglic et al. [30] used joint rider parameter in their algorithm to present two different riders waiting at the same meeting point. These multiple riders can be matched with a driver together only if it is the most feasible match. Otherwise, these riders can be matched with different drivers as well.
(ii) Cheikh and Hammadi [28] assumed that joint rider can be used for riders, who want to travel together. In their algorithm, this parameter is determined by riders and these riders cannot be separated by the algorithm.
- Time flexibility. This parameter is used in many algorithms to represent flexibility of participants in their schedule. In ride-matching algorithms, it is calculated as follows:

$$
\begin{equation*}
f=\left(T_{o d}^{L A}-t_{o d}\right)-T_{o d}^{E D}, \tag{1.1}
\end{equation*}
$$

where $T_{o d}^{L A}, t_{o d}$ and $T_{o d}^{E D}$ represent latest arrival time, travel time from origin to destination location and earliest departure time, respectively. To use this formula, earliest departure time from origin location and latest arrival time to the destination location are specified by the participants. Travel time is calculated by dividing travel distance to an average speed. In other words, calculation of travel time requires an average speed assumption that may be not feasible because of ever-changing traffic conditions.

- Allowable waiting time. Waiting time is one of the crucial parameters that can be used in a ride-matching algorithm. Ghoseiri et al. [38] used allowable waiting time parameter, which is specified by participants, instead of calculating time flexibility. Masoud and Hammadi [14] also used allowable waiting time as a constraint in addition to time flexibility.
- Social parameters. These parameters can be used in ride-matching algorithms to represent characteristics and choices of the participants. While most of the ride-matching algorithms focus on the system-wide benefits, participants consider their own benefits to overcome security concerns, to enjoy ride-sharing or any other social reasons. For example, a participant may want to be matched with another participant at the same gender or close to his/her age. These social parameters can represent age, gender, pet restrictions, smoking restrictions, employment status or willingness to meet new people, i.e. socialize. Social parameters are very important in real-life; however, these parameters are omitted in most of the ride-matching algorithms. This is mostly because, considering
these parameters brings an important computational burden to the algorithms. Ghoseiri et al. [38] utilizes social parameters, namely gender, age, pet restrictions and smoking, in their optimization model as constraints, but they did not offer a solution approach to their model.
- Acceptable walking distance. This parameter was used for riders, who agree to walk to some predetermined meeting points. This parameter causes increase in participation rate, because this gives a chance to the drivers, who are not willing to change their routes, to be included in a ride-sharing system. Additionally, it is sometimes hard for drivers to find a specific location given by riders, so meeting points can be helpful to overcome this challenge. On the other hand, meeting points are very advantageous for riders, who do not want to reveal their home addresses for security reasons.
- Acceptable detour distance. This parameter is similar to acceptable walking distance. In this case, a driver submits this parameter to specify how much they are willing to change their route to pick a rider up.
- Number of allowable transfers. This parameter was used in ride-matching algorithms, in which multi-hop ride-matching was allowed. This parameter is specified by riders to represent how many times they are willing to change their transport vehicle. This parameter is included in ride-matching algorithms as a constraint.

Some ride-matching algorithms and parameters used in these algorithms are summarized in Table 1.2. In the algorithms presented in Table 1.2, joint rider parameter did not get enough attention. Time flexibility was widely used, yet, travel times were assumed to be known or calculated by dividing travel distance to an average speed. Nevertheless, assumption of known travel time or average speed would not reflect situations in real-life. Therefore, time flexibility should be considered carefully. Ghoseiri et al. [38] used allowable waiting time parameter specified by the participants instead of time flexibility. Masoud and Jayakrishnan [14] used time flexibility and allowable waiting time together as constraints. Social parameters were only used by Ghoseiri et al. [38] as constraints, despite the fact that social parameters are seen as very important to achieve critical mass [3]. Concept of meeting points, presented in algorithms of

Ghoseiri et al. [38] and Stiglic et al. [30], requires additional parameters such as acceptable walking distance and acceptable detour distance. When multi-hop ride-sharing is allowed, number of allowable transfer can be limited as seen in the algorithms of Ghoseiri et al. [38] and Masoud and Jayakrishnan [14].

Table 1.2. Parameters used in some ride-matching algorithms in the literature.

| Reference | Joint rider | Time flexibility | Allowable waiting time | Social parameters | Acceptable walking distance | Acceptable detour distance | Number of allowable transfers |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Agatz et al. (2011) [15] | x | Yes | x | X | X | x | x |
| Ghoseiri et al. (2011) [38] | x | X | Yes | (*) | Yes | Yes | Yes |
| Masoud and Jayakrishnan (2017) [14] | x | Yes | Yes | X | X | (**) | Yes |
| Cheikh and Hammadi (2016) [28] | Yes | Yes | X | X | X | x | X |
| Najmi et al. (2017) [23] | X | Yes | X | X | X | X | X |
| Wang et al. (2017) [39] | X | Yes | X | x | X | X | X |
| Stiglic et al. (2015) [30] | Yes | Yes | x | x | Yes | Yes | X |
| (*) Used as constraints. |  |  |  |  |  |  |  |
| (**) Used but not limited. |  |  |  |  |  |  |  |

### 1.3.4. Assumptions

Real-life is very complicated to fully represent it in an algorithm. Therefore, many assumptions should be made while constructing an algorithm to be able to solve them in feasible time. Some assumptions made in the investigated ride-matching algorithms are as follows:

- Rolling horizon approach. Rolling horizon approach forces the matching algorithm to postpone finalization of the previously found matches until a deadline specified by the users. This technique aims to increase the number of matches by including future ride requests in the matching algorithm.
- Flexible rider-driver role. This approach assumes that a driver can accept to be a rider instead of a driver if a tempting request is offered. This is possible in real-life no matter the possibility is low or not. Many algorithms omitted this assumption and assumed fixed rider-driver role, because the flexibility in roles brings significantly large burden to computations.
- Rider relocation. Some algorithms assumed that riders walk to some meeting points for ride-sharing. This way, they can meet with a driver on the driver's routes or at least closer to driver's route that is acceptable by the driver. Thus, participation rate can be increased.
- Driver detour. Many algorithms assumed that drivers change their route at an acceptable level to meet with riders.
- Known travel time. This assumption was made by some researchers to calculate a time flexibility for the participants. As mentioned in the preceding section, this assumption can be considered as weak due to ever-changing traffic conditions.
- Matching rule. This is an assumption to describe single rider-single driver, multiple riders-single driver or single rider-multiple drivers matches. Single rider-single driver match is preferred to ease computational burden. In this scenario, a driver is assumed to be matched with single rider. Some researchers achieved to match a driver with multiple riders. In this case, capacity of the driver, i.e. number of empty seats in the vehicle, should be more than the number of drivers. In a single rider-multiple drivers match, namely multi-hop match, riders are assumed to transfer between vehicles to reach their destinations.
- Multi-modal. This assumption refers to the case, where ride-sharing is combined with public transportation. In other words, riders use ride-sharing option to reach a point, where they can transfer to public transportation. This may lead to increase in matching rate. There is still a need for studies that combine ridesharing and public transportation.

Some assumptions made in the literature is summarized in Table 1.3. In Table 1.3 , it is seen that rolling horizon approach, which forces participants to wait until a deadline specified by them, was widely used; however, the participants would not want
to wait a long time to be matched even if they give a deadline [29]. Ghoesiri et al. [38] did not use rolling horizon approach but they did not offer any solution approach to their model either. Cheikh and Hammadi [28] and Stiglic et al. [30] did not use rolling horizon approach either but they also did not offer an alternative approach. Flexible rider-driver role was proposed by Agatz et al. [15] but in their study computation times were ignored. Rider relocation was used in the studies, in which meeting points were assigned. In all investigated algorithms drivers detour to meet riders at riders' origin locations or meeting locations. Most of the studies assumed travel times are known or can be calculated with an average speed, whereas, Ghoseri et al. [38] used travel distance and waiting times specified by participants. Most of the algorithms allowed multiple riders-single driver match, while some of them also allowed multihop matching for riders. On the other hand, none of these algorithms constructed a multi-modal matching system.

Table 1.3. Assumptions made in the literature.

| Reference | Rolling horizon | Flexible rider-driver role | Rider relocation | Driver detour | Known travel time | Matching <br> rule | Multi-modal |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Agatz et al. (2011) [15] | Yes | Yes | x | Yes | Yes | SS | x |
| Ghoseiri et al. (2011) [38] | x | x | Yes | Yes | x | MS, SM | x |
| Masoud and Jayakrishnan (2017) [14] | Yes | x | Yes | Yes | Yes | MS, SM | x |
| Cheikh and Hammadi (2016) [28] | x | x | x | Yes | Yes | MS, SM | x |
| Najmi et al. (2017) [23] | Yes | x | x | Yes | Yes | SS | x |
| Wang et al. (2017) [39] | Yes | x | x | Yes | Yes | MS | x |
| Stiglic et al. (2015) [30] | x | x | Yes | Yes | Yes | MS | x |
| SS: Single rider-single driver, MS: Multiple riders-single driver, SM: Single rider-Multiple drivers. |  |  |  |  |  |  |  |

### 1.3.5. Summary and Discussion on Ride-Matching Algorithms

Ride-matching algorithms, which match drivers, who owns a vehicle with empty seats, with riders, who look for a vehicle to ride, are at the center of ride-sharing
systems. In this section, some ride-matching algorithms in the literature were investigated. Objective functions and parameters used in these algorithms were examined, as well as, their solution approaches and assumptions made to construct these algorithms. The aim was to present challenges and opportunities to construct a successful ride-matching algorithm.

It was concluded that there are some broad areas for researches:

- Objective functions, which should be defined to reflect real-life concerns.
- Parameters, which consider variables faced in the real-world while maintaining feasible computation times.
- Assumptions, which offer solvable ride-matching algorithms while considering facts, which are important for participants.

Objective functions are the main components of a ride-matching algorithms that help decide which rider will be matched with a driver or vice versa. Past attempts to make ride-sharing popular among people have failed to achieve critical mass [17]. Therefore, objective functions should be determined such that more people would be willing to involve in a ride-sharing system. Many of the investigated ride-matching algorithms focused on system-wide benefits such as maximizing total travel distance savings or number of matched participants. There is an algorithm among the investigated studies, which used objective function of minimizing total waiting and delay time for the convenience of the participants but this objective alone may not be sufficient to attract enough people into a ride-sharing system. It is concluded that new objective functions, which consider primarily benefits of users, are needed. There is no point of maximizing system benefits if there are not enough participants in a ride-sharing system to be consistent.

Parameters used in ride-matching algorithms play a key role for algorithms to be successful. More parameters will lead to increase in computation times, but eliminating more than enough parameters will cause algorithms to be deficient. It is concluded that there is a need to determine the importance of parameters used in ride-matching
algorithms. For example, joint rider parameter, which represents riders, who are willing to travel together, presents a real-life request because many riders may want to travel with their friends for social reasons and security reasons. Including this parameter in a ride-matching algorithm may increase participation rate; however, this parameter may also bring computational burden. Therefore, the advantages and disadvantages of such parameters should be investigated and supported with numerical studies. Furthermore, social parameters were not included in most of the investigated studies. Social parameters are used in one study among them [38], but they are only used in the constraints. In this study, participants' choices are asked and matches are finalized based on their answers. For example, if a rider asks to be matched with a driver at the same gender, the algorithm eliminates the drivers who do not satisfy this condition. This can be seen as a positive outcome, but this also causes decrease in matching ratio. As a result, alternative methods can be developed such that an algorithm can consider social parameters and when there are no better options, the algorithm can offer matches to the participants even if these constraints are not satisfied. There is also a need for studies, which assess the effects of including social parameters on performance of such algorithms.

Each ride-matching algorithm should make some assumptions to solve the matching problem at feasibly short notice. Rolling horizon approach was proposed to increase matching rate by making finalization of the matching until a deadline to include newarriving requests in the system. This approach causes increase in waiting times for the participants, which may cause decrease in satisfaction ratio. Alternative approaches can be studied in future studies.

As a conclusion, there are still many remained challenges for the ride-matching algorithms that will provide great research opportunity. A successful ride-matching algorithm may play a key role to achieve critical mass in ride-sharing. Especially, demands of participants, who are the main reasons to construct ride-sharing systems, should be investigated carefully. Advanced ride-matching algorithms should be developed to satisfy the needs of the participants.

### 1.4. Motivation behind Utilizing Needleman-Wunsch Algorithm

To be able to match drivers with riders, drivers are required to go to riders' origin location or suitable meeting points. For this reason, either drivers should change their routes to pick up riders or riders should wait at a point that is located on drivers' routes. When drivers change their route to pick up riders, only the single rider-single driver match option is available unless dynamic routing for drivers is utilized. Dynamic routing brings significant computational burden that may result in infeasible computation times. Consequently, to allow multiple riders-single driver match, drivers' routes should be fixed to maintain feasible computation times. This can be achieved by asking drivers which routes they choose before the beginning of their travels or assigning the shortest path to their destination for them.

In this dissertation, due to lack of data regarding routes of potential drivers, drivers are assumed to choose the routes assigned for them, which are the shortest path to the destination locations. Riders are assumed to agree on going to the meeting locations, which are located on drivers' routes and available for vehicles to pick up riders. Meeting points are represented by letters. Thus, routes of drivers are represented by letter arrays. If the origin and destination points of a rider are located on a driver's route, then route feasibility for the rider and the driver are satisfied. To create an automated ride-matching, sequence analysis should be done for aligning routes and meeting locations represented by letter arrays.

Recent decades, bioinformatics community has addressed longest common subsequence (LCS) problem. They use sequence analysis to find and score the similarities between a sample amino acid chain and amino acid chains of known proteins [40]. The LCS problem is studied under alignment algorithms created by Needleman-Wunsch [41]. They presented the first systematic tool to consider the insertion and deletion of letters from a letter array that naturally occurs in biological sequences [42]. NeedlemanWunsch algorithm is one of first examples of dynamic programming and still widely used. It is an exact matching algorithm, so it is widely preferred especially when the quality of alignment is of the utmost importance [2].

When sequence alignment algorithms are considered, performance and scalability become more critical as input sizes increase. Therefore, computational complexity of sequence alignment algorithms should be investigated in terms of time and space. This can be measured by examining computation time and memory consumption, which are referred as time complexity and space complexity, respectively [1]. To determine the efficiency of an algorithm, an upper bound on the asymptotic growth rate of the algorithm, "O", is used. Let $\mathrm{X}[1 \ldots \mathrm{n}]$ and $\mathrm{Y}[1 \ldots \mathrm{~m}]$ be two letter arrays with the length of $m$ and $n$, respectively. If it is known that a sequence alignment algorithm has an upper bound of mxn in its worst case, it is referred as $\mathrm{O}(\mathrm{mxn})$. $\mathrm{O}(\mathrm{mxn})$ means that as input size increases, the worst case running time of the algorithm will increase with a rate proportional to mxn. Time and space complexity of some sequence alignment algorithms and their main characteristics are given in Table 1.4. In this table, $m$ and $n$ are lengths of sequences and $m$ is bigger than $n$.

Table 1.4. Some sequence matching algorithms and their characteristics [1,2].
\(\left.$$
\begin{array}{|l|c|c|c|c|}\hline \text { Algorithm name } & \begin{array}{c}\text { Preprocess time } \\
\text { complexity }\end{array} & \begin{array}{c}\text { Search time } \\
\text { complexity }\end{array}
$$ \& \begin{array}{c}Space <br>

Complexity\end{array} \& Characteristics\end{array}\right]\)| Global alignment. |
| ---: |
| Needleman Wunsch |

In this dissertation, sequence alignment algorithm is used to check if the origin and destination locations of a rider are covered by route of a driver. Therefore, length of sequence for a rider is always two and length of sequence for a driver's route equals to or bigger than two. Some characteristics of route alignment are as follows: (a) A letter occurs only once in a route sequence, because a driver would visit the same location only once, (b) to verify a driver's route covers both origin and destination locations of a rider, all letters should be compared, so an exact matching algorithm should be utilized, (c) Trace-back process is not needed, because to check origin and destination are covered by a route, only the score of the algorithm is needed, (d) gaps and mismatchings should not be penalized. Based on these characteristics of route alignment used in this dissertation, algorithms that utilizes heuristics, such as Boyer-Moore, are not applicable for route alignment problem. Among the rest of the algorithms presented in Table 1.4, affine gap penalty is less efficient than NeedlemanWunsch, Smith and Waterman and Hirschberg by means of time and space complexity. The remaining three algorithms have the same time complexity. Since, trace-back process is not required for route alignment, these three algorithms can be considered. In the literature, a simulation study was conducted to show time and space complexity of these algorithms [1]. Figure 1.3 depicts the time and space complexities of these algorithms under different size of inputs.Figure 1.3 shows that the Hirschberg resulted in good performance of space complexity, whereas, the Needleman-Wunsch algorithm resulted in the best time complexity. As a result, the Needleman-Wunsch algorithm is selected for route alignment for the following reasons:

- It is one of the most used and basic algorithms in bioinformatics over decades.
- It is an exact sequence alignment algorithm that is a required characteristic for route alignment.
- It resulted in the best time performance compared to its competitors, namely Smith and Waterman and Hirschberg, which satisfy other conditions for route alignment.


Figure 1.3. Time and space complexities of the Needleman-Wunsch (blue), Smith and Waterman (green) and Hirschberg (yellow). (A) Time complexities in miliseconds, (B) space complexities in bytes [1].

### 1.5. Contributions

In this dissertation, a novel ride-matching algorithm is proposed to overcome the aforementioned challenges. In other words, a ride-matching algorithm is developed that optimizes matches between drivers and riders by considering their characteristics and choices at a reasonably short notice. The main contributions of this dissertation to the literature can be summarized as follows:

- In the proposed algorithm, to identify similarities among the travel patterns of users, the routes of the drivers are assumed to be fixed. Suitable riders are identified using a sequence alignment algorithm, namely the Needleman-Wunsch algorithm. The Needleman-Wunsch algorithm is widely used in the bioinformatics field to identify similarities between a sample amino acid chain with amino acid chains recorded in a database [43]. The basic function of the Needleman-Wunsch algorithm is to align arrays of letters and rate their similarity [41]. In recent years, this algorithm has been used in social and geographical studies. In such
studies, travel or activity patterns are presented as arrays of letters comparable to amino acid chains [44, 45]. In the proposed algorithm, the routes of the users are presented as arrays of letters, and the similarity between these arrays is scored to find feasible matches.
- The characteristics and choices of users, such as gender, age, employment and tendency to meet new people, are included in the objective function of the proposed algorithm. Similar parameters have been presented in the literature as constraints [38]. In the proposed algorithm, the similarities between these parameters are scored by multiplying their weights assigned by participants. Using this approach, a rider can be matched with a driver even should some of the passengers' choices are not completely satisfied, as long as the match is still acceptable.


### 1.6. Organization of This Dissertation

This dissertation is structured as follows. In Chapter 2, defines the problem and introduces the ride-sharing model. In Chapter 3, the solution approach for this ridesharing model is outlined, and the application of the Needleman-Wunsch algorithm in this study is also described. Chapter 4 presents the evaluation of the survey outcomes. In Chapter 5, a simulation study is performed using the data acquired from the survey. Furthermore, simulation studies using a traditional weighted bipartite matching algorithm and an optimization algorithm that includes social factors are conducted, and performance of the proposed algorithm is compared with that of these algorithms. In Chapter 6, details of the sensitivity analysis performed for the proposed algorithm are described and results of the analysis are evaluated. Chapter 7 concludes the dissertation by summarizing the results of this study.

## 2. PROBLEM DEFINITION

The main objective in attempting to solve the ride-matching problem is to find the most feasible matches between riders and drivers. Figure 2.1 depicts an example of a ride-sharing schema. The letters, namely A, B, C, D, E, F and G, represent the locations. In this example, driver $d 1$ has origin and destination locations "A" and "E", respectively. Rider $r 1$ wishes to travel from "C" to "E", rider $r 2$ from " B " to " D ", rider $r 3$ from "C" to "E" and rider $r 4$ from " $F$ " to "E." The driver may choose to be matched with some of the riders based on their route and characteristics.


Figure 2.1. Ride-sharing schema for a driver and several riders.

The ride-sharing system contains a set of participants $P$. These participants are divided into two groups: a set of drivers $D$ and a set of riders $R$. Each rider and driver make a trip announcement which defines their travel requests. A set of trip announcements $S$ is defined such that $R \subset S$ and $D \subset S$. Each trip announcement $s \subset S$ is associated with origin and destination locations $o_{s}$ and $d_{s}$.

It is assumed that drivers do not change their prespecified routes. Thus, routes are assigned for the drivers based on their origin and destination locations. To check time feasibility, it is assumed that riders will wait past their latest departure time as long as they know a driver is coming for them. Therefore, the earliest departure time $T^{E D}$ and the latest departure time $T^{L D}$ are assigned for each announcement. The latest arrival time and travel time, which are used in traditional optimization algorithms, are
ignored, because time suitability is checked with announcement and allowable waiting times.

In this algorithm, each rider $r \in R$ specifies the rider count $k_{r}$, that is, the number of riders willing to travel together as a rider group. For example, a single rider's rider count value is one, whereas two friends, who are willing to travel together in the same vehicle, have a rider count value of two. Each driver $d \in D$ specifies his or her capacity, that is, the number of empty seats $c_{d}$. A novel aspect of this algorithm is the objective function, which maximizes participants' benefits by considering their characteristics and choices. Shaheen et al. [46] suggest that gender, age and employment status are key drivers of ride-sharing. The proposed algorithm uses the following four parameters and their respective weights to define the benefits of the participants: gender $g_{s}$; age $a_{s}$; employment status $w_{s}$; socialness or willingness to meet new people, $\sigma_{s}$; gender weight $\gamma_{g}$; age weight $\gamma_{a}$; employment status weight $\gamma_{w}$; and socialness weight $\gamma_{\sigma}$. In previous studies, the trip preferences of both drivers and riders, including age, gender, smoking preference and pet restrictions, were incorporated as constraints; however, these are not used in the objective functions $[23,38,47]$.

### 2.1. Feasible Match

A match between a rider and a driver can be considered feasible if their routes and schedules are similar. These similarities are defined as spatial and temporal constraints, respectively. Additional constraints, such as distance savings that are prioritized in traditional weighted bipartite matches can be defined for feasible matches, as long as spatial and temporal constraints are satisfied.

The proposed algorithm assumes that a driver can pick up riders at meeting points located on the driver's route. In the example given in Figure 2.1, driver $d 1$ plans to travel from point "A" to "E", and rider $r 1$ wishes to travel from "C" to "D". The best route for the driver is "ABCDE." The match between $d 1$ and $r 1$ is defined as spatially feasible, as the route of driver $d 1$ contains both the origin and the destination of rider $r 1$.

To verify time feasibility, drivers and riders specify their latest departure times. It is assumed that when a rider specifies a latest notification time of 15 minutes and a driver responds to this call within this time range, the match can be defined as temporally feasible. This is true even if a rider has to wait more than 15 minutes, as riders can wait more than 15 minutes should they know that a driver is coming to pick them up.

### 2.2. Matching Algorithm

To match riders with the most feasible drivers, arcs are created between each rider and spatially and temporally feasible drivers. The illustrative graph in Figure 2.2 represents the sample case presented in Figure 2.1. In Figure 2.2, the numbers on the edges denote the joint socialness score (JSS). The JSSs are calculated using social parameters and parameter weights. It is assumed that driver $d 1$ is taking the "ABCDE" route, which includes the origins and destinations of riders $r 1, r 2$ and $r 3$. Therefore, arcs are only created for these pairs and not for $r 4$, whose origin and destination are not on the driver's route.


Figure 2.2. An illustrative graph with a driver and four riders.

The objective of the proposed algorithm is to maximize the benefits of both the riders and the drivers. The benefits are measured with JSSs.

The objective function for each rider $r$ becomes

$$
\begin{equation*}
\operatorname{maximize} \quad \gamma^{r d}=x_{g}^{r d} \gamma_{g}^{r} \gamma_{g}^{d}+x_{a}^{r d} \gamma_{a}^{r} \gamma_{a}^{d}+x_{w}^{r d} \gamma_{w}^{r} \gamma_{w}^{d}+x_{\sigma}^{r d} \gamma_{\sigma}^{r} \gamma_{\sigma}^{d} . \tag{2.1}
\end{equation*}
$$

In Equation 2.1, weights of the social factors of the rider $r$ and his or her feasible driver $d$, specifically gender weight $\gamma_{g}$, age weight $\gamma_{a}$ and employment status weight $\gamma_{w}$, are multiplied to calculate the JSS, $\gamma_{r d}$. The variable $x$ is positive one if the social characteristics are the same and negative one if they are different. The objective function is calculated separately for each rider. First, the objection function of the rider with the earliest trip announcement time is calculated. After this rider is matched using the objective function, the next rider is selected, and the process is repeated. A sample calculation of the JSS is presented in Table 2.1, which presents the characteristics of driver $d 1$ and rider $r 1$. It is assumed that all users want to be matched with a user with similar characteristics. The weights are obtained from the users, who are asked to rate the weights of each social factor from zero to five. A rating of zero indicates that it is not important to be matched with a user with the same social characteristic; a rating of five indicates that being matched with a similar user is very important.

Table 2.1. An illustrative example of the computation of the JSS.

|  | Driver $d 1$ |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Characteristics | Weight | Characteristics | Weight | $x_{r d}$ | Scores |
| Gender | male | 1 | female | 5 | -1 | -5 |
| Age | $18-25$ | 3 | $25-40$ | 4 | -1 | -12 |
| Employment | TAU | 4 | TAU | 4 | 1 | 16 |
| Socialness | Yes | 5 | Yes | 3 | 1 | 15 |
| Total score |  |  |  |  |  | 14 |

In the example given in Table 2.1, driver $d 1$ is a male driver with an age of between 18-25 who works at the TAU. Driver $d 1$ states that the weights of a rider's gender, age range and working place are one, three and four out of five, respectively. Driver $d 1$ also states that he is willing to meet new people with an weight factor of five. In contrast, rider $r 1$ is a female with an age of between 25-40 who also works at TAU. Her weight factor for willingness to meet new people is three. As mentioned previously, the variable $x_{r d}$ is assigned a value of positive one if characteristics are the same and negative one otherwise. In this situation, the value of $x_{r d}$ is negative one for gender and age because the driver and the rider's gender and age range are different. The value of $x_{r d}$ is positive one for employment and socialness because they are working at the same location and they are both willing to meet with new people. The score for gender becomes $1 x 5 x(-1)=(-5)$. When the scores of the other social characteristics are calculated in this way, the JSS can be calculated by simply adding all of these scores.

In order to find the feasible matches for a rider, a capacity constraint should be checked. For the proposed algorithm, the number of empty seats available in the driver's vehicle, $c_{d}$, should be greater than the rider count, $k_{r}$. For example, if riders $r 1$ and $r 2$ are a married couple and want to travel together, only one of them request a ride. The rider count of this couple is two, and they cannot be matched with a driver with only one empty seat. To satisfy this constraint, the following equation is included in the proposed algorithm:

$$
\begin{equation*}
c_{d} \geq k_{r} \tag{2.2}
\end{equation*}
$$

## 3. SOLUTION APPROACH

One of the most significant barriers in ride-matching problems is dealing with large number of participants within a feasible time period [3]. In this section, the approach adopted to solving the defined ride-matching problem is discussed.

### 3.1. Time Feasibility

In the algorithm proposed in this dissertation, the earliest and latest departure times specified by the participants are used to analyze time feasibility. Therefore, traditional time constraints are not used in the matching algorithm. Instead, a status factor is defined for each participant to determine whether the request for a ride that he or she makes is active or passive. As mentioned previously, it is assumed that even if a driver arrives at the meeting location after a rider's latest departure time, the rider will still wait for the driver if they are matched between the specified earliest departure time and the latest departure time.

Many traditional optimization algorithms [15,39] calculate time flexibility $f$ using travel times $t_{o d}$, earliest departure time $T^{E D}$ and latest arrival times $T^{L A}$ as shown in Equation 1.1, where, the value of $t_{o d}$ is calculated using the average speed of the vehicles.

Instead of travel and latest arrival times, the earliest and latest departure times are used in the proposed algorithm. This approach is adopted because travel times vary greatly in metropolitan cities, especially during peak hours, and these time calculations impose a significant computational burden on the computer software. Therefore, an algorithm (Figure 3.1) was created to check the announcement status based on the given earliest and latest departure times of a participant. This algorithm is run every minute and updates the values of announcement activeness.

```
\(T^{E D}=\) earliest departure time specified by the participant
\(T^{L D}=\) latest departure time specified by the participant
if \(T^{E D}<\) current time \& current time \(<T^{L D}\) then
    Participant Status \(="\) active \("\)
else
    Participant Status \(=\) "passive"
end if
```

Figure 3.1. Announcement status updating algorithm.

### 3.2. Route Feasibility and the Needleman-Wunsch Algorithm

In the proposed algorithm, drivers' routes are assumed to be prespecified and fixed because they are not willing to change their prespecified routes [48]. Therefore, to satisfy the route feasibility constraint, a rider's origin and destination locations should be on the driver's route. The route of each driver $n_{d}$ is determined based on the driver's origin and destination locations, and a set of meeting locations $M$ are defined.

In the example given in Figure 2.1, it is clear that driver $d 1$, who wants to travel from point "A" to point "E," will use the route "ABCDE." Driver $d 1$ can be matched with riders $r 1, r 2$ and $r 3$ because their origins and destinations are located on the driver's route. However, an algorithm is required to find the similarities between the routes of the driver and the riders. To analyze route similarity the Needleman-Wunsch algorithm, one of the first examples of dynamic programming, is used.

The Needleman-Wunsch algorithm scores the alignment of two groups of letters. A matrix $(M[i, j])$ is created, and scores of matching, mismatching and gap are assigned. These scores are assigned to the cells such that if the letters are same, matching score is assigned; if they are different, mismatching score is assigned; if one of the letters is missing, gap score is assigned. The missing letter in a letter array is defined as indel value. The algorithm has various solving methods, but all of them give the same result.

The steps involved in solving the problem are as follows [49]:
(i) A matrix, S , is defined, where $i$ and $j$ denoting the row and column numbers. Let $m$ and $n$ denote the lengths of the first and second letter arrays, then

$$
0 \leq i \leq m \text { and } 0 \leq j \leq n
$$

(ii) The values of S are set to one if there is a match and to zero if there is no match (assuming the matching score is one and the mismatching score is zero). If there is a gap, that is to say an indel value in the letter groups, a gap score is assigned. When the gap score is zero,

$$
S[i, 0]=0 \text { for } i=1,2, \ldots, m \text { and } S[0, j]=0 \text { for } j=1,2, \ldots, n
$$

(iii) Compute scores starting from the top-left cell using following equation:

$$
\begin{equation*}
M[i, j]=S[i, j]+\max (M[i-1: x], M[j-1: y]) \tag{3.1}
\end{equation*}
$$

(iv) Start the traceback process from the bottom-right cell and continue by selecting the cell with the lowest value from the adjacent columns and rows.

In example given in Figure 2.1, to check the route feasibility between driver $d 1$ and rider $r 1$, the letter arrays "ABCDE" and "CE" should be aligned. The sequence alignment for this pair will result in a score of two, and an alignment is found such that

$$
\begin{array}{ccc}
A B & C D & E \\
-- & C- & E .
\end{array}
$$

For the algorithm proposed in this dissertation, only the score of the matrix, not the alignment of the letters, is needed. Therefore, the Needleman-Wunsch algorithm is modified by eliminating the traceback process. In this algorithm, calculation of the matrix begins at the top-left cell and finishes at the bottom-right cell. The S and

M matrices are calculated as depicted in Figures 3.2 and 3.3. In Figure 3.2, the S matrix is created as follows: If the letters are the same, then a matching score of one is written; otherwise, a mismatching score of zero is written. In Figure 3.3, the M matrix is created using equation 3.1. Since $S[1,1]=0, M[0,1]=0$ and $M[1,0]=0, M[1,1]$ is calculated as 0 . The bottom-right cell $\mathrm{M}[2,5]$ is calculated as 2 because $\mathrm{s}[2,5]=1$, $\mathrm{M}[1,5]=1$ and $\mathrm{M}[2,4]=1$, thus $\max (\mathrm{M}[1,5], \mathrm{M}[2,4])=1$ and $\mathrm{M}[2,5]=\mathrm{S}[2,5]+1=2$.

|  |  | $\boldsymbol{A}$ | $\boldsymbol{B}$ | $\boldsymbol{C}$ | $\boldsymbol{D}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{E}$ |  |  |  |  |  |
| $\boldsymbol{C}$ | 0 | 0 | 0 | 0 | 0 |
| $\boldsymbol{E}$ | 0 | 0 | 0 | 0 | 0 |

Figure 3.2. The Needleman-Wunsch algorithm after the generation of the $S$ matrix.

|  |  | $\boldsymbol{A}$ | $\boldsymbol{B}$ | $\boldsymbol{C}$ | $\boldsymbol{D}$ | $\boldsymbol{E}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 0 | 0 | 0 | 0 | 0 |
| $\boldsymbol{C}$ | 0 | 0 | 0 | 1 | 1 | 1 |
| $\boldsymbol{E}$ | 0 | 0 | 0 | 1 | 1 | 2 |

Figure 3.3. The Needleman-Wunsch algorithm after the generation of the M matrix.

When using the Needleman-Wunsch algorithm for route checking, if the letters representing the origin and the destination of the rider are along the route of the driver, the score (the value of the cell $m x n$ ) equals two. Thus, it is concluded that when the Needleman-Wunsch algorithm is used to compare the letter arrays representing the route of driver $d$ and the origin and destination of rider $r$ and the matching score is
one, the mismatching score and gap penalty are zero, driver $d$ and rider $r$ are said to be spatially feasible, if the score is two. The proposed algorithm for checking route feasibility is given in Figure 3.4.

```
m= number of letters in rider's route
n= number of letters in driver's route
matchscore = 1
mismatchscore, gappenalty =0
for i in m+1 do
    for j in n+1 do
        match = score[i-1][j-1] + matchscore(seq1[i-1], seq2[j - 1])
        delete = score[i-1][j]+ gappenalty
        insert = score[i][j-1]+ gappenalty
        score [i][j] = max(match, delete, insert)
    end for
end for
return score[m][n]
```

Figure 3.4. Needleman-Wunsch algorithm to check route feasibility.

### 3.3. Joint Socialness Score (JSS)

The JSS is used to score the similarity of two participants' characteristics. The JSS of driver $d$ and rider $r$ is calculated using Equation 2.1.

In this equation, $\gamma_{g}, \gamma_{a}, \gamma_{w}$ and $\gamma_{\sigma}$ represent gender weight, age weight, employment status weight and socialness weight, respectively. The value $x$ is a variable defined such that $x \in\{1,-1\}$. Its value is positive one if the characteristics are the same and negative one if the characteristics are different. $x$ can be defined as follows:

$$
\begin{array}{rr}
x=1, & \text { if characteristics are similar } \\
x=-1, & \text { otherwise } .
\end{array}
$$

In order to solve for the values of $x$ variables, the similarities of the characteristics of participants are checked. In the example given in Table 2.1, characteristics of driver $d 1$ are male, aged 18-25, attending TAU and positive tendency to socialness. Similarly, characteristics of rider $r 1$ are female, aged 25-40, attending TAU and positive tendency to socialness. Then, characteristics of the driver and the rider are compared. For example, $x$ for genders of the driver and the rider is assigned as -1 , because their genders are different. An example calculation of JSS is demonstrated in Table 2.1.

### 3.4. Matching Process

In this section, the matching process is outlined. The matching process is carefully constructed to ease computational burden it imposes on the systems used. The "first come, first served (FCFS)" method is applied. When a rider enters the system, the capacity constraint for all available drivers is first checked. Next the JSSs for all feasible drivers are calculated. The rider is matched with the driver whose corresponding JSS is the highest. The proposed algorithm follows these steps:
(i) If there is a new announcement, update the database.
(ii) Select the unmatched rider whose announcement time is the earliest.
(iii) Select the temporally feasible driver with the earliest announcement time.
(iv) Check whether the rider's origin and destination locations are on the driver's route.
(v) If driver's route is feasible for the rider, calculate the JSS between the driver and the rider and add this pair to the matchable pair list.
(vi) If there is an unchecked driver, go to step three and repeat the process.
(vii) Select the driver with the best JSS from the matchable pair list and match him or her with the rider.
(viii) Eliminate the rider from the system and subtract the rider count from the capacity of the matched driver.
(ix) Update the database and repeat the process, starting from step one.

Note that if a rider is matched with a driver even for small part of the driver's route, the capacity of the driver's vehicle is reduced for the entire route. However, the route can be divided into sections using the Needleman-Wunsch algorithm. This may increase the number of matches but also increases computation times. For example, when a driver following the route "ABCDE" picks up a rider with origin "C" and destination "E," the capacity of the driver is decreased for the entire route. In reality, the driver can pick up another rider whose origin and destination locations are on the route "ABC." In the algorithm proposed in this dissertation, the option of separating the route into sections is omitted to reduce the length of computation times. The matching algorithm is described in Algorithm 3.5. The flowchart of the algorithm is presented in Figure 3.6.

```
m=number of riders
n =number of drivers
for i in range(0,m) do
    if rider count > 0 then
        for j in range(0,n) do
            if driver capacity > rider count then
                Route feasibility is checked as in Figure 3.4
                if route is feasible then
                    calculate socialness score {See Eqn.2.1}
                end if
            end if
        end for
    end if
    Match the rider with the best driver
    Eliminate the rider from the system
    capacity of the driver = capacity of the driver - rider count
end for
```

Figure 3.5. The proposed matching process.


Figure 3.6. Flowchart of the proposed matching process.

## 4. DATA COLLECTION AND ANALYSIS

### 4.1. Turkish-German University

The survey was conducted at the TAU, which is located in the Beykoz region, 10 km away from the nearest center of Istanbul, namely Kavacik. Istanbul has a very wide public transportation web, yet TAU has few transportation options because it is located in a district that is relatively sparsely inhabited. As depicted in Figure 4.1, there are only four bus stations located at a walkable distance from the campus entrances. Bus station one is located at Gate B, while bus stations two, three and four are approximately a six-minute walk away. Furthermore, the frequency of bus arrivals at these stations is quite low. A student may wait for approximately 20-30 minutes for a bus during the day. All of the buses take long routes to campus. This makes the travel duration from the city center (Kavacik) to campus at least 30 minutes, whereas the trip takes 10 minutes by private vehicle. As a result, many students prefer to hitchhike at the main enterance of the campus shown in Figure 4.1.


Figure 4.1. Location of the TAU Campus in Beykoz, Istanbul.

### 4.2. Survey Data

In 2018, there were nearly 2,000 students and staff at the TAU. A stated preference survey with 604 participants was performed at the university. The survey was conducted with faculty members and other staff members (e.g. janitors, tea makers, etc.), in addition to students, in order to understand the behaviors of all potential participants. The survey investigated participants' travel behavior and thoughts on ride-sharing systems. The survey investigated a variety of socioeconomic characteristics, such as gender, age, occupation, education and car ownership. Participants were also questioned on their travel characteristics, including frequency of using private cars and public transportation, trip time and cost, most preferred transportation mode, trip mode alternative and tendency to hitchhike. Technological characteristics, such as tendency to use mobile applications for transport and attitude toward new alternative transportation modes (such as ride-sharing), were also investigated. The survey questions are presented in Appendix A. The description of the survey is presented in Table 4.1.

Table 4.1. Descriptive results of the survey.

|  | Students | Faculty Staff | Administrative Staff | Other Staff | Total |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Total no. of participants | 497 | 32 | 2 | 17 | 548 |
| No. of participants who own <br> a private or family car | 44 | 16 | 0 | 9 | 479 |
| Proportion of participants who own <br> a private or family car to total | $8.85 \%$ | $50 \%$ | $0 \%$ | $52.94 \%$ | $87.41 \%$ |
| No. of participants who do not <br> own a private or family car | 453 | 16 | 2 | 8 | 69 |
| Proportion of participants who do not <br> own a private or family car | $91.15 \%$ | $50 \%$ | $100 \%$ | $47.06 \%$ | $12.59 \%$ |
| Average travel time from home <br> to the campus | 58.23 | 37.72 | 17.5 | 19.76 | 55.69 |

In Table 4.1, it can be seen that average travel times of students and staff greatly differ. This is because most of the university staff live near the university, while most of the students live with their family in homes located far from the university.

The questions posed to the participants to gain insight into their ride-sharing preferences are presented in Table 4.2. The participants were asked to assign each of these questions a value ranging from zero to five to represent the weights of sharing a ride with a similar participant. These weight factors are utilized in the algorithm to find joint weight factors. The results of the answers to the questions given in Table 4.2 are given for the students, faculty staff, administrative staff and other staff in Table 4.3, 4.4, 4.5 and 4.6 , respectively and summarized in Table 4.7. In these tables, drivers are participants who own a private or family car; the rest of the participants are classified as riders.

Table 4.2. Social factors and related survey questions.

| Parameter | Relevant Question |
| :--- | :--- |
| Gender | Would you agree sharing a ride with people of the same gender? |
| Age | Would you agree sharing a ride with people of a similar age? |
| Employment | Would you agree sharing a ride with people from the same university? |
| Socialness | Would you agree sharing a ride with strangers? |

Table 4.3. The average weights of the social parameters for the students.

|  | Students |  |  |
| :--- | :--- | :--- | :--- |
|  | driver | rider | total |
| Importance of gender (0-5) | 1.61 | 2.70 | 2.61 |
| Importance of age (0-5) | 2.59 | 2.59 | 2.59 |
| Importance of employment (0-5) | 2.61 | 1.86 | 1.92 |
| Importance of socialness (0-5) | 1.84 | 1.10 | 1.16 |

Table 4.4. The average weights of the social parameters for the faculty staff.

|  | Faculty Staff |  |  |
| :--- | :--- | :--- | :--- |
|  | driver | rider | total |
| Importance of gender (0-5) | 2.50 | 2.12 | 2.31 |
| Importance of age (0-5) | 1.75 | 1.69 | 1.72 |
| Importance of employment (0-5) | 2.19 | 1.69 | 1.94 |
| Importance of socialness (0-5) | 1.37 | 0.25 | 0.81 |

Table 4.5. The average weights of the social parameters for the administrative staff.

|  | Administrative Staff |  |  |
| :--- | :--- | :--- | :--- |
|  | driver | rider | total |
| Importance of gender (0-5) | 0 | 0 | 0 |
| Importance of age (0-5) | 0 | 0 | 0 |
| Importance of employment (0-5) | 0 | 0 | 0 |
| Importance of socialness (0-5) | 0 | 0 | 0 |

Table 4.6. The average weights of the social parameters for the other staff.

|  | Other Staff |  |  |
| :--- | :--- | :--- | :--- |
|  | driver | rider | total |
| Importance of gender (0-5) | 4.78 | 3.25 | 4.06 |
| Importance of age (0-5) | 0.78 | 0.50 | 0.65 |
| Importance of employment (0-5) | 0.89 | 0.62 | 0.76 |
| Importance of socialness (0-5) | 0 | 1.50 | 0.71 |

Table 4.7. The average weights of the social parameters for all participants.

|  | Total |  |  |
| :--- | :---: | :---: | :---: |
|  | driver | rider | total |
| Importance of gender (0-5) | 2.23 | 2.68 | 2.63 |
| Importance of age (0-5) | 2.16 | 2.51 | 2.47 |
| Importance of employment (0-5) | 2.29 | 1.82 | 1.88 |
| Importance of socialness (0-5) | 1.49 | 1.07 | 1.13 |

Table 4.3, 4.4, 4.5, 4.6 and 4.7 indicate that gender, age and employment play key roles for ride sharing as Shaheen et al. suggested in their study [46]. The socialness factors in a ride-matching algorithm can also be used to encourage participation in a ride-sharing system. The average results indicate that the weights of age, gender, employment and socialness are $2.47,2.63,1.88$ and 1.13 out of 5 , respectively. However, these values differ significantly among different groups. For example, the weight of gender for ride-sharing is 4.06 among other staff, which means that gender is very important to them when sharing a ride. In contrast, gender is not very important to the students, who assigned this factor an average rating of 2.61 points out of 5 . Additionally, students may be more interested than university staff in using a ridesharing system to meet new people.

The residential locations of the participants in the survey were used to identify suitable meeting locations. The home addresses of the participants were not asked to maintain their privacy; instead, participants were asked to name the bus stations closest to their home. It is assumed that drivers will use highways because of the traffic problems in Istanbul. The cost of traffic congestion in Istanbul was calculated to be $\$$ 3.12 billion in 2005 and congestion has continued growing [50,51]. To define meeting locations suitable for both drivers and riders, the route origin locations are assigned to the nearest meeting locations, which are the bus stations located on the highways. A map of Istanbul and the defined meeting points is presented in Figure 4.2.


Figure 4.2. Map of Istanbul and meeting points for ride-Sharing.

## 5. SIMULATION STUDY

In this chapter, the proposed ride-matching algorithm is tested using data set obtained from the survey performed at Turkish-German University and the results are discussed. Performance and matching qualities of the proposed algorithm are compared with other algorithms, namely the traditional bipartite matching algorithm and an optimization algorithm.

### 5.1. Application of Other Matching Algorithms

In this section, the two other ride-matching algorithm, which are compared with the proposed matching algorithm, namely the traditional bipartite matching algorithm and an optimization algorithm, which includes social parameters, are presented and their applications are described.

### 5.1.1. Traditional Weighted Bipartite Matching Algorithm

The traditional bipartite matching algorithm was constructed with the objective function of maximizing system-wide distance savings. This algorithm allows single rider-single driver matches and ignores the choices of participants. The algorithm builds arcs between each rider and each driver. These arcs are considered feasible if they create positive distance savings. Distance savings are calculated using the following equation:

$$
\begin{equation*}
\sigma_{(i, j, k, l)}=d_{o_{i} d_{i}}-\left(d_{o_{i} k}+d_{k l}+d_{l d_{i}}\right)+\sum_{j \in R}\left(d_{o_{j} d_{j}}-\left(d_{o_{j} k}+d_{l d_{j}}\right)\right) . \tag{5.1}
\end{equation*}
$$

In Equation 5.1, distance savings are calculated for the scenario in which driver $i$ picks up rider $j$ from point $k$ and drops him or her off at point $l$. In order to maximize system-wide distance savings, the calculations of distance savings are performed for all possible matches before any match is finalized. The matches are then finalized, starting with the match that offers the highest distance savings. Since all participants in the system must wait for the algorithm to make calculations for all possible matches, it takes a relatively long time to find a match for a participant. The approach used to match drivers and passengers in the weighted bipartite algorithm is presented in Figure 5.1. Flowchart of this algorithm is shown in Figure 5.2.

```
m= number of riders
n= number of drivers
for }j\mathrm{ in range(0,n) do
    if driver capacity > 0 then
        for i in range(0,m) do
            Calculate distance savings as in Eqn. 5.1
            if distance savings }\geq0\mathrm{ then
                add to feasible matches
            end if
        end for
        end if
end for
for k in range(0,feasible_matches_count) do
    Select the match with max distance saving
    Eliminate the matched rider and driver from the list
end for
```

Figure 5.1. Weighted bipartite matching algorithm.


Figure 5.2. Flowchart of the weighted bipartite ride-matching algorithm.

### 5.1.2. The Optimization Algorithm with Social Parameters

An optimization algorithm that includes social parameters was also constructed. This algorithm's objective function is to maximize distance savings. This algorithm allows multiple riders-single driver matches. Distance savings are calculated using Equation 5.1. The route of the driver is assumed to be fixed.

Unlike the proposed algorithm, which uses social parameters in an objective function, this optimization algorithm uses social parameters as constraints [38]. As a result, in the approach used to solve the optimization problem, a driver is matched with a rider only if all of their choices and characteristics match. In contrast, the algorithm proposed in this dissertation can match a female rider with a male driver if there is no better option. As mentioned previously, participants are asked to assign values ranging from zero to five to the parameters. To simulate this algorithm using the survey outcomes, the choices and characteristics of the participants can be transformed accordingly. When a male participant assigns zero, one or two points to "same gender choice," he can travel with a male or female driver. Similarly, if he assigns values of three, four or five, he will be assigned to the same gender.

The optimization algorithm checks the compatibility of social parameters not only between a rider and a driver but also between a rider and other riders. When multiple riders are allowed, the match among riders is also checked. Two versions of this algorithm are constructed, one for single rider-single driver matches (Optimization A) and one for multiple riders-single driver matches (Optimization B). The matching algorithm developed based on these considerations, is depicted in Figure 5.3. Since the only difference between Optimization A and Optimization B is the number of riders to be matched with a driver, the same algorithm is used for both of them.

```
m,n = number of riders, number of drivers
for j in range(0,n) do
    if driver capacity > 0 then
        for i in range(0,m) do
            if distance savings (Eqn. 5.1) \geq0 then
                if routes are compatible then
                    if social choices are compatible then
                        add to feasible matches
                end if
            end if
            end if
        end for
    end if
end for
for k in range(0,feasible_matches_count) do
    Select the match with max distance saving
    if driver_capacity > 0 then
        if driver is unmatched then
            Match the driver with the rider
        Eliminate the matched rider from the list
        driver_capacity = driver_capacity - 1
        else if driver is matched with other riders then
            if social choices are compatible between riders then
            Match the driver with the rider
            Eliminate the matched rider from the list
            driver_capacity =driver_capacity - 1
            end if
        end if
    end if
end for
```

Figure 5.3. Optimization with social factors algorithm.


Figure 5.4. Flowchart of the optimization ride-matching algorithm.

### 5.2. Performance of the Ride-matching Algorithms

The proposed algorithm was modeled in Python 2.7, and its performance was measured on a computer with an i5 2.7 GHz processor and 8 GB of RAM. All of the ride-matching algorithms described in this dissertation were modeled in Python 2.7 using the same data and the same computer.

To conduct a computational study, the survey data were used such that each participant was assumed to be included in the ride-sharing system. Travel demands were created based on survey answers such that:

- The origins of the participants were assumed to be the meeting locations closest to their homes, and the destination was assumed to be the TAU.
- In order to test the algorithms with the highest possible number of participants, two assumptions were made:
(i) All trip announcements were known prior to the beginning of the day.
(ii) All of the participants wished to arrive to the university at the same time.
(iii) All riders can wait for a driver as long as it takes if they know there is a vehicle coming to pick them up.
- Since there are very few students who own a car, all participants with a private car or a family car were counted as drivers.
- Participants' choices and characteristics were determined using questions from the survey presented in Table 4.2.
(i) The ages of the participants were categorized into four age groups: under 18, 18-24, 25-40 and over 40. These groups present children, students, young faculty and senior faculty, respectively.
(ii) Employment status was categorized as student, faculty staff, administrative staff or other staff.
(iii) All participants were assumed to be willing to meet new people, but the weight factor differed from person to person.

To fairly compare the performance of the proposed algorithm with the traditional weighted bipartite matching algorithm and the optimization algorithm, the algorithms were tested using different scenarios. Performance results are given in Table 5.1. In this table, Algorithms A, B, C and D represent the proposed algorithms given in Algorithm 3.5. In Algorithm A, three rider-single driver matches were allowed, and social parameters were included. In Algorithm B, single rider-single driver matches were allowed, and social parameters were included. In Algorithms C and D, social parameters were excluded. Algorithm C allowed three rider-single driver matches while Algorithm D allowed single rider-single driver matches. The traditional weighted bipartite matching algorithm, which is presented in Algorithm 5.1, allows only single rider-single driver matches. This is because the algorithm assumes that a driver will change his or her route to pick up a rider. Social parameters are excluded in this algorithm. Since the route of the driver is fixed in the optimization algorithm, multiple riders-single driver matches are allowed. Two versions of the optimization algorithm that included social parameters, which are given in Figure 5.3, were tested. Optimization A represented the optimization model that included social parameters and allowed single rider-single driver matches. Optimization B used the same algorithm and allowed three ridersingle driver matches. Each algorithm was run 10 times to find average values. The computation times presented in the table are the averages of these iterations.

Table 5.1. Performance of the ride-matching algorithms.

|  | Alg. A | Alg. B | Alg. C | Alg. D | Bipartite | Optimization A | Optimization B |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Socialness factor | Included | Included | Excluded | Excluded | Excluded | Included | Included |
| Driver Capacity | 3 | 1 | 3 | 1 | 1 | 1 | 3 |
| Rider Count | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| Number of matches | 191 | 67 | 191 | 67 | 67 | 61 | 80 |
| Average total <br> computation time (sec) | 17.65 | 11.63 | 9.36 | 8.07 | 101.64 | 171.52 | 214.09 |
| Average computation <br> time per match (sec) | 0.09 | 0.17 | 0.05 | 0.12 | 1.52 | 2.81 | 2.68 |

Table 5.1 indicates that the computation time of the traditional weighted bipartite algorithm was 12.6 times higher than the equivalent version of the proposed algorithm (Algorithm D). However, the number of matches did not change. This is likely because there were many riders to be matched. When social characteristics and choices were included in the single rider-single driver match, the proposed algorithm (Algorithm B) performed 14.7 times faster than the optimization algorithm (Optimization A). When a driver could be matched with three riders and social concerns were considered, the computation time of the proposed algorithm (Algorithm A) was found to be 12.1 times faster than that of the optimization algorithm (Optimization B). The number of matches found by the optimization algorithm was considerably lower than that of the proposed algorithm. This is because no lower bound was set for social parameter scoring in the proposed algorithm, so no match could be defined as unfeasible due to differences in social parameters. Overall, the proposed algorithm found a match for a rider within one second, even when including social characteristics and choices in its calculations. These results suggest that the proposed algorithm presents not only more qualitative matches but also feasible computation times for real-life applications.

### 5.3. Quality of Matches

The importance of presenting choices to ride-sharing participants has been discussed in the literature. This is seen as one of the key factors in achieving critical mass in ride-sharing $[3,46]$. Therefore, the matches found by the algorithms presented in the preceding section (Section 5.2) were analyzed to measure the impacts of the choices. The quality of the matches was measured by finding the average JSSs of the matches found by the algorithms. The results are summarized in Table 5.2.

When social factors were excluded for single rider-single driver matches, the proposed algorithm (Algorithm D) yielded higher JSS values compared to the weighted bipartite algorithm (Table 5.2). Note that when the proposed algorithm included social parameters (Algorithms A and B), it yielded greater JSSs compared to those algorithms that did not include social parameters (Algorithms C and D and the bipartite algorithm). When social parameters are included, the optimization algorithms

Table 5.2. Quality of the matches.

|  | Alg. A | Alg. B | Alg. C | Alg. D | Bipartite | Optimization A | Optimization B |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Total number of riders | 479 | 479 | 479 | 479 | 479 | 479 | 479 |
| Number of matched riders | 191 | 67 | 191 | 67 | 67 | 61 | 80 |
| Average JSS value of the <br> matched pairs | 8.25 | 7.87 | 1.07 | 4.48 | 3.57 | 11.42 | 16.35 |
| Number of matched pairs <br> having a JSS greater than zero | 154 | 51 | 127 | 48 | 46 | 52 | 70 |

(Optimization A and Optimization B) had greater JSS values compared to the proposed algorithms (Algorithms A and B). This is because the optimization algorithms used social parameters as constraints and accepted matches only if all of the social parameters of the participants were compatible. The proposed algorithm will match incompatible matches if there is no better option.

When a lower bound of zero was set for JSS values, 48 out of 67 possible matches were found using Algorithm D. In Algorithm D, social parameters were not included. The number of matches found by the weighted bipartite algorithm was 46 out of 67 . When social parameters were included, this value increased to 51 for the proposed algorithm (Algorithm B). The number of matches found by the optimization algorithm for single rider-single driver matches (Optimization A) was 52 out of 67 . The minor difference between Algorithm B and Optimization A was caused by the FCFS approach used by the proposed algorithm. To clarify, the proposed algorithm matches a rider with the earliest announcement time with a driver, even if some of their social parameters are incompatible, whereas the optimization algorithm skips matching an incompatible rider and instead finds another rider who is compatible with the driver. When the capacities of the vehicles were set to three and social factors were considered, the proposed algorithm (Algorithm A) found 154 matches, while the optimization algorithm (Optimization B) found 70 matches. Thus, it is concluded that if a lower bound is set, Algorithm A finds 2.2 times more matches when compared to Optimization B (when social factors are concerned and multiple riders-single driver matches are allowed).

## 6. SENSITIVITY ANALYSIS

In this chapter, influences of the model parameters on the results of the proposed ride-matching algorithm were identified. To understand which inputs affect the output variability of the proposed algorithm, regression analysis was used. To conduct regression analysis, 615 iterations with different combinations of numbers of riders, numbers of drivers, capacities of drivers, rider counts, numbers of riders who reject first match and JSS limits were analyzed. The results, namely ratio of matched riders, computation times and average JSSs of the matches, were measured on a computer with an i5 2.7 GHz processor and 8 GB of RAM. The computational results are shown in Appendix B.

### 6.1. Regression Analysis

Regression Analysis is widely used statistical method to understand the relationship between a dependent variable with one or more independent variables [52]. Using regression analysis, an equation, which defines the relationship between a dependent and one or more independent variables, are created, and coefficients of the independent variables and constant value are calculated [53,54]. When there are more than one independent variables, multiple regression analysis is utilized. Using multiple regression, contributions of the independent variables on the variability of dependent variable are calculated; however, in some cases the contribution of some independent variables may not be significantly important [55].

There are two types of regression analysis based on the number of independent variables: Simple linear regression and multiple linear regression. In simple linear regression, the relationship between a dependent variable $Y$ and an independent variable $X$ is shown in Equation 6.1.

$$
\begin{equation*}
Y=\beta_{0}+\beta_{1} X+\varepsilon \tag{6.1}
\end{equation*}
$$

In Equation 6.1, $\beta_{0}, \beta_{1}$ and define regression coefficients, and $\varepsilon$ defines an error value that shows the difference between calculated and observed values.

When there are more that two independent variables, the relationship between a dependent variable and $n$ independent variables $X_{1}, X_{2}, \ldots, X_{n}$ are shown in Equation 6.2.

$$
\begin{equation*}
Y=\beta_{0}+\beta_{1} X_{1}+\beta_{2} X_{2}+\ldots+\beta_{n} X_{n}+\varepsilon \tag{6.2}
\end{equation*}
$$

In Equation 6.2, $X_{1}, X_{2}, \ldots, X_{n}$ represent $n$ independent variables, $\beta_{1}, \beta_{2}, \ldots, \beta_{n}$ represent regression coefficients and $\varepsilon$ represents the error value.

### 6.2. Regression Analysis of Parameters

Multiple linear regression analysis were made for dependent variables, namely ratio of matched riders, computation time and average JSSs of the matches. There are six independent variables as follows:

- Number of riders.
- Number of drivers.
- Capacity of each driver's vehicle.
- Rider count.
- Number of riders rejecting first match.
- JSS limit.

Number of riders and number of drivers show the available participants in a given ride-sharing system. Capacity represents the number of available seats in each available driver's vehicle. Rider count means that how many riders want to travel together in the same vehicle. One ride-sharing request are made by riders, even if rider count is specified as more than one. Riders, who would reject the match assigned by a ridematching algorithm, are also considered. The parameter "number of riders rejecting first match" is used for riders, who reject their first match assigned by an algorithm but accept the second match, if there are any. In the proposed algorithm, JSS of the matches were not limited. To measure the effect of such limit, the parameter "JSS limit" is used. This parameter sets a limit for JSS of the matches, and reject the matches giving lower JSS than the JSS limit and force algorithm to search for other matches that satisfy this constraint.

615 numerical calculations were performed with different combinations of the independent variables. The algorithm was calculated five times for each combination due to stochastic behavior of the problem. Regression analysis were made using a commercially available software SPSS Version 25 . The computation times were measured on a computer with an i5 2.7 GHz processor and 8 GB of RAM.

### 6.2.1. Analysis for Ratio of Matched Riders

In this section, the effects of numbers of riders, numbers of drivers the ratio of matched riders, capacities of drivers, rider counts, numbers of riders who reject first match and JSS limits on the ratio of the matched riders are analyzed using multiple regression analysis and the results are evaluated. Summary output of multiple linear regression model is shown in Table 6.1.

The $R^{2}$ value, which is the proportion of variance in the dependent variable that can be explained by the independent variables. In Table 6.1, the $R^{2}$ value of 0.913 means that the independent variables, namely numbers of riders, numbers of drivers, capacities of drivers, rider counts, numbers of riders who reject first match and JSS limits, explain $91.3 \%$ of the variability of the dependent variable, ratio of matched

Table 6.1. Model summary of the regression for ratio of matched riders.

| Model Summary $b$Model R R Square Adjusted R Square <br> Std. Error of the Estimate    <br> 1 $0.956_{a}$ 0.913 0.913 <br> $7.82703 \%$    <br> a Predictors: (Constant), JSS Limit, Number of riders rejecting first match,    <br> Rider count, Number of riders, Capacity of each driver's vehicle, Number of drivers    <br> b Dependent Variable: Ratio of matched riders    |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: |

riders. In other words, high $R^{2}$ value indicates a good level of prediction.

Table 6.2. ANOVA of the regression for ratio of matched riders.

| ANOVA $_{a}$ |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Model | Sum of Squares | df | Mean Square | F | Sig. |
| Regression | 393161.630 | 6 | 65526.938 | 1069.612 | $0.000_{b}$ |
| Residual | 37247.510 | 608 | 61.262 |  |  |
| Total | 430409.139 | 614 |  |  |  |
| a Dependent Variable: Ratio of matched riders |  |  |  |  |  |
| b Predictors: (Constant), JSS Limit, Number of riders accepting first match, <br> Rider count, Number of riders, Capacity of each driver's vehicle, Number of drivers |  |  |  |  |  |

The analysis of variance (ANOVA) results are shown in Table 6.2. F value defines the ratio of two mean squares. When the F value is large and significance is lower than 0.01 , then it is concluded that the independent variables statistically significant to predict the dependent variable. In Table 6.2, F value and significance states that the regression model is good fit of the data.

In Table 6.3, unstandardized coefficients indicate how much the dependent variable varies with an independent variable when other independent variables are held

Table 6.3. Coefficients of the regression for ratio of matched riders.

| Coefficients ${ }_{a}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Model | Unstandardized Coefficients |  | Standardized <br> Coefficients | t | Sig. |
|  | B | Std. Error | Beta |  |  |
| (Constant) | 55.563 | 2.437 |  | 22.804 | 0.000 |
| Number of riders | -0.139 | 0.003 | -0.758 | -52.140 | 0.000 |
| Number of drivers | 0.280 | 0.017 | 0.240 | 16.155 | 0.000 |
| Capacity of each driver's vehicle | 11.033 | 0.480 | 0.335 | 23.005 | 0.000 |
| Rider count | -22.347 | 0.914 | -0.345 | -24.443 | 0.000 |
| Number of riders rejecting first match | 0.015 | 0.004 | 0.045 | 3.320 | 0.001 |
| JSS Limit | -0.157 | 0.010 | -0.227 | -16.199 | 0.000 |
| a Dependent Variable: Ratio of matched riders |  |  |  |  |  |

constant. The general form of the equation to predict ratio of matched riders is shown in Equation 6.2. Based on the coefficients shown in Table 6.3, this equation is rewritten as:

$$
\begin{equation*}
Y_{\text {romr }}=55.563-0.139 X_{n o r}+0.280 X_{n o d}+11.033 X_{c o d}-22.347 X_{r c}+0.015 X_{n r j}-0.157 X_{j s s} . \tag{6.3}
\end{equation*}
$$

In Equation 6.3, $Y_{\text {romr }}, X_{n o r}, X_{n o d}, X_{c o d}, X_{r c}, X_{n r j}, X_{j s s}$ represent ratio of matched riders, number of riders, number of drivers, capacity of drivers, rider count, number of riders rejecting first match and JSS limit, respectively. The statistical significance of these independent variables are also presented in Table 6.3 under the column "Sig." . Based on regression analysis, the following results can be made:

- Number of riders are statistically significant to explain ratio of matched riders. Figure 6.1 and Figure 6.2 show that when number of riders increases, ratio of matched riders decreases. In Figure 6.1, high driver capacity causes increase in ratio of matched riders. When there are 50 riders and driver capacities are set to 3 , ratio of matched riders approaches to $100 \%$. In Figure 6.2, increase in rider count led to decrease in ratio of matched riders. These results can be explained with limited number of drivers.
- Number of drivers are statistically significant to explain ratio of matched riders. Figure 6.3 and Figure 6.4 indicate that high number of drivers results in increase in ratio of matched riders. Figure 6.3 shows that capacity of drivers are also found to be directly proportional with ratio of matched riders. Figure 6.4 shows that increase in rider count causes decrease in ratio of matched riders. This can be explained with limited number of drivers.
- Figure 6.5 indicates that ratio of matched riders slightly increases with increasing number of riders rejecting first match. Table 6.3 shows that this change is statistically significant. Since ratio of number of riders to drivers is large, riders may be matched with drivers, even if they reject their first match or different riders may be matched because some riders may not be matched after rejecting their first match.
- Figure 6.6 shows that setting higher JSS limit causes decrease in ratio of matched riders. This is because, JSSs of some matches are smaller than JSS limits.


Figure 6.1. Ratio of matched riders versus number of riders by capacities of drivers.


Figure 6.2. Ratio of matched riders versus number of riders by rider count.


Figure 6.3. Ratio of matched riders versus number of drivers by different capacities.


Figure 6.4. Ratio of matched riders versus number of matched drivers by rider count.


Figure 6.5. Ratio of matched riders versus number of matched riders rejecting first match.


Figure 6.6. Ratio of matched riders versus JSS limit.

### 6.2.2. Analysis for Computation Time

In this section, using multiple regression analysis, computation times of the proposed algorithm with different combinations of independent variables are examined. Summary output of multiple linear regression model is presented in Table 6.4.

Table 6.4. Model summary of the regression for computation times.

| Model Summary ${ }_{b}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Model <br> 1 | $\begin{gathered} \mathbf{R} \\ 0.980_{a} \end{gathered}$ | R Square $0.961$ | Adjusted R Square $0.961$ | Std. Error of the Estimate $1.775814$ |
| a Predictors: (Constant), JSS Limit, Number of riders accepting first match, <br> Rider count, Number of riders, Capacity of each driver's vehicle, Number of drivers |  |  |  |  |
| b Dependent Variable: Computation time |  |  |  |  |

The high $R^{2}$ value states that the regression model explains well the relationship between the dependent variable, computation time, and independent variables, numbers of riders, numbers of drivers, capacities of drivers, rider counts, numbers of riders who reject first match and JSS limits.

Table 6.5. ANOVA of the regression for computation times.

| $\mathrm{ANOVA}_{a}$ |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Model | Sum of Squares | df | Mean Square | F | Sig. |
| Regression | 47242.229 | 6 | 7873.705 | 2496.803 | $0.000_{b}$ |
| Residual | 1917.337 | 608 | 3.154 |  |  |
| Total | 49159.565 | 614 |  |  |  |
| a Dependent Variable: Computation time |  |  |  |  |  |
| b Predictors: (Constant), JSS Limit, Number of riders accepting first match, |  |  |  |  |  |
| Rider count, Number of riders, Capacity of each driver's vehicle, Number of drivers |  |  |  |  |  |

The analysis of variance (ANOVA) results for computation times are shown in Table 6.5. Large F and 0.000 significance values indicate that the independent variables statistically significant to predict the dependent variable. In other words, the regression model for computation times is good fit of the data.

Table 6.6. Coefficients of the regression for computation times.

| Coefficients ${ }_{a}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Model | Unstandardized CoefficientsStandardized <br> Coefficients |  |  | t | Sig. |
|  | B | Std. Error | Beta |  |  |
| (Constant) | -2.334 | 0.553 |  | -4.222 | 0.000 |
| Number of riders | 0.031 | 0.001 | 0.494 | 50.549 | 0.000 |
| Number of drivers | 0.242 | 0.004 | 0.613 | 61.504 | 0.000 |
| Capacity of each driver's vehicle | 1.922 | 0.109 | 0.173 | 17.665 | 0.000 |
| Rider count | -3.955 | 0.207 | -0.181 | -19.068 | 0.000 |
| Number of riders rejecting first match | 0.006 | 0.001 | 0.051 | 5.589 | 0.000 |
| JSS Limit | 0.105 | 0.002 | 0.450 | 47.819 | 0.000 |
| a Dependent Variable: Computation time |  |  |  |  |  |

Based on the results depicted in Table 6.6, the equation for computation time is as follows:

$$
\begin{equation*}
Y_{c o m}=-2.334+0.031 X_{\text {nor }}+0.242 X_{\text {nod }}+1.922 X_{c o d}-3.955 X_{r c}+0.006 X_{n r j}+0.105 X_{j s s} . \tag{6.4}
\end{equation*}
$$

In Equation 6.4, $Y_{\text {com }}, X_{n o r}, X_{n o d}, X_{c o d}, X_{r c}, X_{n r j}, X_{j s s}$ represent computation time, number of riders, number of drivers, capacity of drivers, rider count, number of riders rejecting first match and JSS limit, respectively. The statistical significance of these
independent variables presented in Table 6.6 shows that all independent variables are statistically significant to explain computation time. Based on regression analysis, the following results can be made:

- Number of riders are statistically significant to explain computation times. Figure 6.7 and Figure 6.8 show that when number of riders increases, computation times increase because of increase in number of computation. Similarly, in Figure 6.7, high driver capacity causes more increase in computation times. In Figure 6.8, increase in rider count led to decrease in computation times. This is because, number of computations remains same when rider count is increased; however, since all drivers are matched before computing for all riders, number of computations decreases.
- Number of drivers are statistically significant to explain computation times. Figure 6.9 and Figure 6.10 indicate that high number of drivers results in increase in computation times. Figure 6.9 shows that capacity of drivers are also found to be directly proportional with computation times. These are because the number of computation increases with increasing number of drivers and capacities. Figure 6.10 shows that increase in rider count causes decrease in computation times because smaller number of computations is needed.
- Figure 6.11 indicates that computation times slightly increase with increasing number of riders rejecting first match. This is because, more computations are needed to match riders when the riders reject their first matches, new matches are searched.
- Figure 6.12 shows that setting higher JSS limit causes increase in computation times. More computations are needed to find a new match for a participant, when JSS of the assigned match is lower than the JSS limit.


Figure 6.7. Computation time versus number of riders by capacities of drivers.


Figure 6.8. Computation time versus number of riders by rider count.


Figure 6.9. Computation time versus number of drivers by different capacities.


Figure 6.10. Computation time versus number of matched drivers by rider count.


Figure 6.11. Computation time versus number of matched riders rejecting first match.


Figure 6.12. Computation time versus JSS limit.

### 6.2.3. Analysis for Average JSSs of Matched Pairs

In this section, average JSSs of Matched Pairs with variable independent parameters are investigated using multiple regression analysis. Summary output of multiple linear regression model is presented in Table 6.7.

Table 6.7. Model summary of the regression for average JSSs of matched pairs.

| Model Summary $_{b}$ |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
| Model | R | R Square | Adjusted R Square | Std. Error of the Estimate |
| 1 | $0.826_{a}$ | 0.683 | 0.680 | 6.950573994 |
| a Predictors: (Constant), JSS Limit, Number of riders accepting first match, |  |  |  |  |
| Rider count, Number of riders, Capacity of each driver's vehicle, Number of drivers |  |  |  |  |
| b Dependent Variable: Average JSS |  |  |  |  |

The $R^{2}$ value states that the regression model can explain $68.3 \%$ of the relationship between the dependent variable, average JSSs of matched pairs, and independent variables, numbers of riders, numbers of drivers, capacities of drivers, rider counts, numbers of riders who reject first match and JSS limits. Therefore, it can concluded that the regression model is good fit for the given data.

The analysis of variance (ANOVA) results for computation times are shown in Table 6.8. Large $F$ and 0.000 significance value indicates that the independent variables statistically significant to predict the dependent variable. In other words, the regression model for computation times is good fit of the data.

Based on the results depicted in Table 6.9, the equation for computation time is as follows:

Table 6.8. ANOVA of the regression for average JSSs of matched pairs.

| ANOVA $_{a}$ |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Model | Sum of Squares | df | Mean Square | F | Sig. |
| Regression | 62716.225 | 6 | 10452.704 | 216.365 | $0.000_{b}$ |
| Residual | 29131.219 | 603 | 48.310 |  |  |
| Total | 91847.443 | 609 |  |  |  |
| a Dependent Variable: Average JSS |  |  |  |  |  |
| b Predictors: (Constant), JSS Limit, Number of riders accepting first match, |  |  |  |  |  |
| Rider count, Number of riders, Capacity of each driver's vehicle, Number of drivers |  |  |  |  |  |

$$
\begin{equation*}
Y_{j s s}=45.800-0.020 X_{n o r}-0.013 X_{n o d}+0.204 X_{c o d}-0.775 X_{r c}+0.001 X_{n r j}+0.290 X_{j s s} . \tag{6.5}
\end{equation*}
$$

In Equation 6.5, $Y_{j s s}, X_{n o r}, X_{n o d}, X_{c o d}, X_{r c}, X_{n r j}, X_{j s s}$ represent JSSs of matched pairs, number of riders, number of drivers, capacity of drivers, rider count, number of riders rejecting first match and JSS limit, respectively. The statistical significance of these independent variables presented in Table 6.9. This results state that number of riders and JSS limit are statistically significant parameters to explain JSSs of matched pairs. Based on regression analysis, the following results can be made:

- Figure 6.13 and Figure 6.14 show that when number of riders increases, average JSSs are slightly decreased. Although, number of riders are found to be statistically significant, these slight changes may be explained by the randomness of the data. In Figure 6.13, high driver capacity causes increase in average JSSs. In Figure 6.14, increase in rider count led to decrease in average JSSs. However, capacity of drivers and rider count are not statistically significant to explain average JSSs.

Table 6.9. Coefficients of the regression for average JSSs of matched pairs.

| Coefficients $a_{a}$ |  |  |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model | Unstandardized CoefficientsStandardized <br> Coefficients |  |  |  |  |  |  |  |
|  | B | Std. Error | Beta | t | Sig. |  |  |  |
|  | 45.800 | 2.202 |  | 20.798 | 0.000 |  |  |  |
| Number of riders | -0.020 | 0.002 | -0.235 | -8.411 | 0.000 |  |  |  |
| Number of drivers | -0.013 | 0.015 | -0.024 | -0.849 | 0.396 |  |  |  |
| Capacity of each driver's <br> vehicle | 0.204 | 0.426 | 0.013 | 0.478 | 0.633 |  |  |  |
| Rider count | -0.775 | 0.812 | -0.026 | -0.954 | 0.341 |  |  |  |
| Number of riders rejecting <br> first match | 0.001 | 0.004 | 0.007 | 0.249 | 0.803 |  |  |  |
| JSS Limit | 0.290 | 0.009 | 0.835 | 31.276 | 0.000 |  |  |  |
| a Dependent Variable: Average JSS |  |  |  |  |  |  |  |  |

- Figure 6.15 and Figure 6.16 show that number of drivers, capacities and rider count do not affect average JSSs, significantly. Table 6.9 indicates that these parameters are not statistically significant to explain average JSSs.
- Figure 6.17 shows that number of riders rejecting first match does not affect average JSSs. Results presented in Table 6.9 state that this parameter is not statistically significant for average JSSs.
- Figure 6.18 shows that setting higher JSS limit causes significant increase in average JSSs. The matching algorithm rejects matches having lower JSS than a JSS limit. Therefore, average JSSs of the matched pairs increases when higher JSS limits are set.


Figure 6.13. Average JSSs of matched pairs versus number of riders by capacities of drivers.


Figure 6.14. Average JSSs of matched pairs versus number of riders by rider count.


Figure 6.15. Average JSSs of matched pairs versus number of drivers by different capacities.


Figure 6.16. Average JSSs of matched pairs versus number of matched drivers by rider count.


Figure 6.17. Average JSSs of matched pairs versus number of matched riders rejecting first match.


Figure 6.18. Average JSSs of matched pairs versus JSS limit.

## 7. CONCLUSION \& DISCUSSIONS

In this chapter, contributions of the dissertation, discussion of the results, the limitations of the study and future recommendations are presented.

### 7.1. Summary of the Contributions

- A literature review on ride-sharing is conducted. Several ride-matching algorithms in the literature are investigated based on their objective functions, parameters and assumptions.
- A sequence alignment algorithm used in the bioinformatics field, namely the Needleman-Wunsch algorithm, is utilized to check route alignment. In the proposed algorithm, drivers' routes are assumed to be prespecified and fixed. The Needleman-Wunsch algorithm checks if the origin and the destination of a rider are located on the routes of drivers.
- The proposed ride-matching algorithm includes the social parameters of age, gender, employment and willingness to meet new people. To the best of the author's knowledge, social parameters are included in the objective function of a ridematching algorithm for the first time. Similar parameters have been presented in the literature as constraints [38]. In the proposed algorithm, the similarities between these parameters are scored. A new parameter, namely JSS, is defined to represent social compatibility between participants.
- The importance of social characteristics and choices of the TAU students and staff were revealed based on a stated preference survey, conducted among 604 students and members of staff at the TAU in 2018.
- The effects of parameters of the proposed algorithm on ratio of matched participants, computation times and average JSSs of the matched pairs were analyzed.


### 7.2. Conclusions and Discussions

- In this dissertation, a review on several ride-matching algorithms is conducted based on their objective functions, parameters and assumptions and a new ridematching is proposed. Most of these ride-matching algorithms focused on system wide benefits. Some objective functions are maximizing total distance savings, minimizing total travel time, minimizing total travel cost, maximizing number of matches and maximizing total waiting and delay time. These approaches assumed that participants would want to be matched to maximize system benefits; however, they would want to maximize their own benefits. Furthermore, these algorithms assumed that participants would accept the matches found by these algorithms.
- FCFS approach is utilized in the proposed algorithm to decrease waiting times of participants to be matched. Traditional optimization approaches calculate all possible matches to find the best matches. Rolling horizon approach used in some algorithms forces participants to wait until a deadline in order to include participants, who make ride requests after the initialization of the matching process. Although, this approach improves the results of the objective functions, participants would not want to wait a long period of time. Utilizing FCFS approach, the proposed algorithm finds a match for the rider with the earliest announcement time and eliminates the rider from the database before searching a match for other participants. In this way, waiting time of a participant decreases. Additionally, number of computation decreases, because the matched riders and drivers are eliminated from the database before searching a match for the remaining participants. Consequently, utilizing FCFS approach decreases computation times, but the best match to maximize system-wide JSSs may not be found.
- The outcomes of the survey conducted for this dissertation state that social parameters, such as gender, age, employment and willingness to meet new people, are significant for participants to be included in a ride-sharing system. A new parameter, JSS, is presented to score social compatibility of the participants. The objective function of the proposed algorithm is set to be maximizing total JSS. In the literature, social parameters were used as constraints. This approach
significantly decreases number of matches. In the proposed algorithm, number of matches remains same with number of matches found by the algorithms excluding social parameters; because the proposed algorithm can match participants with low JSSs if there is no better option.
- The results of the simulation study indicate that the computation times of the proposed algorithm are significantly lower than the traditional weighted bipartite algorithm and the optimization algorithm with social parameters. When subjected to the same constraints, the proposed algorithm's computation time was 12.6 times lower than that of the weighted bipartite algorithm and 14.7 times lower than that of the optimization algorithm. The quality of matches was analyzed using JSS values. When social concerns were omitted, the proposed algorithm yielded a $25 \%$ higher average JSS value compared to the weighted bipartite algorithm. When social factors were included, the optimization algorithm presented better results; however, the number of matches decreased dramatically compared to the proposed algorithm.
- Sensitivity analysis for ratio of matched riders, computation times and average JSSs of matched pairs are conducted to analyze the effects of numbers of riders, numbers of drivers the ratio of matched riders, capacities of drivers, rider counts, numbers of riders who reject first match and JSS limits. Ratio of matched riders increases with number of drivers and capacities of drivers, whereas it decreases with increasing number of riders and rider count. Number of riders rejecting first match causes a slight increase in ratio of matched riders. This is because, there are limited number of drivers and large number of riders. Higher JSS limit led to decrease in ratio of matched riders, because some matches are rejected due to low JSSs.
- Computation times are directly related to number of computations. Therefore, it increases with increasing number of number of riders, number of drivers and capacities of drivers and it decreases with increasing number of rider count. Similarly, setting JSS limit increases computation times.
- Average JSSs of matched pairs are mainly affected by JSS limit. Setting a JSS limit forces the algorithm to reject matches with JSSs lower than JSS limit. Therefore, increasing JSS limit results in increase in average JSS.


### 7.3. Limitations of the Study

- In this dissertation, the general limitation is insufficient data set to simulate the ride-matching algorithms. Since the real travel demands with travel times and routes were needed, outcomes of the stated preference survey conducted at the TAU were transformed into travel demands by assuming all participants travel from their home to the TAU and they wanted to be at the TAU at the same time. These assumptions are made to test the algorithms with the highest possible number; however, if the participants do not travel at the same time, number of available participants to be matched may be very small to find successful matches.
- In this dissertation, it is assumed that all drivers use the same predefined route, but drivers may choose different routes in real life. Route flexibility is ignored in the proposed algorithm, but this can be included into the proposed algorithm by offering a route choice to drivers.
- The riders were assumed to be willing to go to the nearest meeting points; however, the distances between homes of the riders and meeting points are not taken into account.
- The survey is conducted in the TAU, which has limited public transportation options. The importance of factors affecting participants' travel behavior may vary for other campuses.


### 7.4. Recommendations

- To achieve critical mass in ride-sharing, demands of potential participants, such as willingness to be matched from the same gender or age, should be defined carefully and they should be included in ride-matching algorithms. The importance of the objective functions, parameters and assumptions utilized in ride-matching algorithm should be examined.
- To achieve critical mass in ride-sharing, number of drivers in the system is very crucial. In future studies, implementations to increase number of drivers should be discussed and incentives for drivers should be investigated.
- The variable, $x$, is defined as positive one or negative one depending on the similarity of social characteristics and choices of drivers and riders. The algorithm can be extended by utilizing fuzzy logic for the $x$ variable.
- Using the Needleman-Wunsch algorithm, the proposed algorithm can be developed. The Needleman-Wunsch algorithm allows the route of a driver to be split into matched parts and unmatched parts so that the driver can be matched with other riders if origin and destinations of the riders are located on the unmatched part of the driver's route. Similarly, multi-hop ride-sharing can be added. Consequently, ratio of matched riders and drivers can be increased.
- The effects of adding new parameters into the proposed algorithm should be investigated. Furthermore, meeting locations are represented by letters, but it is possible to using more than one letters to describe a location or even a time stamp. This may bring advantages, such as building dynamic routing, but computational burden may increase. A trade-off analysis for such upgrades for the proposed algorithm can be discussed in the future.
- The importance of social parameters and travel choices of potential participants should be investigated by conducting surveys in other campuses. Similarly, the survey is conducted among the students and staff of a university, but this can be extended by conducting surveys among other types of participants. Thus, better understanding of participants' travel behaviour can be achieved.
- The proposed biosequence based ride-sharing algorithm can be extended by utilizing different algorithms, such as Fast Optimal Global Sequence Alignment Algorithm, to increase computation time performance.


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# APPENDIX A: CAMPUS TRANSPORTATION SURVEY 

Tarih:
TÜRK - ALMAN ÜNIVERSITESI ULAŞIM TERCIHLERI ANKETi

## Bu anket Türk - Alman Üniversitesi, Mühendislik Fakültesi Yenilik ve Teknoloji Yönetimi Projesi kapsamında yapılmaktadır. Anketin amacı ulaşım ve park sorunlarını araştırmaktır. <br> *Araştırma bilimsel bir nitelik taşıdığından derlenen kişi ve aile bilgileri gizli tutulacaktır.

$\begin{array}{cccc}\begin{array}{c}\text { Ogğrenci } \\ \text { ( ) }\end{array} & \text { Akademik Personel } & \text { Idari Personel } & \text { Çalışan } \\ \text { Yaşnı: } & \text { () Cinsiyetiniz: } & \mathrm{E}()^{\text {() }} & \text { () } \\ \text { () }\end{array}$
Yaşınız:
Bölümünüz:
Kaçıncı döneminiz :
İkamet Ettiğiniz ilçe :
Size en yakın otobüs durağınin ismi :
Nerede ikamet ediyorsunuz?
Kendi aracinız var mı?
Okula gelmek için kullandığınız ailenize ait araç var mı?


|  |  | Asla | (Haftada Kaç Gün) |  |  | Her Zaman |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1. Okula özel araç ile gelmediğinizde; |  | 0 | 1 | , | 3 | 4 | 5 |
| 1.1. | En çok hangi ulassım aracını tercih ediyorsunuz ? |  |  |  |  |  |  |
| 1.1.1. | Otobüs | ( ) | ( ) | ( ) | ( ) | ( ) | ( ) |
| 1.1.2. | Taksi | ( ) | ( ) | ( ) | ( ) | ( ) | ( ) |
| 1.1.3. | Vapur | () | () | () | () | () | () |
| 1.1.4. | Shuttle | ( ) | () | ( ) | ( ) | () | ( ) |
| 1.1.5. | Okul Personel Servisi | ( ) | ( ) | ( ) | ( ) | () | () |
| 1.1.6. | Aracı olan arkadaşımla gelirim. | () | () | () | ( ) | () | () |
| 1.1.7. | Diğer: ............. | () | () | () | () | () | () |
| 1.2. Otobüs tercihinizde en önemli faktör nedir? |  |  |  |  |  |  |  |
| 1.2.1. | Erken gelmesi | () | () | () | ( ) | ( ) | ( ) |
| 1.2.2. | Seyahat süresinin kısa olması | () | () | () | () | () | () |
| 1.2.3. | Aktarmasız okula gitmesi | () | () | () | () | () | () |
| 1.2.4. | Okulun önüne kadar gitmesi | ( ) | () | ( ) | ( ) | ( ) | ( ) |
| 1.2.5. | Konforlu olması | () | () | () | () | () | () |
| 1.2.6. | Diger: .............. | () | () | () | () | () | () |
| 1.3. | Okula toplu ulaşımla geldiǧimde aktarma sayısı az olan rotay tercih ederim. | () | () | () | () | () | () |
| 1.4. | Okula toplu ulaşımla geldiǧimde ulaşım süresi kısa olan rotay tercih ederim. | () | () | () | () | () | () |
| 1.5. | Okula gelirken en çok hangi otobüsü/otobüsleri tercih ediyorsunuz? | 1........ | 2........ | 3........ | 4........ | 5........ | 6........ |
| 1.6. | Herhangi bir toplu ulaşım aracına varmak için şu kadar | 1 dk | 5 dk | 10 dk | 20 dk | 30 dk | $30+\mathrm{dk}$ |
|  | yürüyebilirim. | ( ) | ( ) | ( ) | ( ) | ( ) | ( ) |
| 2. Okula gelmek için özel aracınız varsa; |  | Asla | (Haftada Kaç Gün) |  |  |  | Her Zaman |
|  |  | 0 | 1 | 2 | 3 | 4 | 5 |
| 2.1 . | Aracmila okula kadar gelirim. | ( ) | () | () | ( ) | () | () |
| 2.2. | Araamı uygun bir yere park eder ve toplu ulaşımla devam ederim. | () | () | () | () | () | () |
| 2.3. | Masrafi fazla olduğu için belli bir yere kadar arabayla gelirim. | () | () | () | () | () | () |
| 2.4. | Yalnızca vaktim dar olduğunda araç ile kullanırım. | () | () | () | () | () | () |
| 2.5. | Daha konforlu olduğu için aracım ile gelirim. | () | () | () | () | () | () |
| 2.6. | Masrafı fazla olduğu için kullanmam. | () | () | () | () | () | () |
| 2.7. | Trafik sebebiyle araçile gelmem. | ( ) | ( ) | ( ) | ( ) | ( ) | ( ) |
| 2.8. | Okula gelirken en çok hangi yolları tercih ediyorsunuz ? |  |  |  |  |  |  |
| 2.8.1. | Riva Yolu | ( ) | () | ( ) | () | () | () |
| 2.8.2. | Sahil yolu | ( ) | () | ( ) | () | ( ) | ( ) |
| 2.8.3. | Diğer: .......... | () | () | () | () | () | () |
| 2.9. | Okula km olarak en kisa yolu tercih ederim. | () | () | () | () | () | () |
| 2.10 . | Okula süre olarak en kısa yolu tercih ederim. | ( ) | () | () | () | () | ( ) |

Figure A.1. Campus transportation survey, page 1.

|  |  | Asla |  |  | Her Zaman |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | şımına genel olarak bakışını: | 0 | 1 | 2 | 3 | 4 | 5 |
| (Otostop, Car-Pooling, Ride-Sharing vb.) |  |  |  |  |  |  |  |
| 3.1. | Bakışım olumludur. | ( ) | () | ( ) | ( ) | () | () |
| 3.2 . | Yabancılara güvenmediğim için başkasının aracına binmem veya | () | () | () | () | () | () |
| başkasını aracıma almam. |  |  |  |  |  |  |  |
| 3.3. | Araç paylaşacağım kişi/lerin TAÜ'den olması önemlidir. | () | () | () | () | () | () |
| 3.4. | Otostop çekmemde/otostopçu almamda; |  |  |  |  |  |  |
| 3.4.1. | Hava durumu etkilidir. | () | () | () | () | () | () |
| 3.4.2. | Saat etkilidir. | () | () | ( ) | ( ) | ( ) | ( ) |
| 3.4.3. | Karşı tarafin cinsiyeti etkilidir. | () | () | ( ) | ( ) | ( ) | ( ) |
| 3.4.4. | Karşı tarafın tanıdık olması önemlidir. | () | () | ( ) | ( ) | ( ) | ( ) |
| 3.4.5. | Karşı tarafın üniversiteden olması önemlidir. | () | () | () | () | () | () |
| 3.5. Bir APP üzerinden; |  |  |  |  |  |  |  |
| 3.5.1. | Okuldan biri ile araç paylaşıım. | () | () | ( ) | ( ) | () | () |
| 3.5.2. | Herhangi biri ile araç paylaşırım. | () | () | ( ) | ( ) | ( ) | ( ) |
| 3.5.3. | Hakkında olumlu yorumlar olan biriyle araç paylaşıım. | () | () | ( ) | () | () | () |
| 3.6. Araç paylaşımının; |  |  |  |  |  |  |  |
| 3.6.1. | Trafik üzerindeki etkilerini önemserim. | () | () | ( ) | ( ) | ( ) | ( ) |
| 3.6.2. | Çevre üzerindeki etkilerini (karbondioksit salınımı | () | () | ( ) | ( ) | ( ) | ( ) |
| azaltması vb.) önemserim. |  |  |  |  |  |  |  |
|  |  | Asla |  |  |  |  | Her Zaman |
| 4. Kampüse Özel araç ile gelmiyorsanız araç paylaşımı için; |  | 0 | 1 | 2 | 3 | 4 | 5 |
| 4.1 . | Para veririm. | () | () | ( ) | ( ) | ( ) | ( ) |
| 4.2 . | Vereceğim ücret toplu ulaşım ile aynı ise kabul ederim. | () | () | () | ( ) | () | ( ) |
| 4.3. | Vereceğim ücret toplu ulaşımın 2 katı kadar olur ise kabul | () | () | ( ) | ( ) | () | ( ) |
| edebilirim. |  |  |  |  |  |  |  |
| 4.4. | Okula gelirken otostop çekerim. | () | () | ( ) | ( ) | ( ) | ( ) |
| 4.5 . | Okuldan eve giderken otostop çekerim. | () | () | () | ( ) | () | () |
| 4.6. | Araç sahibine göre her arabaya binmem. | ( ) | () | ( ) | ( ) | ( ) | ( ) |
| 4.7. | Araç modeline göre her arabaya binmem. | () | () | () | () | ( ) | () |
|  |  | 1 dk | 5 dk . | 10 dk . | 15 dk . | 30 dk . | 1+ saat |
| 4.8. | Araan kalkışı için maksimum ne kadar süre bekleyebilirsiniz. | () | () | ( ) | ( ) | ( ) | ( ) |
| 4.9 . | Araç paylaşımı için şu kadar mesafe yürüyebilirim. | () | () | ( ) | ( ) | ( ) | ( ) |
| 4.10 . | Sürücüsūz (otonom) araçlar olursa daha çok tercih ederim. | () | () | () | () | () | () |
| 4.11. | Okul dısıından bir/birkaç yabancıyla taksi paylaşabilirim. | ( ) | () | ( ) | ( ) | ( ) | ( ) |
| 4.12. | Okuldan bir/birkaç yabancıyla taksi paylaşabilirim. | () | () | ( ) | () | () | () |
| 4.13 . | Tanıdık bir/birkaç kişiyle taksi paylaşabilirim. | () | () | ( ) | ( ) | () | ( ) |
| 4.14. | Daha önce Über gibi uygulamalan kullandım. | () | () | () | () | () | () |
| 4.15 . | Neden otostop çekerim? |  |  |  |  |  |  |
| 4.15.1. | Toplu ulaşım olmadığında otostop çekerim. | () | () | () | ( ) | () | ( ) |
| 4.15.2. | Ücretsiz olduğu için otostop çekerim. | ( ) | () | ( ) | ( ) | ( ) | ( ) |
| 4.15.3. | Yeni insanlar tanımak için otostop çekerim. | () | () | ( ) | ( ) | ( ) | ( ) |
| 4.15.4. | Daha konforlu seyahat için otostop çekerim. | () | () | ( ) | ( ) | () | ( ) |


|  |  | Asla |  |  |  |  | Her Zaman |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5. Kampüse özel araç ile geliyorsanız araç paylaşımı için; |  | 0 | 1 | 2 | 3 | 4 | 5 |
| 5.1. | Ücretini alarak paylaşabilirim. | () | () | ( ) | ( ) | () | ( ) |
| 5.2. | Ücretsiz yolcu ile paylaşmam. | () | () | ( ) | () | () | () |
| 5.3. | Okula gelirken otostopçu alıım. | () | () | () | ( ) | () | ( ) |
| 5.4. | Okuldan çıkarken otostopçu alırım. | () | () | ( ) | ( ) | () | () |
| 5.5. | Sadece üniversiteden otostopçu alırım. | () | () | () | ( ) | () | ( ) |
| 5.6. | Üniversiteden de olsa her otostopçuyu kabul etmem. | () | () | ( ) | ( ) | () | ( ) |
| 5.7. | Araç paylaşımı için rotamı bir miktar değiştirebilirim. | () | () | ( ) | () | () | ( ) |
| 5.8. | Araç paylaşımı için şu kadar süre beklerim. | () | () | ( ) | ( ) | () | ( ) |
| 5.9. | Otopark imkanı sadece aracını paylaşanlara verilirse aracımı | () | () | ( ) | ( ) | () | ( ) |
| paylaşabilirim. |  |  |  |  |  |  |  |
| 5.10. | Masraflar azalırsa aracımla okula gelirim. | () | () | ( ) | () | () | ( ) |
|  |  | 1 dk | 5 dk . | 10 dk . | 15 dk . | 30 dk . | 1+ saat |
| 5.11. | Aracımı ücreti karşlığında paylaşırsam yolcuyu en fazla şu kadar süre beklerim: | () | ( ) | ( ) | ( ) | ( ) | ( ) |
|  |  |  |  |  |  |  |  |
| 5.12. | Daha önce Uber benzeri uygulamalarla aracıma yolcu aldım. | () | () | ( ) | () | () | ( ) |
| 5.13. | Aracıma otostopçu almamda şunlar etkilidir: |  |  |  |  |  |  |
|  | Yeni insanlar tanımak için otostopçu alıım. | () | () | ( ) | () | () | () |
| 5.13.2. | İnsanlara yardımcı olmak için otostopçu alırım. | ( ) | () | ( ) | () | () | ( ) |
| 5.13.3. | Diğer: .... | (1) | (1) | (1) | (1) | (1) | (1) |

Figure A.2. Campus transportation survey, page 2.

## APPENDIX B: COMPUTATIONAL RESULTS

The following tables show the computational results of the proposed algorithm using different values.
Table B.1. Computational results of the proposed algorithm.

| Iteration \# | Number <br> of <br> Riders | Number <br> of <br> Drivers | Capacity | Rider <br> Count | Number of Riders Rejecting First Match | $\begin{gathered} \text { JSS } \\ \text { Limit } \end{gathered}$ | Computation Time | Average <br> JSS of <br> Matched <br> Pairs | Number <br> of <br> Matched <br> Riders | Number <br> of <br> Matched <br> Drivers | Ratio of Matched Riders | Ratio of Matched Drivers | Ratio of <br> Riders <br> Accepting <br> First Match | Case <br> \# |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 479 | 69 | 3 | 1 | 0 | -100 | 22.7080 | 8.2513 | 191 | 64 | 39.87\% | 92.75\% | 100.00\% | 1 |
| 2 | 479 | 69 | 3 | 1 | 0 | -100 | 22.9750 | 8.2513 | 191 | 64 | $39.87 \%$ | 92.75\% | 100.00\% | 1 |
| 3 | 479 | 69 | 3 | 1 | 0 | -100 | 22.5390 | 8.2513 | 191 | 64 | 39.87\% | 92.75\% | 100.00\% | 1 |
| 4 | 479 | 69 | 3 | 1 | 0 | -100 | 22.8450 | 8.2513 | 191 | 64 | 39.87\% | 92.75\% | 100.00\% | 1 |
| 5 | 479 | 69 | 3 | 1 | 0 | -100 | 22.6100 | 8.2513 | 191 | 64 | 39.87\% | 92.75\% | 100.00\% | 1 |
| 6 | 479 | 65 | 3 | 1 | 0 | -100 | 21.6720 | 7.8548 | 179 | 60 | $37.37 \%$ | 92.31\% | 100.00\% | 1 |
| 7 | 479 | 65 | 3 | 1 | 0 | -100 | 20.9820 | 8.1844 | 179 | 60 | $37.37 \%$ | 92.31\% | 100.00\% | 1 |
| 8 | 479 | 65 | 3 | 1 | 0 | -100 | 21.0600 | 8.0279 | 179 | 60 | $37.37 \%$ | 92.31\% | 100.00\% | 1 |
| 9 | 479 | 65 | 3 | 1 | 0 | -100 | 21.1690 | 7.9553 | 179 | 60 | $37.37 \%$ | 92.31\% | 100.00\% | 1 |
| 10 | 479 | 65 | 3 | 1 | 0 | -100 | 21.0960 | 8.6313 | 179 | 60 | $37.37 \%$ | 92.31\% | 100.00\% | 1 |
| 11 | 479 | 60 | 3 | 1 | 0 | -100 | 19.4090 | 8.7746 | 173 | 58 | $36.12 \%$ | 96.67\% | 100.00\% | 1 |
| 12 | 479 | 60 | 3 | 1 | 0 | -100 | 19.4030 | 6.7866 | 164 | 55 | 34.24\% | 91.67\% | 100.00\% | 1 |
| 13 | 479 | 60 | 3 | 1 | 0 | -100 | 18.8220 | 6.8264 | 167 | 56 | 34.86\% | 93.33\% | 100.00\% | 1 |
| 14 | 479 | 60 | 3 | 1 | 0 | -100 | 18.8230 | 7.6886 | 167 | 57 | $34.86 \%$ | 95.00\% | 100.00\% | 1 |
| 15 | 479 | 60 | 3 | 1 | 0 | -100 | 19.3740 | 8.9364 | 173 | 58 | 36.12\% | 96.67\% | 100.00\% | 1 |
| 16 | 479 | 55 | 3 | 1 | 0 | -100 | 17.4410 | 8.8224 | 152 | 51 | 31.73\% | 92.73\% | 100.00\% | 1 |
| 17 | 479 | 55 | 3 | 1 | 0 | -100 | 17.0700 | 6.9557 | 158 | 54 | $32.99 \%$ | 98.18\% | 100.00\% | 1 |
| 18 | 479 | 55 | 3 | 1 | 0 | -100 | 17.1550 | 6.6000 | 155 | 52 | 32.36\% | 94.55\% | 100.00\% | 1 |
| 19 | 479 | 55 | 3 | 1 | 0 | -100 | 16.6500 | 7.2081 | 149 | 50 | 31.11\% | 90.91\% | 100.00\% | 1 |
| 20 | 479 | 55 | 3 | 1 | 0 | -100 | 17.2320 | 7.3484 | 155 | 53 | 32.36\% | 96.36\% | 100.00\% | 1 |
| 21 | 479 | 50 | 3 | 1 | 0 | -100 | 16.0770 | 7.1571 | 140 | 48 | 29.23\% | 96.00\% | 100.00\% | 1 |
| 22 | 479 | 50 | 3 | 1 | 0 | -100 | 17.4830 | 6.0979 | 143 | 48 | 29.85\% | 96.00\% | 100.00\% | 1 |
| 23 | 479 | 50 | 3 | 1 | 0 | -100 | 17.3690 | 8.2937 | 143 | 48 | 29.85\% | 96.00\% | 100.00\% | 1 |

Table B．1．Computational results of the proposed algorithm．（cont．）

| ¢ | $\rightarrow$ | $\rightarrow$ | $\rightarrow$ | $-$ | $-$ | $\rightarrow$ | $-$ | $\rightarrow$ | $\rightarrow$ | $\rightarrow$ | $\rightarrow$ | $-$ | $-$ | $\rightarrow$ | $\rightarrow$ | － | $-$ | $-$ | $\rightarrow$ | $\checkmark$ | $\rightarrow$ | － | － |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & \text { ô } \\ & \text { on } \\ & 0 . \\ & 0 \end{aligned}$ | $\begin{aligned} & 0 . \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { so } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { so } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { ô } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { oi } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { 合 } \\ & 0 \\ & 0 \\ & 0 \\ & \hline 0 \end{aligned}$ | $\begin{aligned} & \text { so } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { ồ } \\ & \text { O. } \\ & \text { O} \end{aligned}$ | $\begin{aligned} & \text { so } \\ & 0 \\ & 0 \\ & \dot{0} \\ & \hline \end{aligned}$ | $\begin{aligned} & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { ob } \\ & \text { ob } \\ & \text { O} \end{aligned}$ | $\begin{aligned} & \text { so } \\ & 0 \\ & 0 \\ & \vdots \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { ồ } \\ & \stackrel{0}{\dot{O}} \\ & \text { ? } \end{aligned}$ | $\begin{aligned} & \text { so } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { so } \\ & 0 . \\ & \dot{0} \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { ob } \\ & \text { ob } \\ & \text { O} \end{aligned}$ | $\begin{aligned} & \text { so } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { ồ } \\ & \text { O. } \\ & \text { O} \end{aligned}$ | $\begin{aligned} & \text { ơ } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { 合 } \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ |  |
|  | $\begin{aligned} & \text { ol } \\ & \text { ó } \\ & \dot{\theta} \end{aligned}$ |  |  |  | $\begin{aligned} & \text { so } \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\left.\begin{array}{\|c} 00 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{array} \right\rvert\,$ | $\begin{aligned} & 00 \\ & \underset{~}{7} \\ & \vdots \end{aligned}$ | $\begin{aligned} & 00 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & 00 \\ & 00 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { 処 } \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{array}{\|c} 00 \\ 0 \\ 0 \\ 0 \\ 8 \end{array}$ | $\begin{aligned} & \text { so } \\ & 0 \\ & \stackrel{1}{\circ} \end{aligned}$ | $\begin{array}{\|c} \stackrel{\circ}{\circ} \\ \stackrel{\sim}{7} \\ \underset{\sim}{2} \end{array}$ | $\begin{array}{\|c\|c} 00 \\ 1 \\ 1 \\ 0 \\ \infty \\ \infty \end{array}$ |  | $\begin{aligned} & \text { so } \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ |  | $\begin{aligned} & \text { so } \\ & \text { ó } \\ & \text { in } \end{aligned}$ | $\begin{aligned} & \text { so } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { so } \\ & \text { ó } \\ & \text { B } \end{aligned}$ |  | $\begin{aligned} & 00 \\ & 0 \\ & 0 \\ & \dot{\theta} \end{aligned}$ | $\begin{aligned} & \text { ob } \\ & \text { ob } \\ & \text { B. } \end{aligned}$ |
|  | $\begin{array}{\|c} \substack{0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0} \end{array}$ |  | $\left.\begin{array}{\|c} 0 \\ \stackrel{0}{0} \\ \stackrel{\rightharpoonup}{0} \end{array} \right\rvert\,$ | $\begin{array}{\|c} \text { 合 } \\ \underset{\sim}{\dot{o}} \end{array}$ | $\begin{array}{\|c} \substack{0 \\ \stackrel{0}{0} \\ \stackrel{\sim}{N}} \end{array}$ | $\left\|\begin{array}{c} 0 \\ 0 \\ \vdots \\ 0 \\ \hline \end{array}\right\|$ | $\begin{array}{\|c\|c\|c\|c\|c\|c\|c\|c\|c\|} \hline 1 \\ \stackrel{1}{\mathrm{~N}} \end{array}$ |  |  | $\begin{aligned} & \text { 合 } \\ & \text { 令 } \end{aligned}$ | $\begin{array}{\|c} \substack{0 \\ \underset{\sim}{\mathrm{i}} \\ \underset{\sim}{\mathrm{~N}}} \\ \hline \end{array}$ |  | $\begin{array}{\|l\|l} 00 \\ 0 \\ \infty \\ \underset{\sim}{0} \end{array}$ | $\begin{array}{\|c} \stackrel{\circ}{\mathrm{H}} \\ \underset{\sim}{\mathrm{j}} \end{array}$ | $\begin{aligned} & \circ 0 \\ & \infty \\ & \infty \\ & \dot{\sim} \end{aligned}$ | $\begin{aligned} & \text { 合 } \\ & \underset{~}{2} \end{aligned}$ | $\begin{aligned} & \text { So } \\ & \text { O} \\ & \dot{\mathrm{N}} \end{aligned}$ |  |  | $\begin{gathered} \infty \\ \infty \\ \infty \\ \infty \\ \underset{\sim}{\infty} \end{gathered}$ | $\begin{array}{\|l\|l} \hline 0 \\ \mathrm{C} \\ \mathbf{~} \end{array}$ |  | $\begin{array}{\|l\|l} 80 \\ 18 \\ 18 \\ 10 \end{array}$ |
|  | $\stackrel{\infty}{4}$ | 18 | フู | ブ | 18 | \％ | 7 | ¢ | $\infty$ | ค | $\bigcirc$ | $\infty$ | ¢ั | $\overrightarrow{1}$ | ค | 18 | $\stackrel{1}{\circ}$ | $\stackrel{\square}{\circ}$ | － | $\stackrel{\sim}{r}$ | $\stackrel{\sim}{\sim}$ | － | $\stackrel{1}{\sim}$ |
|  | $\stackrel{\Im}{7}$ |  | $\stackrel{1}{9}$ | $\stackrel{\text { ® }}{\text {－}}$ | $\stackrel{\rightharpoonup}{7}$ | $\stackrel{1}{9}$ | 적 | $\stackrel{\circ}{7}$ | $\stackrel{\cong}{\rightrightarrows}$ | $\ddot{\exists}$ | $\stackrel{\rightharpoonup}{0}$ | $\underset{\exists}{7}$ | 8 | ס | 8 | － | $\stackrel{\rightharpoonup}{\square}$ | $\mathscr{\infty}$ | $\otimes$ | $\varnothing \sim$ | $\infty$ | $\stackrel{\circ}{\infty}$ | H |
|  | $\begin{aligned} & \underset{O}{\circ} \\ & \underset{\sim}{\circ} \\ & \dot{\infty} \end{aligned}$ | $\left\|\begin{array}{c} 1 \\ \dot{e} \\ i \\ 0 \end{array}\right\|$ | $\begin{gathered} 0 \\ \underset{N}{1} \\ 0 \\ 0 \end{gathered}$ | $\begin{aligned} & \stackrel{\circ}{\otimes} \\ & \stackrel{\rightharpoonup}{\circ} \\ & \stackrel{\rightharpoonup}{\circ} \end{aligned}$ | $\begin{aligned} & \stackrel{10}{8} \\ & \stackrel{\otimes}{2} \\ & \stackrel{10}{2} \end{aligned}$ | $\left\|\begin{array}{c} 0 \\ 0 \\ 0 \\ \infty \\ \infty \\ \infty \end{array}\right\|$ |  | $\begin{gathered} \underset{\sim}{\underset{\sim}{N}} \\ \underset{\sim}{2} \end{gathered}$ |  | $\begin{gathered} \mathscr{\infty} \\ \underset{\sim}{\oplus} \\ \infty \\ \infty \end{gathered}$ | $\begin{aligned} & \stackrel{D}{\mathrm{I}} \\ & \underset{\mathrm{I}}{2} \end{aligned}$ | $\begin{aligned} & \text { in } \\ & 0 \\ & \infty \\ & 0 \\ & 0 \end{aligned}$ | $\begin{gathered} \Omega \\ \\ \stackrel{n}{0} \\ 1 \end{gathered}$ | $\begin{gathered} \underset{Z}{A} \\ \underset{\sim}{\mathrm{~N}} \end{gathered}$ | $\begin{aligned} & \text { 覴 } \end{aligned}$ | $\begin{array}{\|l\|l} \substack{0 \\ 0 \\ 0 \\ 0 \\ 子 \\ \hline} \end{array}$ |  | $\begin{gathered} \text { N } \\ \underset{\sim}{\mathrm{N}} \end{gathered}$ | $$ | $\begin{aligned} & \text { 式 } \\ & \text { No } \\ & \text { Non } \end{aligned}$ | $\left\|\begin{array}{c} 10 \\ 0 \\ \vdots \\ 0 \\ 0 \end{array}\right\|$ | $\left.\begin{array}{\|c} \stackrel{10}{0} \\ \infty \\ \\ \end{array} \right\rvert\,$ | \％ |
|  | $\begin{aligned} & \text { ه} \\ & \underset{\sim}{\infty} \\ & \end{aligned}$ | $\begin{aligned} & \mathrm{O} \\ & \mathrm{~N} \\ & \mathrm{O} \\ & \mathrm{i} \end{aligned}$ | $\begin{aligned} & 0 \\ & \underset{N}{0} \\ & 0 \\ & \end{aligned}$ | $\begin{aligned} & O \\ & \infty \\ & \infty \\ & \infty \\ & \underset{\sim}{0} \\ & \hline \end{aligned}$ | $\begin{gathered} \underset{\sim}{\circ} \\ \underset{\sim}{0} \\ \underset{\sim}{\infty} \end{gathered}$ | $\left.\begin{gathered} 0 \\ 0 \\ 0 \\ 0 \\ \dot{O} \end{gathered} \right\rvert\,$ | $\begin{gathered} \underset{0}{0} \\ \underset{\sim}{0} \end{gathered}$ | $\begin{aligned} & \underset{\sim}{\boldsymbol{m}} \\ & \underset{\sim}{\rightrightarrows} \end{aligned}$ | $\begin{aligned} & \stackrel{o}{\stackrel{ }{\wedge}} \\ & \stackrel{\wedge}{=} \end{aligned}$ | $\begin{aligned} & 0 \\ & \tilde{O} \\ & \text { O} \\ & \text { in } \end{aligned}$ | $\begin{aligned} & 0 \\ & \underset{\text { In }}{0} \\ & \text { a } \end{aligned}$ | $\begin{aligned} & O \\ & \stackrel{i}{n} \\ & 1 \\ & \underset{i}{i} \end{aligned}$ | $\begin{aligned} & 0 \\ & \\ & \\ & 0 \end{aligned}$ | $\begin{aligned} & 0 \\ & 0.0 \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \stackrel{\otimes}{7} \\ & \underset{\sim}{\circ} \end{aligned}$ | $\begin{aligned} & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ |  | $\left\|\begin{array}{c} 0 \\ \infty \\ 1 \\ \infty \\ \infty \end{array}\right\|$ | $\begin{aligned} & 0 \\ & \stackrel{0}{0} \\ & \underset{\sim}{0} \\ & \infty \end{aligned}$ | $\begin{gathered} \underset{\sim}{\underset{~}{~}} \\ \underset{\infty}{\prime} \end{gathered}$ | $\left\|\begin{array}{c} \underset{O}{0} \\ \infty \\ \infty \\ \infty \end{array}\right\|$ | $\left\lvert\, \begin{gathered} 9 \\ 0 \\ 0 \\ \infty \\ \infty \\ \infty \end{gathered}\right.$ | $\underset{\sim}{8}$ |
| 法 者 | $\underset{1}{8}$ | $\underset{木}{8}$ | $\stackrel{\underset{1}{2}}{\stackrel{\circ}{1}}$ | $\stackrel{8}{7}$ | $\underset{\substack{8 \\ \hline}}{ }$ | $\stackrel{8}{9}$ | $\stackrel{8}{7}$ | $\stackrel{8}{7}$ | $\underset{\substack{\circ \\ \hline}}{ }$ | $\underset{1}{8}$ | $8$ | $\stackrel{8}{9}$ | $\stackrel{8}{7}$ | $\stackrel{8}{7}$ | $\underset{\sim}{\underset{1}{\circ}}$ | $\stackrel{8}{7}$ | $\underset{i}{8}$ | $\underset{1}{8}$ | $\stackrel{\underset{7}{8}}{\stackrel{8}{1}}$ | $\stackrel{8}{9}$ | $\stackrel{8}{1}$ | $\stackrel{8}{7}$ | $\stackrel{8}{7}$ |
|  | 0 | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | 0 | － | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $\bigcirc$ | － | 0 | － | － | － |
| نِ | $\checkmark$ | $\rightarrow$ | $-$ | $-$ | $-$ | － | $-$ | $\rightarrow$ | $\rightarrow$ | $\cdots$ | $\rightarrow$ | $-$ | $\rightarrow$ | $\rightarrow$ | $-$ | － | $-$ | $\checkmark$ | － | $-$ | － | $-$ | － |
| $\begin{aligned} & \stackrel{\rightharpoonup}{0} \\ & \text { だ } \\ & \text { だ } \end{aligned}$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ |
|  | 앙 | 앙 | 18 | 18 | 18 | ） | 18 | \％ | g | gr | g | fr | $\stackrel{1}{8}$ | 낭 | ¢ | ¢ | 낭 | ¢ | ¢ | ¢ | － | ¢ | － |
|  | $\stackrel{8}{4}$ | $\stackrel{8}{4}$ | $\stackrel{8}{4}$ | $\stackrel{8}{4}$ | 8 | 8 | 8 | $\stackrel{8}{7}$ | 9 | $\stackrel{8}{9}$ | 9 | $\stackrel{9}{7}$ | $\stackrel{8}{4}$ | $\stackrel{8}{7}$ | 9 | $\stackrel{9}{9}$ | 8 | 8 | $\stackrel{9}{4}$ | 8 | $\stackrel{8}{4}$ | $\stackrel{9}{7}$ | $\stackrel{9}{7}$ |
|  | N | $\stackrel{1}{\text { ® }}$ | $\stackrel{\sim}{\circ}$ | ล | $\stackrel{\sim}{\sim}$ | $\stackrel{\sim}{\text { ® }}$ | ¢ | ल | ¢ | $\check{\gtrless}$ | ¢ | $\stackrel{4}{6}$ | $\because$ | － | $\propto$ | g | q | 7 | ホู | $\mathfrak{F}$ | \＃ | 18 | ¢ |

Table B．1．Computational results of the proposed algorithm．（cont．）

| U | $\checkmark$ | $\rightarrow$ | － | $\rightarrow$ | $\rightarrow$ | $\rightarrow$ | － | $\rightarrow$ | $\rightarrow$ | － | $\rightarrow$ | $\rightarrow$ | $\rightarrow$ | $\rightarrow$ | $\rightarrow$ | － | $-$ | $\rightarrow$ | － | $\rightarrow$ | $\rightarrow$ | $\rightarrow$ | － |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & \text { ô } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & 0 . \\ & 0 . \\ & 0 \\ & \dot{O} \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { 合 } \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { oig } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & 00 \\ & 0 \\ & 0 . \\ & 0 . \end{aligned}$ | $\begin{aligned} & \text { oo } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { ô } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { so } \\ & \text { ob } \\ & \stackrel{0}{0} \end{aligned}$ | $\begin{aligned} & 0 . \\ & 0 . \\ & 0 \\ & \dot{0} \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { ol } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { so } \\ & 0 . \\ & 0 . \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { ô } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & \hline 1 \end{aligned}$ | $\begin{aligned} & \text { 合 } \\ & 0 \\ & \dot{0} \\ & \hline \end{aligned}$ | $\begin{aligned} & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { of } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { ò } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { 合 } \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & 00 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { ob } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { ô } \\ & 0 \\ & \dot{6} \\ & \hline 0 \end{aligned}$ | $\begin{aligned} & \text { ô } \\ & \text { O} \\ & \text { O} \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { ồ } \\ & \text { ò } \\ & \text { B } \end{aligned}$ | 合 |
|  | $\begin{aligned} & \text { 合 } \\ & 0 \\ & \dot{O} \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { ồ } \\ & 0 \\ & 0 . \\ & 0 \\ & \hline \end{aligned}$ | $\begin{array}{\|c} 00 \\ 0 \\ 0 \\ \hline 0 \end{array}$ | $\begin{aligned} & 0 . \\ & 0 . \\ & 0 . \\ & 0 . \\ & \hline \end{aligned}$ | $\begin{aligned} & 00 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ |  | $\begin{aligned} & \text { ol } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { ồ } \\ & 0 \\ & \dot{0} \\ & \text { O} \end{aligned}$ | $\begin{aligned} & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { ol } \\ & 0 \\ & 0 \\ & 8 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { oi } \\ & 0 \\ & 8 \\ & 8 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { ol } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & 0 . \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & 00 \\ & 0 \\ & 0 \\ & \dot{0} \\ & \vdots \end{aligned}$ | $\begin{aligned} & \text { ol } \\ & 0 \\ & 0 \\ & \dot{0} \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { ờ } \\ & 0 \\ & \dot{6} \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { oi } \\ & 0 \\ & 8 \\ & 8 \\ & \hline \end{aligned}$ | $\begin{aligned} & 00 \\ & 0 \\ & 0 \\ & \dot{0} \\ & \dot{-1} \end{aligned}$ | $\begin{aligned} & \text { ol } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { ồ } \\ & 0 \\ & \dot{0} \\ & \text { O} \end{aligned}$ | $\begin{aligned} & \text { ô } \\ & \text { ò } \\ & \text { of } \end{aligned}$ | $\begin{aligned} & \text { ồ } \\ & \stackrel{0}{6} \\ & \text { B, } \end{aligned}$ | $\begin{aligned} & 0 . \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ |
|  | $\begin{aligned} & \text { of } \\ & 10 \\ & 10 \\ & 10 \end{aligned}$ | $\left\|\begin{array}{\|c} 20 \\ 10 \\ 1 \\ 1 \\ 1 \end{array}\right\|$ | $\begin{array}{\|c} 0 \\ 0 \\ 0 \\ \underset{\sim}{\infty} \end{array}$ | $\begin{array}{\|c} 00 \\ 10 \\ 10 \\ 10 \end{array}$ | $\begin{array}{\|c} \stackrel{\circ}{0} \\ \stackrel{e}{\mathrm{O}} \\ \underset{\sim}{2} \end{array}$ |  |  | $\begin{aligned} & \text { ô } \\ & \stackrel{\sim}{ٌ} \\ & \text { in } \end{aligned}$ |  | $\begin{gathered} \text { 合 } \\ \stackrel{\rightharpoonup}{9} \end{gathered}$ | $\begin{aligned} & \text { ô } \\ & \stackrel{\rightharpoonup}{6} \\ & \stackrel{\circ}{\circ} \end{aligned}$ | $\begin{aligned} & \text { ol } \\ & \stackrel{\rightharpoonup}{\mathrm{o}} \\ & \text { on } \end{aligned}$ |  | $\left.\begin{gathered} 00 \\ \stackrel{0}{9} \\ \dot{j} \end{gathered} \right\rvert\,$ |  | $\begin{aligned} & \text { co } \\ & \stackrel{\circ}{\circ} \\ & \end{aligned}$ | $\begin{array}{\|l\|} \hline 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{array}$ | $\left\|\begin{array}{c} 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{array}\right\|$ | $\begin{array}{\|l\|l} \hline 0 \\ \stackrel{0}{\mathrm{o}} \\ \text { © } \end{array}$ | $\begin{array}{\|c} \stackrel{\circ}{0} \\ \stackrel{\rightharpoonup}{9} \\ \infty \end{array}$ | $\begin{array}{\|c} \stackrel{\circ}{0} \\ \stackrel{0}{9} \\ \infty \end{array}$ |  |  |
|  | $\stackrel{18}{\sim}$ | $\stackrel{\text { คั }}{ }$ | ～ | $\stackrel{19}{\sim}$ | $\stackrel{\sim}{\sim}$ | $\stackrel{\text { คे }}{ }$ | $\stackrel{\text { ค }}{ }$ | ค | $\stackrel{\sim}{\sim}$ | $\stackrel{12}{2}$ | $\stackrel{12}{2}$ | $\stackrel{12}{7}$ | $\stackrel{12}{2}$ | $\stackrel{12}{2}$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | 9 | 15 | 15 | 10 | 15 |
|  | N | さ | F | ざ | 8 | 용 | $\stackrel{\circ}{\circ}$ | 8 | 8 | \＃ | \＆ | 18 | 夺 | \＃ | － | $\stackrel{\sim}{\circ}$ | ลิ | ¢ | ¢ | 12 | 12 | 12 | $\stackrel{12}{2}$ |
|  |  | $\left\|\begin{array}{c} 0 \\ 0 \\ 0 \\ 0 \\ \infty \end{array}\right\|$ | $\begin{aligned} & \infty \\ & \stackrel{\otimes}{\circledast} \\ & = \\ & = \end{aligned}$ | $\left\|\begin{array}{c} 0 \\ 7 \\ 7 \\ i \end{array}\right\|$ | $\left\|\begin{array}{c} 0 \\ \stackrel{0}{0} \\ \stackrel{\rightharpoonup}{\sigma} \end{array}\right\|$ | $\begin{array}{\|c} \substack{0 \\ Z \\ \underset{~}{2} \\ \hline} \end{array}$ | $\begin{array}{\|c} \stackrel{0}{0} \\ 0 \\ \infty \\ 0 \end{array}$ | $\begin{aligned} & 8 \\ & \stackrel{8}{\square} \\ & \underset{\sim}{2} \end{aligned}$ |  | $\begin{gathered} \underset{O}{O} \\ \underset{\sim}{7} \\ \underset{子}{2} \end{gathered}$ |  | $\begin{gathered} \underset{8}{8} \\ \underset{i}{8} \\ \hline 10 \end{gathered}$ | $\begin{aligned} & \stackrel{1}{0} \\ & \underset{\sim}{\circ} \\ & \infty \end{aligned}$ | $\left.\begin{gathered} \underset{\sim}{N} \\ \underset{N}{n} \end{gathered} \right\rvert\,$ | $\begin{aligned} & \stackrel{\gtrless}{\gtrless} \\ & \stackrel{\ominus}{\ominus} \\ & - \end{aligned}$ | $\begin{aligned} & \text { O} \\ & 0 \\ & 0 \\ & \text { in } \\ & \text { in } \end{aligned}$ | $\begin{aligned} & 0 \\ & \underset{N}{0} \\ & \infty \\ & \infty \end{aligned}$ | $\left.\begin{aligned} & 0 \\ & 1 \\ & 1 \\ & = \end{aligned} \right\rvert\,$ |  |  | $\begin{aligned} & \text { n} \\ & \stackrel{\sim}{i} \\ & \stackrel{\rightharpoonup}{n} \end{aligned}$ | $\begin{array}{\|c} \substack{80 \\ ⿻ 𨈑 ㇒\\ } \end{array}$ | ¢ |
|  | $\begin{gathered} 0 \\ \stackrel{0}{2} \\ \stackrel{0}{1} \\ \stackrel{1}{2} \end{gathered}$ | $\left\lvert\, \begin{gathered} 0 \\ \substack{0 \\ 10 \\ 10 \\ 1} \end{gathered}\right.$ | $\begin{aligned} & \stackrel{0}{0} \\ & \stackrel{N}{0} \\ & \stackrel{0}{1} \end{aligned}$ | $\begin{aligned} & 8 \\ & \stackrel{8}{10} \\ & \stackrel{4}{8} \end{aligned}$ | $\left\|\begin{array}{c} 0 \\ \stackrel{0}{\mathrm{~T}} \\ \stackrel{0}{0} \end{array}\right\|$ | $\left\lvert\,\right.$ | $\left.\begin{array}{\|c} 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{array} \right\rvert\,$ | $\begin{aligned} & \stackrel{\circ}{0} \\ & \stackrel{1}{\circ} \\ & \hline \end{aligned}$ | $\begin{gathered} 0 \\ \underset{7}{7} \\ \dot{6} \end{gathered}$ | $\begin{gathered} 8 \\ \underset{\sim}{2} \\ \hline 0 \end{gathered}$ | $\left\|\begin{array}{l} 0 \\ 0 \\ 0 \\ 0 \\ i \end{array}\right\|$ | $$ |  | $\left.\begin{gathered} 0 \\ 1 \\ 1 \\ 10 \\ 10 \end{gathered} \right\rvert\,$ | $\begin{aligned} & 8 \\ & \hline 8 \\ & \infty \\ & \rightarrow \\ & \rightarrow \end{aligned}$ | $\begin{aligned} & \text { O} \\ & \text { O} \\ & \text { Of } \end{aligned}$ | $\left\|\begin{array}{c} 0 \\ \substack{1 \\ 1 \\ 1 \\ f} \end{array}\right\|$ | $\left\lvert\, \begin{gathered} \infty \\ \underset{\sim}{\mathscr{Z}} \\ \underset{\sim}{2} \end{gathered}\right.$ | $\left\lvert\, \begin{gathered} P \\ N \\ N \\ \end{gathered}\right.$ | $\left.\begin{array}{\|c} 0 \\ \underset{\sim}{1} \\ \infty \\ \infty \end{array} \right\rvert\,$ | $\stackrel{\otimes}{\otimes}$ | $\begin{aligned} & \underset{y}{7} \\ & \underset{\sim}{n} \end{aligned}$ | ¢ |
| 法 | $\underset{1}{8}$ | $\underset{\substack{8 \\ 7 \\ \hline}}{ }$ | $\stackrel{8}{7}$ | $\underset{1}{8}$ | $\stackrel{8}{9}$ | $\underset{\substack{8 \\ \hline}}{ }$ | $\underset{1}{8}$ | $\stackrel{8}{7}$ | $\begin{array}{\|c} \stackrel{8}{7} \\ \hline \end{array}$ | $\stackrel{8}{7}$ | $\underset{1}{8}$ | $\underset{\sim}{\mathrm{O}}$ | $\underset{\underset{1}{8}}{8}$ | $\underset{\substack{8 \\ \hline}}{ }$ | $\stackrel{8}{7}$ | $\underset{\underset{1}{\circ}}{8}$ | $\stackrel{8}{9}$ | $\begin{array}{\|l\|} \hline 0 \\ \vdots \end{array}$ | $\underset{\substack{8 \\ \hline}}{ }$ | $\stackrel{8}{7}$ | $\underset{7}{8}$ | $\stackrel{8}{4}$ | $\stackrel{8}{1}$ |
|  | 0 | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | － | $\bigcirc$ | 0 | $\bigcirc$ | $\bigcirc$ | 0 | 0 | $\bigcirc$ | － | － | 0 | $\bigcirc$ | － | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
|  | $\rightarrow$ | $-$ | － | $\rightarrow$ | $\rightarrow$ | $\rightarrow$ | － | $-$ | $\checkmark$ | － | $-$ | $\rightarrow$ | $\rightarrow$ | $\rightarrow$ | － | $-$ | － | － | － | $-$ | $\rightarrow$ | $-$ | － |
|  | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ |
|  | เู | $\stackrel{19}{\text {－}}$ | ำ | เฺ | $\stackrel{\text { ® }}{ }$ | ค | ค | ค | $\stackrel{1}{2}$ | $\stackrel{12}{2}$ | $\stackrel{12}{9}$ | $\stackrel{12}{9}$ | $\stackrel{19}{9}$ | $\stackrel{12}{2}$ | 9 | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | 9 | 15 | $\bigcirc$ | 10 | 10 |
|  | 8 | 9 | $\stackrel{8}{4}$ | 8 | 8 | 9 | $\stackrel{9}{7}$ | $\stackrel{8}{4}$ | 8 | $\stackrel{8}{4}$ | $\stackrel{8}{7}$ | $\stackrel{9}{7}$ | $\stackrel{8}{7}$ | $\stackrel{8}{4}$ | $\stackrel{9}{7}$ | $\stackrel{9}{4}$ | $\stackrel{8}{4}$ | 8 | $\stackrel{9}{8}$ | 8 | $\stackrel{9}{9}$ | $\stackrel{1}{8}$ | $\stackrel{8}{7}$ |
| 岱 | $\stackrel{\text { F }}{ }$ | $\stackrel{\infty}{\square}$ | ¢ | 옹 | $\stackrel{1}{2}$ | ํ | \％ | 4 | 18 | $\stackrel{\circ}{\circ}$ | is | $\infty$ | 品 | 8 | $\square$ | © | $\%$ | ¢ | 8 | 8 | $\stackrel{\square}{6}$ | $\infty$ | 8 |

Table B．1．Computational results of the proposed algorithm．（cont．）

| Uّ \＃ | $\rightarrow$ | $\rightarrow$ | $\rightarrow$ | $\rightarrow$ | $\rightarrow$ | $\rightarrow$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | N | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | N | $\sim$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & 0 . \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\left\lvert\, \begin{aligned} & 00 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}\right.$ | $\begin{aligned} & \text { so } \\ & \text { ob } \\ & \text { O} \end{aligned}$ | $\begin{aligned} & \text { so } \\ & 0 . \\ & \dot{0} \\ & \hline 0 \end{aligned}$ | $\begin{aligned} & \text { of } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { so } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \mathrm{O} \\ & \stackrel{0}{\mathrm{O}} \\ & \stackrel{\theta}{0} \end{aligned}$ | $\begin{aligned} & \text { so } \\ & \text { O} \\ & \text { O. } \end{aligned}$ | $\begin{aligned} & \text { OO } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { so } \\ & 0 . \\ & 0 . \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { so } \\ & 0 . \\ & 0 . \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { so } \\ & 0 . \\ & \dot{0} \\ & \hline 0 \end{aligned}$ | $\begin{aligned} & \text { of } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & 00 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { 合 } \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { ô } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { so } \\ & 0 . \\ & 0 . \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { ồ } \\ & \stackrel{0}{\dot{0}} \\ & \text { 2, } \end{aligned}$ | $\begin{aligned} & \text { 合 } \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { so } \\ & 0 . \\ & 0 . \\ & 0 \end{aligned}$ | $\left\|\begin{array}{l} 00 \\ 0 \\ 0 \\ \dot{0} \\ 0 \end{array}\right\|$ | $\begin{aligned} & \text { so } \\ & 0 \\ & \dot{0} \\ & 0 \end{aligned}$ | 合 |
|  | $\begin{aligned} & \text { ơ } \\ & 0 \\ & 0 . \\ & 0 \\ & 0 \end{aligned}$ | $\left.\begin{aligned} & 00 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned} \right\rvert\,$ | $\begin{aligned} & \text { ô } \\ & \text { O} \\ & \text { O. } \end{aligned}$ | $\begin{aligned} & \text { oi } \\ & 0 . \\ & 0 . \\ & 0 . \end{aligned}$ | $\begin{aligned} & \text { oig } \\ & 0 . \\ & 0 . \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { ò } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { SO } \\ & \text { ou } \\ & \text { ín } \end{aligned}$ |  |  | $\begin{aligned} & \text { so } \\ & \text { M } \\ & \text { 广í } \end{aligned}$ | $\begin{gathered} \text { ò } \\ \stackrel{1}{4} \\ \dot{O} \end{gathered}$ | $\begin{aligned} & 80 \\ & 0 \\ & 0 \\ & 0 \\ & 8 \end{aligned}$ |  | $\begin{array}{\|c\|c} 00 \\ 0 \\ 0 \\ \infty \\ 0 \end{array}$ |  | $\begin{aligned} & 0 \\ & \infty \\ & 0 \\ & \underset{O}{6} \end{aligned}$ |  |  |  | $\begin{aligned} & \text { sio } \\ & 0 \\ & \stackrel{.}{\circ} \end{aligned}$ | $\begin{array}{\|c} \substack{0 \\ \hat{6} \\ e \\ 0 \\ 0} \end{array}$ | $\begin{array}{\|c\|c\|} \infty \\ \infty \\ \infty \\ \infty \\ \infty \end{array}$ | 旍 |
|  | $\begin{aligned} & \stackrel{\circ}{\rightrightarrows} \\ & \underset{\sim}{\circ} \end{aligned}$ | $\begin{array}{\|c\|c} \substack{0 \\ e \\ 0 \\ 0 \\ \hline} \end{array}$ | $\begin{aligned} & \text { ôe } \\ & \text { O. } \end{aligned}$ | $\begin{aligned} & \text { êe } \\ & \text { êe } \\ & \hline 0 \end{aligned}$ |  |  |  | $\begin{array}{\|c} \substack{0 \\ e \\ e \\ e \\ 0 \\ \hline} \end{array}$ | $\begin{array}{\|c} \substack{0 \\ 0 \\ e \\ e \\ 0 \\ \hline \\ \hline} \end{array}$ | $\begin{aligned} & \text { so } \\ & \text { è } \\ & \underset{\sim}{\circ} \end{aligned}$ |  | $\begin{aligned} & \text { ô } \\ & \stackrel{0}{0} \\ & \stackrel{1}{0} \end{aligned}$ |  | $\left\lvert\, \begin{gathered} \substack{0 \\ 0 \\ 0 \\ N \\ \dot{N} \\ \text { N }} \end{gathered}\right.$ |  |  | $\begin{array}{\|c} \substack{\text { on } \\ \underset{\sim}{j} \\ \hline} \end{array}$ |  |  |  | $\begin{array}{\|c} \substack{0 \\ \underset{~}{c} \\ \underset{\sim}{i} \\ \hline} \end{array}$ | $\begin{array}{\|c} \substack{o \\ \underset{\sim}{n} \\ \underset{\sim}{\mathrm{~N}}} \end{array}$ |  |
|  | $\bigcirc$ | $\checkmark$ | $-$ | $\checkmark$ | $\checkmark$ | － | 4 | $\stackrel{18}{6}$ | 8 | 18 | 4 | $\overline{6}$ | $\square$ | 6 | $\overline{6}$ | ก | $\stackrel{\circ}{\circ}$ | $\because$ | 10 | 合 | $\infty$ | H | \％ |
|  | $\stackrel{19}{2}$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\stackrel{\text { a }}{ }$ | $\stackrel{\text { a }}{ }$ | － | $\stackrel{\circ}{\mathrm{I}}$ | $\stackrel{9}{\mathrm{I}}$ | 극 | $\stackrel{\rightharpoonup}{-}$ | $\stackrel{\text { I }}{ }$ | İ | $\stackrel{\cong}{\beth}$ | $\exists$ | $\exists$ | $\ddot{7}$ | $\underset{7}{2}$ | $\stackrel{9}{7}$ | － | $\stackrel{2}{2}$ |
|  |  | $\left\|\begin{array}{c} o \\ 0 \\ 0 \\ 1 . \\ 1 \\ 1 \end{array}\right\|$ |  | $\begin{aligned} & \stackrel{8}{8} \\ & 0 \\ & 0 \\ & \hline 1 \end{aligned}$ | $\begin{aligned} & \mathrm{O} \\ & \hline \mathbf{O} \\ & - \\ & -1 \end{aligned}$ | $\begin{array}{r} 8 \\ \hline 8 \\ 0 \\ 0 \\ \dot{8} \end{array}$ | $\begin{aligned} & \stackrel{\circ}{8} \\ & \hline \mathrm{O} \\ & \mathrm{o} \end{aligned}$ | $\left\|\begin{array}{c} \substack{0 \\ 0 \\ 0 \\ \infty \\ \infty} \end{array}\right\|$ |  | $\begin{aligned} & \mathrm{O} \\ & \hline \mathrm{O} \\ & \mathrm{o} \\ & \text { on } \end{aligned}$ | $\begin{aligned} & \stackrel{8}{8} \\ & \stackrel{\rightharpoonup}{\infty} \\ & \infty \end{aligned}$ | $\begin{aligned} & \text { o} \\ & \substack{0 \\ 0 \\ 0} \end{aligned}$ | $\begin{aligned} & \mathrm{O} \\ & \stackrel{\rightharpoonup}{\circ} \\ & \underset{\sim}{n} \end{aligned}$ | $\left\lvert\, \begin{gathered} 9 \\ \underset{\sim}{N} \\ \underset{N}{2} \end{gathered}\right.$ |  |  | $\begin{aligned} & \text { or } \\ & \stackrel{\theta}{\circ} \\ & \dot{\theta} \end{aligned}$ | $\begin{gathered} \mathscr{N} \\ \underset{\sim}{\infty} \\ \infty \end{gathered}$ | $\left\lvert\, \begin{gathered} 0 \\ 0 \\ \infty \\ \infty \\ 0 \end{gathered}\right.$ | $\begin{aligned} & \text { No } \\ & \substack{0 \\ 0 \\ 0} \end{aligned}$ | $\begin{aligned} & \stackrel{0}{0} \\ & \stackrel{0}{0} \\ & 0 \\ & 0 \end{aligned}$ | $\begin{gathered} \overrightarrow{0} \\ \infty \\ \infty \\ 0 \end{gathered}$ | N |
| $\begin{aligned} & \text { 吉 } \\ & \stackrel{0}{0} \\ & \stackrel{0}{0} \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \underset{\sim}{\mathrm{N}} \\ & \infty \\ & \underset{\sim}{\infty} \end{aligned}$ | $\left\lvert\, \begin{gathered} \underset{8}{8} \\ \underset{\substack{2}}{i} \end{gathered}\right.$ | $\begin{gathered} \stackrel{\rightharpoonup}{\mathrm{o}} \\ \stackrel{\sim}{\mathrm{~N}} \end{gathered}$ | $\begin{aligned} & \underset{\mathrm{A}}{\mathrm{O}} \\ & \underset{\sim}{\mathrm{~N}} \end{aligned}$ | $\left\|\begin{array}{c} \underset{\sim}{\infty} \\ \stackrel{\infty}{\mathrm{i}} \end{array}\right\|$ |  | $\begin{aligned} & 8 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{gathered} 0 \\ \underset{7}{9} \\ \underset{\sim}{\infty} \end{gathered}$ | $\begin{aligned} & 0 \\ & \stackrel{0}{A} \\ & \underset{\infty}{\infty} \end{aligned}$ | $\begin{aligned} & \stackrel{\circ}{\circ} \\ & \stackrel{0}{0} \\ & \underset{\sim}{\infty} \end{aligned}$ | $\begin{array}{\|c} \underset{\sim}{\underset{N}{N}} \\ \underset{\sim}{\infty} \end{array}$ |  | $\begin{aligned} & \text { N } \\ & \text { N } \\ & \underset{\sim}{1} \end{aligned}$ | $\begin{array}{\|c} 0 \\ 0 \\ 0 \\ \underset{\sim}{0} \\ \underset{0}{2} \end{array}$ |  | $\begin{aligned} & \circ \\ & \stackrel{\otimes}{6} \\ & \stackrel{\rightharpoonup}{\dot{~}} \end{aligned}$ | $\begin{gathered} 0 \\ 0 \\ 0 \\ \underset{-}{\bullet} \end{gathered}$ | $\begin{aligned} & \stackrel{0}{8} \\ & \stackrel{0}{0} \\ & \stackrel{\oplus}{0} \end{aligned}$ |  |  | $\left\|\begin{array}{c} \underset{\sim}{O} \\ \underset{\infty}{\infty} \\ \stackrel{\rightharpoonup}{n} \end{array}\right\|$ |  |  |
| 没 考 | $\underset{1}{8}$ | $\underset{\substack{8 \\ \hline \\ \hline}}{ }$ | $\underset{\substack{8 \\ \hline}}{ }$ | $\underset{1}{8}$ | $\underset{\sim}{8}$ | $\underset{\substack{\mathrm{O}}}{ }$ | $\underset{1}{8}$ | $\stackrel{8}{9}$ | $\underset{木}{8}$ | $\underset{\sim}{8}$ | $\underset{\substack{8 \\ \hline}}{ }$ | $\underset{\substack{8 \\ \hline \\ \hline}}{ }$ | $\underset{\square}{8}$ | $\stackrel{8}{9}$ | $\underset{7}{8}$ | $\underset{1}{8}$ | $\underset{\substack{8 \\ \hline}}{ }$ | $\underset{1}{8}$ | $\underset{\substack{8 \\ \hline}}{ }$ | $\underset{1}{8}$ | $\underset{\sim}{8}$ | $\underset{\substack{8 \\ \hline 1 \\ \hline}}{ }$ | $\stackrel{8}{1}$ |
|  | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | 0 | 0 | － | － | $\bigcirc$ | － | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | 0 | $\bigcirc$ | － | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | － | － | $\bigcirc$ |
| （1） | $\cdots$ | $-$ | $-$ | $\cdots$ | $\rightarrow$ | $\rightarrow$ | － | $\rightarrow$ | $\sim$ | － | $-$ | － | $\rightarrow$ | $\rightarrow$ | － | $\rightarrow$ | $-$ | $\rightarrow$ | $-$ | $-$ | $\rightarrow$ | $\rightarrow$ | $\rightarrow$ |
| $\begin{aligned} & \stackrel{\rightharpoonup}{\mathrm{N}} \\ & \text { た } \\ & \text { だ } \end{aligned}$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | ～ | $\sim$ | $\sim$ | $\sim$ | ～ | $\sim$ | $\sim$ | ～ | $\sim$ |
|  | $\sim$ | $\checkmark$ | $-$ | $\checkmark$ | $\checkmark$ | $-$ | 앙 | 9 | 8 | 8 | 8 | 18 | 48 | $\stackrel{1}{8}$ | 8 | 48 | 8 | 8 | 8 | 8 | 8 | 18 | 号 |
|  | $\stackrel{8}{4}$ | 8 | 9 | $\stackrel{8}{4}$ | $\stackrel{9}{4}$ | 8 | $\stackrel{9}{4}$ | 9 | $\stackrel{9}{9}$ | 8 | 8 | $\stackrel{8}{7}$ | 9 | $\stackrel{8}{4}$ | $\stackrel{9}{9}$ | 8 | 8 | 9 | $\stackrel{8}{7}$ | $8$ | $\stackrel{9}{7}$ | $\stackrel{9}{4}$ | $\stackrel{8}{4}$ |
|  | $\bigcirc$ | N | ก | ® | 䍗 | 10 | P1 | N | $\stackrel{\infty}{\sim}$ | 9 | $\stackrel{\circ}{\infty}$ | $\vec{\infty}$ | ¢ | $\propto$ | － | 4 | $\otimes$ | － | $\infty$ | $\otimes$ | 8 | E | § |

Table B．1．Computational results of the proposed algorithm．（cont．）

| Uّ \＃ | $\sim$ | $\sim$ | ～ | $\sim$ | $\sim$ | $\sim$ | ค | $\sim$ | N | $\sim$ | ～ | $\sim$ | $\sim$ | $\sim$ | ～ | N | $\sim$ | $\sim$ | ～ | $\sim$ | $\sim$ | $\sim$ | $\sim$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & \text { so } \\ & 0 \\ & \dot{0} \\ & 0 \end{aligned}$ | $\begin{aligned} & 0 . \\ & 0 \\ & 0 \\ & \dot{0} \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { so } \\ & 0 . \\ & 0 . \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { ồ } \\ & 0 . \\ & \stackrel{\theta}{0} \\ & \hline \end{aligned}$ | $\left\lvert\, \begin{aligned} & 00 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}\right.$ | $\begin{aligned} & \text { so } \\ & \text { © } \\ & \text { O} \end{aligned}$ | $\begin{aligned} & \text { so } \\ & 0 . \\ & 0 . \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { so } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & 00 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { 合 } \\ & 0 \\ & \dot{0} \\ & \hline 0 \end{aligned}$ | $\begin{aligned} & \text { so } \\ & \text { ob } \\ & \stackrel{0}{6} \end{aligned}$ | $\begin{aligned} & \text { 合 } \\ & 0 \\ & \dot{0} \\ & \hline 0 \end{aligned}$ | $\begin{aligned} & \text { of } \\ & 0 . \\ & 0 . \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { of } \\ & 0 . \\ & 0 . \\ & 0 . \end{aligned}$ | $\begin{aligned} & 0 . \\ & 0 . \\ & 0 . \\ & 0 . \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { 合 } \\ & 0 \\ & \dot{0} \\ & \hline \end{aligned}$ |  | $\begin{aligned} & \text { so } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & 0.0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & 00 \\ & 0 \\ & 0 \\ & \dot{O} \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { ồ } \\ & \stackrel{0}{0} \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { 合 } \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $$ |
|  | $\begin{aligned} & \text { co } \\ & 10 \\ & 10 \\ & 0 \\ & \text { O} \end{aligned}$ |  |  | $\begin{aligned} & \text { ö } \\ & \stackrel{0}{\dot{0}} \\ & \dot{8} \end{aligned}$ | $\left.\begin{array}{\|c} 00 \\ 0 \\ 0 \\ \dot{8} \end{array} \right\rvert\,$ | $\begin{aligned} & \text { ol } \\ & \text { of } \\ & \text { ᄋ } \end{aligned}$ | $\begin{aligned} & \text { B0 } \\ & \text { O} \\ & \text { í } \end{aligned}$ | $\begin{aligned} & \text { ol } \\ & 0 \\ & o \\ & \infty \\ & \infty \end{aligned}$ | $\begin{aligned} & 00 \\ & 0.0 \\ & i 0 \\ & 8.8 \end{aligned}$ |  |  | $\begin{aligned} & 00 \\ & 0.0 \\ & i 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { ol } \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { ol } \\ & \text { ob } \\ & \text { id } \end{aligned}$ | $\begin{array}{\|c} 00 \\ 0 \\ \text { of } \\ \text { ig } \end{array}$ | $\begin{aligned} & \text { so } \\ & 0 \\ & 0 \\ & \vdots \\ & \hline 0 \end{aligned}$ | $\begin{aligned} & \text { ol } \\ & 00 \\ & \stackrel{0}{6} \end{aligned}$ | $\begin{array}{\|c} 00 \\ 0 \\ 0 . \\ i . \end{array}$ | $\begin{aligned} & \text { ol } \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{array}{\|c} \substack{0 \\ \underset{\sim}{4} \\ \underset{\sim}{1}} \end{array}$ | $\begin{aligned} & 50 \\ & \underset{\sim}{4} \\ & \underset{5}{5} \end{aligned}$ |  | $\begin{aligned} & 80 \\ & 0 . \\ & 0 . \\ & 0 \end{aligned}$ |
|  | $\begin{aligned} & \text { ol } \\ & 0 \\ & \text { B0 } \\ & \text { in } \end{aligned}$ | $\left\|\begin{array}{l} 00 \\ 0 \\ 0 \\ \underset{\sim}{\mathrm{~A}} \end{array}\right\|$ |  | $\begin{aligned} & o 0^{\circ} \\ & \infty \\ & \infty \\ & \dot{9} \end{aligned}$ | $\begin{array}{\|c\|} \hline 0 \\ 0 \\ 0 \\ 0 \\ \underset{\sim}{2} \end{array}$ | $\begin{aligned} & \text { هొ } \\ & \\ & \dot{\sim} \end{aligned}$ | $\begin{gathered} \stackrel{\circ}{\mathrm{O}} \\ \underset{\sim}{\mathrm{j}} \end{gathered}$ | $\left\|\begin{array}{\|c\|} \hline 0 \\ 0 \\ 0 \\ 0 \\ \end{array}\right\|$ | $\begin{array}{\|c} \substack{0 \\ 10 \\ \\ \\ \hline} \end{array}$ | $\begin{aligned} & \text { 吡 } \\ & \stackrel{N}{へ} \\ & \end{aligned}$ | $\begin{aligned} & \stackrel{\circ}{0} \\ & \stackrel{\leftrightarrow}{\infty} \\ & \underset{\sim}{0} \end{aligned}$ | $\begin{array}{\|c} \substack{0 \\ 1 \\ N \\ N\\ } \end{array}$ | $\begin{aligned} & \infty \\ & \infty \\ & \infty \\ & \infty \\ & \infty \\ & \infty \end{aligned}$ | $\left\lvert\, \begin{gathered} 80 \\ \stackrel{0}{0} \\ \stackrel{0}{n} \end{gathered}\right.$ | $\left\lvert\, \begin{array}{\|c} \substack{0 \\ 0 \\ 0 \\ 1 \\ ~} \end{array}\right.$ |  | $\begin{aligned} & \text { ol } \\ & \infty \\ & 0 \\ & 0 \end{aligned}$ | $\left\lvert\, \begin{array}{\|c} 00 \\ 0.0 \\ 0 . \\ 10 \\ 1 \end{array}\right.$ | $\left.\begin{array}{\|c} 0 \\ 0 \\ 0 \\ -1 \end{array} \right\rvert\,$ | $\begin{array}{\|c} \hline 0 \\ \underset{\dot{\circ}}{\mathrm{o}} \\ \underset{\sim}{2} \end{array}$ | $\begin{array}{\|c} \stackrel{\circ}{\circ} \\ \stackrel{\rightharpoonup}{\dot{~}} \\ \dot{\sim} \end{array}$ |  | $\begin{aligned} & 00 \\ & 7 \\ & \ddagger \end{aligned}$ |
|  | \％ | ํ． | \％ | $\stackrel{\infty}{\sim}$ | $\stackrel{\sim}{\square}$ | $\stackrel{\sim}{\square}$ | － | $\stackrel{9}{4}$ | $\stackrel{7}{7}$ | \％ | F | \％ | － | $\infty$ | $\infty$ | \％ | ค） | $\propto$ | 뇽 | \＃ | ¢ | \＃ | $\stackrel{1}{8}$ |
|  | $\stackrel{\circ}{\sim}$ | \％ | $\stackrel{2 g}{\square}$ | 8 | 8 | 8 | ¢๐ | ¢ | $\stackrel{8}{8}$ | $\stackrel{1}{\infty}$ | － | $\stackrel{1}{\infty}$ | $\stackrel{8}{\infty}$ | 10 | R | ® | N | R | $\bigcirc$ | ¢ | $\stackrel{5}{6}$ | ¢ | 8 |
|  |  | $\left\lvert\, \begin{aligned} & \substack{0 \\ 0 \\ \\ 1} \end{aligned}\right.$ | $\begin{gathered} \underset{9}{9} \\ \underset{\sim}{0} \\ \stackrel{0}{0} \end{gathered}$ |  |  | $\begin{aligned} & \stackrel{\text { O}}{\infty} \\ & \stackrel{\circ}{\circ} \\ & \end{aligned}$ | $\begin{gathered} \text { ôe } \\ \substack{0 \\ 0} \end{gathered}$ | $\begin{gathered} \underset{\sim}{0} \\ \stackrel{1}{1} \end{gathered}$ | $\begin{gathered} \infty \\ \infty \\ \\ \underset{\sim}{c} \\ \hline \end{gathered}$ |  | $\begin{aligned} & \text { N } \\ & \stackrel{1}{0} \\ & \stackrel{i}{2} \end{aligned}$ |  |  | $\left\|\begin{array}{c} 8 \\ \hline 8 \\ \hline \\ 1 \end{array}\right\|$ | $\left.\begin{gathered} 0 \\ \substack{0 \\ 1 \\ 10} \end{gathered} \right\rvert\,$ |  | $\begin{aligned} & \text { Nơo } \\ & \stackrel{\substack{0}}{0} \end{aligned}$ | $\left\|\begin{array}{c} 1 \\ \hline 0 \\ \vdots \\ 1 \end{array}\right\|$ |  | $\left\|\begin{array}{l} 0 \\ 1 \\ \hat{0} \\ 0 \end{array}\right\|$ |  |  | $\begin{aligned} & \text { r} \\ & \stackrel{y}{0} \\ & \substack{0} \end{aligned}$ |
|  | $\left\lvert\, \begin{gathered} 0 \\ N \\ \\ \underset{\sim}{1} \end{gathered}\right.$ |  | $\begin{gathered} 0 \\ 0.0 \\ \dot{U} \\ \underset{\sim}{2} \end{gathered}$ | $\left.\begin{gathered} \underset{7}{\rightrightarrows} \\ \underset{\sim}{2} \end{gathered} \right\rvert\,$ |  | $\begin{aligned} & \stackrel{\circ}{\circ} \\ & \stackrel{\rightharpoonup}{m} \\ & \underset{\sim}{n} \end{aligned}$ | $\begin{aligned} & \underset{\sim}{f} \\ & \infty \\ & \underset{\sim}{2} \end{aligned}$ | $\begin{gathered} 0 \\ \stackrel{\rightharpoonup}{\infty} \\ \stackrel{\rightharpoonup}{i} \\ \stackrel{1}{2} \end{gathered}$ | $\begin{gathered} o \\ 0 \\ 0 \\ 0 \\ \mathrm{i} \end{gathered}$ | $\begin{aligned} & 0 \\ & 0 \\ & 1 \\ & 1 \\ & -1 \end{aligned}$ | $\begin{aligned} & 8 \\ & \stackrel{8}{1} \\ & 1 \\ & - \\ & 7 \end{aligned}$ | $\begin{gathered} P \\ \hat{N} \\ \vdots \\ - \\ - \end{gathered}$ | $$ | $\begin{aligned} & 0 \\ & 0 \\ & 0 \\ & 0 \\ & \end{aligned}$ | $\begin{gathered} 0 \\ 0 \\ \underset{\sim}{0} \\ \dot{Q} \end{gathered}$ | $$ | $\begin{gathered} 0 \\ \stackrel{\oplus}{0} \\ \stackrel{0}{0} \end{gathered}$ | $\left\lvert\, \begin{gathered} \underset{\sim}{\underset{1}{\mathrm{j}}} \\ \underset{\sim}{2} \end{gathered}\right.$ | $\begin{gathered} \stackrel{\rightharpoonup}{\mathrm{O}} \\ \mathrm{O} \\ \mathrm{O} \end{gathered}$ | $\left\|\begin{array}{l} 0 \\ \stackrel{R}{0} \\ 0 \\ 0 \\ 0 \end{array}\right\|$ | $\begin{aligned} & 8 \\ & \hline 8 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \stackrel{\circ}{0} \\ & \stackrel{\rightharpoonup}{\mathrm{~N}} \\ & \underset{\sigma}{2} \end{aligned}$ | ¢ |
| 制 | $\underset{1}{8}$ | $\stackrel{8}{7}$ | $\underset{7}{8}$ | $\underset{1}{8}$ | $\underset{\substack{8 \\ \hline \\ \hline}}{ }$ | $\underset{\substack{8 \\ \hline}}{ }$ | $\underset{1}{8}$ | $\stackrel{8}{9}$ | $\underset{\substack{8 \\ \hline \\ \hline}}{ }$ | $\underset{1}{8}$ | $\stackrel{8}{9}$ | $\underset{\substack{8 \\ \hline \\ \hline}}{ }$ | $\underset{1}{8}$ | $\stackrel{8}{7}$ | $\underset{\substack{8 \\ \hline \\ \hline}}{ }$ | $\stackrel{8}{7}$ | $\underset{\substack{8 \\ \hline \\ \hline}}{ }$ | $\underset{\substack{8 \\ \hline 1 \\ \hline}}{ }$ | $\underset{\substack{8 \\ 1 \\ \hline}}{ }$ | $\underset{\sim}{8}$ | $\underset{\substack{8 \\ \hline \\ \hline}}{ }$ | $\underset{木}{8}$ | $\stackrel{8}{7}$ |
|  | $\bigcirc$ | － | $\bigcirc$ | 0 | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | 0 | － | $\bigcirc$ | 0 | $\bigcirc$ | $\bigcirc$ | － | $\bigcirc$ | － | 0 |
|  | $-$ | $\checkmark$ | $-$ | $\rightarrow$ | $-$ | $-$ | $-$ | $\checkmark$ | $\checkmark$ | $-$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $-$ | $\checkmark$ | $\checkmark$ | $-$ | $\checkmark$ | $-$ | － | $-$ | $-$ | $\rightarrow$ |
| $\begin{aligned} & \text { さे } \\ & \text { だ } \\ & \text { だ } \end{aligned}$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | ค | N | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | ～ | $\sim$ |
|  | 18 | 绍 | 绍 | 앙 | 옹 | 옹 | 옹 | 옹 | ！ | $\stackrel{18}{4}$ | 18 | 18 | 夺 | q | \％ | g | \％ | 9 | ¢ | $\stackrel{9}{8}$ | $\stackrel{8}{8}$ | 18 | ¢ |
|  | 8 | $\stackrel{9}{4}$ | $\stackrel{8}{7}$ | $\stackrel{8}{4}$ | 8 | 8 | 8 | 8 | $\stackrel{8}{4}$ | $\stackrel{9}{4}$ | $8$ | 8 | $\stackrel{9}{7}$ | $\stackrel{8}{7}$ | 8 | $\stackrel{8}{4}$ | 9 | 8 | $\stackrel{8}{7}$ | 9 | 8 | $\stackrel{9}{8}$ | 9 |
|  | ®＇ | あ | 8 | 8 | ¢ | $\stackrel{\infty}{\circ}$ | 8 | $\stackrel{\square}{-1}$ | $\stackrel{\rightharpoonup}{\square}$ | No | \％ | $\stackrel{\text { O }}{\substack{\text { a }}}$ | $\stackrel{2}{\square}$ | $\stackrel{\circ}{-}$ | $\stackrel{\text {－}}{\square}$ | $\stackrel{\infty}{\sim}$ | $\stackrel{\otimes}{-1}$ | $\bigcirc$ | $\exists$ | Э | $\stackrel{\square}{7}$ | $\underset{\sim}{Z}$ | $\stackrel{12}{7}$ |

Table B．1．Computational results of the proposed algorithm．（cont．）

| U | $\sim$ | $\sim$ | $\sim$ | $\sim$ | ค | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | ～ | $\sim$ | N | ค | $\sim$ | $\sim$ | $\sim$ | $\sim$ | ค | $\sim$ | N | $\sim$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & \text { 合 } \\ & 0 \\ & \dot{0} \\ & \hline 0 \end{aligned}$ | $\begin{aligned} & 00 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ |  | $\begin{aligned} & \text { of } \\ & 0 . \\ & 0 . \\ & 0 . \end{aligned}$ | $\left\|\begin{array}{l} 00 \\ 0 \\ 0 \\ 0 \\ 0 \end{array}\right\|$ | $\begin{aligned} & \text { oo } \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { 合 } \\ & 0 \\ & \dot{0} \\ & \hline 0 \end{aligned}$ | $\begin{aligned} & 00 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { of } \\ & 0 . \\ & 0 . \\ & 0 . \\ & \hline 1 \end{aligned}$ | $\begin{aligned} & \text { of } \\ & 0 . \\ & 0 . \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { ô } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { so } \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { 合 } \\ & 0 \\ & \dot{0} \\ & \hline 0 \end{aligned}$ | $\left\lvert\, \begin{aligned} & 00 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}\right.$ | $\begin{aligned} & \text { ờ } \\ & \text { O. } \\ & \text { O} \end{aligned}$ | $\begin{aligned} & \text { so } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { oi } \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { ob } \\ & \text { ó } \\ & \text { O} \end{aligned}$ | $\begin{aligned} & 0.0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { so } \\ & \text { ob } \\ & \stackrel{0}{0} \end{aligned}$ | $\begin{aligned} & \text { ob } \\ & \text { ob } \\ & \text { B. } \end{aligned}$ | $\begin{aligned} & \text { ô } \\ & \text { O. } \\ & \text { O} \end{aligned}$ | 合 |
|  | $\begin{aligned} & \text { so } \\ & 0 \\ & 0 \\ & \vdots \\ & \hline 0 \end{aligned}$ | $\begin{aligned} & 0 \\ & 0 \\ & 0 \\ & \vdots \\ & \vdots \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { ob } \\ & \text { ob } \\ & \text { B } \end{aligned}$ | $\begin{array}{\|c} \substack{0 \\ \hat{0} \\ \stackrel{y}{8} \\ \hline \\ \hline} \end{array}$ | $\left.\begin{aligned} & 00 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned} \right\rvert\,$ | $\begin{array}{\|c} 00 \\ 0 \\ 0 \\ 0 \end{array}$ | $\begin{aligned} & \text { so } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\left.\begin{array}{\|c} 00 \\ 0 \\ 0 \\ \dot{8} \end{array} \right\rvert\,$ | $\begin{aligned} & \text { oㅇ } \\ & \text { of } \\ & 0 . \\ & 0.1 \end{aligned}$ | $\begin{aligned} & \text { ol } \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { so } \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { of } \\ & 0 \\ & 0 . \\ & \stackrel{9}{\circ} \end{aligned}$ | $\begin{aligned} & \text { so } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & 0 \\ & 0 \\ & 0 \\ & \vdots \\ & \vdots \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { so } \\ & \text { O. } \\ & \text { ód } \end{aligned}$ | $\begin{aligned} & \text { oi } \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ |  |  | $\begin{aligned} & 80 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ |  | $\begin{aligned} & \text { so } \\ & \text { ó } \\ & \text { B } \end{aligned}$ | $\begin{aligned} & \text { ồ } \\ & \stackrel{0}{6} \\ & \text { in } \end{aligned}$ | $\begin{aligned} & \text { oi } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ |
|  | $\begin{aligned} & \text { O} \\ & \text { ie } \\ & \text { ì } \\ & \text { in } \end{aligned}$ |  | $\begin{aligned} & \text { o̊ } \\ & \stackrel{\circ}{\circ} \\ & \text { í } \end{aligned}$ | $\begin{aligned} & \text { 合 } \\ & \stackrel{\rightharpoonup}{9} \end{aligned}$ | $\begin{array}{\|c} \substack{0 \\ \stackrel{i}{e} \\ \underset{\sim}{i}} \end{array}$ | $\begin{gathered} 0 \\ \stackrel{0}{\infty} \\ \infty \\ 0 \end{gathered}$ |  | $\left\|\begin{array}{c} 0 \\ \stackrel{\rightharpoonup}{\infty} \\ \infty \\ 0 \end{array}\right\|$ | $\begin{array}{\|c} \stackrel{0}{0} \\ \stackrel{\sim}{1} \\ \stackrel{1}{0} \end{array}$ | $\begin{aligned} & \text { so } \\ & \stackrel{0}{0} \\ & \stackrel{1}{-} \end{aligned}$ | $\begin{array}{\|c\|} \substack{0 \\ \rightarrow i \\ \infty} \end{array}$ |  | $\begin{array}{\|c} \underset{\sim}{0} \\ \underset{\infty}{-1} \end{array}$ | $\begin{array}{\|c} 00 \\ \stackrel{0}{0} \\ \stackrel{0}{0} \\ \infty \end{array}$ |  | $\left\|\begin{array}{c} 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{array}\right\|$ | $\begin{gathered} \text { ơ } \\ \substack{0 \\ 0} \end{gathered}$ | $\begin{aligned} & \text { è } \\ & \text { ì } \\ & \text { ón } \end{aligned}$ | $\begin{array}{\|l\|} \hline 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{array}$ | $\left\|\begin{array}{c} 0 \\ \stackrel{0}{0} \\ \underset{1}{0} \end{array}\right\|$ | $\begin{aligned} & \text { ob } \\ & \stackrel{\infty}{7} \end{aligned}$ | $\begin{aligned} & 80 \\ & \stackrel{\infty}{7} \\ & \underset{子}{2} \end{aligned}$ | $\stackrel{\text {－}}{\substack{\infty \\-\\ j}}$ |
|  | $\stackrel{\square}{8}$ | － | － | $\stackrel{\text { ® }}{ }$ | $\stackrel{\circ}{\circ}$ | N | $\stackrel{15}{\sim}$ | － | คั | $\stackrel{18}{\text {－}}$ | $\stackrel{\sim}{\sim}$ | 9 | $\stackrel{\sim}{\sim}$ | $\stackrel{\sim}{2}$ | $\stackrel{\text { ค }}{ }$ | $\stackrel{12}{2}$ | $\stackrel{12}{7}$ | $\stackrel{12}{1}$ | 12 | $\stackrel{12}{9}$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
|  | 8 | 8 | 8 | is | 8 | ¢ | B | F | \％ 7 | 가 | ¢ | ¢ | g | q | ¢ | ¢ | $\stackrel{\circ}{8}$ | ¢ | － | ¢ | $\stackrel{1}{2}$ | ค | $\stackrel{\sim}{\sim}$ |
|  |  | $\left\|\begin{array}{c} \underset{8}{8} \\ 0 \\ \end{array}\right\|$ |  | $\begin{gathered} \stackrel{\rightharpoonup}{N} \\ \underset{\sim}{\infty} \end{gathered}$ | $\left\|\begin{array}{l} 8 \\ \hline 8 \\ \vdots \\ 0 \\ 0 \end{array}\right\|$ | $\begin{aligned} & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \stackrel{8}{0} \\ & \stackrel{1}{4} \\ & \underset{子}{2} \end{aligned}$ |  |  | $\stackrel{\substack{\underset{\sim}{\gtrless} \\ \underset{\sim}{2}}}{ }$ | $\begin{aligned} & 20 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \infty \\ & \propto \\ & \infty \\ & \infty \\ & \underset{\sim}{\circ} \end{aligned}$ | $$ | $\left\|\begin{array}{l} 8 \\ \hline 0 \\ \stackrel{0}{6} \\ \rightarrow+ \end{array}\right\|$ | $\begin{aligned} & \ddot{H} \\ & 0 \\ & 6 \\ & - \\ & \hline \end{aligned}$ | $\begin{aligned} & \check{\circ} \\ & \stackrel{\circ}{\circ} \\ & \underset{\sim}{n} \end{aligned}$ | $\begin{aligned} & \hat{0} \\ & \stackrel{0}{0} \\ & = \\ & = \end{aligned}$ |  | $\begin{aligned} & \text { N } \\ & \stackrel{\rightharpoonup}{n} \\ & \stackrel{R}{n} \end{aligned}$ |  | $\begin{aligned} & 8 \\ & \text { 品 } \\ & 0 \end{aligned}$ | $\begin{aligned} & 8 \\ & 0 \\ & 0 \\ & 0 \\ & i \end{aligned}$ | O |
|  |  | $\left\|\begin{array}{c} 0 \\ \hline \\ \vdots \\ \underset{\infty}{\infty} \end{array}\right\|$ | $\begin{aligned} & 0 \\ & 0 \\ & 0 \\ & \text { in } \\ & \infty \end{aligned}$ | $\begin{gathered} 0 \\ 9 \\ 20 \\ 0 \\ 0 \end{gathered}$ | $\begin{gathered} 0 \\ \infty \\ \infty \\ 0 \\ \infty \\ \infty \end{gathered}$ | $\begin{gathered} \stackrel{\circ}{\mathbb{Z}} \\ \underset{\substack{2}}{ } \end{gathered}$ |  | $\left\|\begin{array}{c} 0 \\ 0 \\ 0 \\ 0 \\ 1 \end{array}\right\|$ | $\begin{aligned} & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{gathered} 8 \\ 0 \\ 0 \\ 0 \\ 0 \end{gathered}$ | $\begin{aligned} & \underset{\infty}{\infty} \\ & \infty \\ & \infty \\ & \end{aligned}$ | $\begin{array}{\|c} \underset{\sim}{0} \\ \infty \\ \infty \\ \dot{0} \end{array}$ | $\begin{gathered} \mathscr{O} \\ \mathscr{\infty} \\ \\ \end{gathered}$ | $\left\|\begin{array}{l} 0 \\ 0 \\ 0 \\ i \\ i \end{array}\right\|$ | $\begin{gathered} 9 \\ \stackrel{9}{\infty} \\ \stackrel{1}{\infty} \end{gathered}$ |  |  | $\begin{aligned} & \underset{8}{\otimes} \\ & \underset{\sim}{\circ} \\ & \hline \end{aligned}$ |  | $\left.\begin{gathered} 9 \\ \lambda \\ \infty \\ \underset{i}{2} \end{gathered} \right\rvert\,$ | $\begin{aligned} & 8 \\ & \underset{\infty}{\infty} \\ & \infty \\ & \infty \end{aligned}$ | $\begin{aligned} & \stackrel{8}{\circ} \\ & \underset{\sim}{\circ} \\ & \infty \end{aligned}$ | $\underset{\sim}{\infty} \underset{\sim}{\infty}$ |
| $\cdots$ | $\stackrel{8}{7}$ | $\stackrel{8}{9}$ | $\underset{\substack{8 \\ \hline}}{ }$ | $\underset{1}{8}$ | $\stackrel{\otimes}{7}$ | $\stackrel{8}{7}$ | $\underset{1}{8}$ | $\stackrel{8}{9}$ | $\stackrel{8}{\mathrm{O}}$ | $\underset{\sim}{8}$ | $\underset{\substack{8 \\ \hline}}{ }$ | $\underset{\substack{8 \\ \hline \\ \hline}}{ }$ | $\stackrel{\otimes}{9}$ | $\begin{aligned} & 8 \\ & \vdots \\ & \hline \end{aligned}$ | $\underset{7}{8}$ | $\underset{\substack{8 \\ \hline}}{2}$ | $\stackrel{8}{7}$ | $\underset{\substack{8 \\ \hline}}{ }$ | $\underset{\substack{8 \\ \hline}}{ }$ | $\underset{1}{8}$ | $\underset{7}{8}$ | $\stackrel{8}{4}$ | $\stackrel{8}{1}$ |
|  | 0 | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | － | 0 | 0 | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | 0 | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | 0 |
|  | $\checkmark$ | － | $-$ | $-$ | $\checkmark$ | $\checkmark$ | $\rightarrow$ | $\checkmark$ | $-$ | $\checkmark$ | $\checkmark$ | $-$ | $\rightarrow$ | $\rightarrow$ | $-$ | $\checkmark$ | $\rightarrow$ | $\checkmark$ | $\checkmark$ | $\rightarrow$ | $\checkmark$ | $-$ | $\rightarrow$ |
|  | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | $\sim$ | N | $\sim$ | $\sim$ | $\sim$ | $\sim$ | ก | $\sim$ | $\sim$ |
|  | ¢ | ¢ | ¢ | ¢ | $\stackrel{\circ}{\circ}$ | － | $\stackrel{15}{\text {－}}$ | $\stackrel{1}{\text {－}}$ | เจ | $\stackrel{1}{\text { ® }}$ | $\stackrel{\sim}{\sim}$ | คิ | $\stackrel{\sim}{\circ}$ | $\stackrel{\sim}{2}$ | $\stackrel{\sim}{\sim}$ | 12 | $\stackrel{12}{1}$ | $\stackrel{12}{2}$ | 12 | 19 | $\bigcirc$ | 9 | 9 |
| 荋 | 8 | $\stackrel{8}{4}$ | 8 | $\stackrel{9}{4}$ | $\stackrel{9}{9}$ | $\stackrel{8}{4}$ | $\stackrel{9}{7}$ | $\stackrel{9}{4}$ | 9 | $\stackrel{9}{7}$ | 8 | $\stackrel{8}{7}$ | $\stackrel{9}{7}$ | $\stackrel{9}{4}$ | 9 | $\stackrel{9}{7}$ | 8 | $\stackrel{9}{7}$ | $\stackrel{8}{7}$ | $8$ | 8 | $\stackrel{9}{7}$ | 9 |
| 皆 | $\stackrel{\square}{7}$ | $\stackrel{7}{7}$ | $\stackrel{\infty}{\exists}$ | $\stackrel{g}{\exists}$ | $\stackrel{\text { a }}{ }$ | － | N | $\stackrel{9}{9}$ | － | $\stackrel{1}{9}$ | $\stackrel{\circ}{-1}$ | $\stackrel{\text { N}}{-}$ | $\stackrel{\text { ¢ }}{\sim}$ | $\stackrel{\text { a }}{ }$ | $\stackrel{\sim}{7}$ | $\stackrel{7}{7}$ | $\stackrel{\sim}{\sim}$ | $\stackrel{刃}{\sim}$ | \％ | $\stackrel{\sim}{9}$ | $\stackrel{\circ}{\square}$ | － | $\stackrel{\infty}{\sim}$ |

Table B.1. Computational results of the proposed algorithm. (cont.)

| Iteration \# | Number <br> of <br> Riders | Number <br> of <br> Drivers | Capacity | Rider <br> Count | Number of Riders Rejecting First Match | $\begin{gathered} \text { JSS } \\ \text { Limit } \end{gathered}$ | Computation Time | Average JSS of Matched Pairs | Number <br> of <br> Matched <br> Riders | $\begin{gathered} \text { Number } \\ \text { of } \\ \text { Matched } \\ \text { Drivers } \end{gathered}$ | Ratio of Matched Riders | Ratio of Matched Drivers | Ratio of <br> Riders <br> Accepting <br> First Match | $\begin{gathered} \text { Case } \\ \# \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 139 | 479 | 10 | 2 | 1 | 0 | -100 | 3.8000 | 14.4500 | 20 | 10 | 4.18\% | 100.00\% | 100.00\% | 2 |
| 140 | 479 | 10 | 2 | 1 | 0 | -100 | 3.7270 | 8.1500 | 20 | 10 | 4.18\% | 100.00\% | 100.00\% | 2 |
| 141 | 479 | 5 | 2 | 1 | 0 | -100 | 2.7550 | 5.5000 | 10 | 5 | 2.09\% | 100.00\% | 100.00\% | 2 |
| 142 | 479 | 5 | 2 | 1 | 0 | -100 | 2.8820 | 8.4000 | 10 | 5 | 2.09\% | 100.00\% | 100.00\% | 2 |
| 143 | 479 | 5 | 2 | 1 | 0 | -100 | 2.8460 | -14.1000 | 10 | 5 | 2.09\% | 100.00\% | 100.00\% | 2 |
| 144 | 479 | 5 | 2 | 1 | 0 | -100 | 2.7950 | 21.0000 | 10 | 5 | 2.09\% | 100.00\% | 100.00\% | 2 |
| 145 | 479 | 5 | 2 | 1 | 0 | -100 | 3.0480 | 20.0000 | 10 | 5 | 2.09\% | 100.00\% | 100.00\% | 2 |
| 146 | 479 | 1 | 2 | 1 | 0 | -100 | 2.1790 | 0.0000 | 2 | 1 | 0.42\% | 100.00\% | 100.00\% | 2 |
| 147 | 479 | 1 | 2 | 1 | 0 | -100 | 2.1760 | 3.5000 | 2 | 1 | 0.42\% | 100.00\% | 100.00\% | 2 |
| 148 | 479 | 1 | 2 | 1 | 0 | -100 | 2.1720 | -33.0000 | 2 | 1 | 0.42\% | 100.00\% | 100.00\% | 2 |
| 149 | 479 | 1 | 2 | 1 | 0 | -100 | 2.1730 | 32.5000 | 2 | 1 | 0.42\% | 100.00\% | 100.00\% | 2 |
| 150 | 479 | 1 | 2 | 1 | 0 | -100 | 2.3000 | 2.5000 | 2 | 1 | 0.42\% | 100.00\% | 100.00\% | 2 |
| 151 | 479 | 69 | 1 | 1 | 0 | -100 | 14.7540 | 7.8657 | 67 | 67 | 13.99\% | 97.10\% | 100.00\% | 3 |
| 152 | 479 | 69 | 1 | 1 | 0 | -100 | 14.8700 | 7.8657 | 67 | 67 | 13.99\% | 97.10\% | 100.00\% | 3 |
| 153 | 479 | 69 | 1 | 1 | 0 | -100 | 14.8410 | 7.8657 | 67 | 67 | 13.99\% | 97.10\% | 100.00\% | 3 |
| 154 | 479 | 69 | 1 | 1 | 0 | -100 | 14.9250 | 7.8657 | 67 | 67 | 13.99\% | 97.10\% | 100.00\% | 3 |
| 155 | 479 | 69 | 1 | 1 | 0 | -100 | 14.8820 | 7.8657 | 67 | 67 | 13.99\% | 97.10\% | 100.00\% | 3 |
| 156 | 479 | 65 | 1 | 1 | 0 | -100 | 14.3840 | 8.8571 | 63 | 63 | 13.15\% | 96.92\% | 100.00\% | 3 |
| 157 | 479 | 65 | 1 | 1 | 0 | -100 | 14.0810 | 8.2656 | 64 | 64 | 13.36\% | 98.46\% | 100.00\% | 3 |
| 158 | 479 | 65 | 1 | 1 | 0 | -100 | 15.1190 | 6.8413 | 63 | 63 | 13.15\% | 96.92\% | 100.00\% | 3 |
| 159 | 479 | 65 | 1 | 1 | 0 | -100 | 14.5620 | 9.3016 | 63 | 63 | 13.15\% | 96.92\% | 100.00\% | 3 |
| 160 | 479 | 65 | 1 | 1 | 0 | -100 | 15.3260 | 7.4063 | 64 | 64 | 13.36\% | 98.46\% | 100.00\% | 3 |
| 161 | 479 | 60 | 1 | 1 | 0 | -100 | 13.1430 | 5.6000 | 60 | 60 | 12.53\% | 100.00\% | 100.00\% | 3 |

Table B.1. Computational results of the proposed algorithm. (cont.)

| Iteration \# | Number <br> of <br> Riders | Number of Drivers | Capacity | Rider <br> Count | Number of Riders Rejecting First Match | $\begin{gathered} \text { JSS } \\ \text { Limit } \end{gathered}$ | Computation <br> Time | Average JSS of Matched Pairs | Number <br> of <br> Matched <br> Riders | $\begin{gathered} \text { Number } \\ \text { of } \\ \text { Matched } \\ \text { Drivers } \end{gathered}$ | $\begin{gathered} \text { Ratio } \\ \text { of } \\ \text { Matched } \\ \text { Riders } \end{gathered}$ | Ratio of <br> Matched <br> Drivers | Ratio of <br> Riders <br> Accepting <br> First Match | $\begin{gathered} \text { Case } \\ \# \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 162 | 479 | 60 | 1 | 1 | 0 | -100 | 14.2280 | 6.1667 | 60 | 60 | 12.53\% | 100.00\% | 100.00\% | 3 |
| 163 | 479 | 60 | 1 | 1 | 0 | -100 | 14.9370 | 9.1035 | 58 | 58 | 12.11\% | 96.67\% | 100.00\% | 3 |
| 164 | 479 | 60 | 1 | 1 | 0 | -100 | 14.0400 | 9.3103 | 58 | 58 | 12.11\% | 96.67\% | 100.00\% | 3 |
| 165 | 479 | 60 | 1 | 1 | 0 | -100 | 12.8460 | 7.6949 | 59 | 59 | 12.32\% | 98.33\% | 100.00\% | 3 |
| 166 | 479 | 55 | 1 | 1 | 0 | -100 | 11.8950 | 9.9259 | 54 | 54 | 11.27\% | 98.18\% | 100.00\% | 3 |
| 167 | 479 | 55 | 1 | 1 | 0 | -100 | 11.8120 | 9.0727 | 55 | 55 | 11.48\% | 100.00\% | 100.00\% | 3 |
| 168 | 479 | 55 | 1 | 1 | 0 | -100 | 12.0190 | 7.9245 | 53 | 53 | 11.06\% | 96.36\% | 100.00\% | 3 |
| 169 | 479 | 55 | 1 | 1 | 0 | -100 | 11.8020 | 7.2037 | 54 | 54 | 11.27\% | 98.18\% | 100.00\% | 3 |
| 170 | 479 | 55 | 1 | 1 | 0 | -100 | 11.9720 | 9.6482 | 54 | 54 | 11.27\% | 98.18\% | 100.00\% | 3 |
| 171 | 479 | 50 | 1 | 1 | 0 | -100 | 10.7850 | 7.7400 | 50 | 50 | 10.44\% | 100.00\% | 100.00\% | 3 |
| 172 | 479 | 50 | 1 | 1 | 0 | -100 | 10.9990 | 9.7000 | 50 | 50 | 10.44\% | 100.00\% | 100.00\% | 3 |
| 173 | 479 | 50 | 1 | 1 | 0 | -100 | 10.9100 | 7.1667 | 48 | 48 | 10.02\% | 96.00\% | 100.00\% | 3 |
| 174 | 479 | 50 | 1 | 1 | 0 | -100 | 10.8120 | 4.5800 | 50 | 50 | 10.44\% | 100.00\% | 100.00\% | 3 |
| 175 | 479 | 50 | 1 | 1 | 0 | -100 | 10.7510 | 6.4400 | 50 | 50 | 10.44\% | 100.00\% | 100.00\% | 3 |
| 176 | 479 | 45 | 1 | 1 | 0 | -100 | 9.7880 | 7.3556 | 45 | 45 | 9.39\% | 100.00\% | 100.00\% | 3 |
| 177 | 479 | 45 | 1 | 1 | 0 | -100 | 9.9010 | 7.8000 | 45 | 45 | 9.39\% | 100.00\% | 100.00\% | 3 |
| 178 | 479 | 45 | 1 | 1 | 0 | -100 | 9.9680 | 9.8222 | 45 | 45 | 9.39\% | 100.00\% | 100.00\% | 3 |
| 179 | 479 | 45 | 1 | 1 | 0 | -100 | 9.7030 | 6.8000 | 45 | 45 | 9.39\% | 100.00\% | 100.00\% | 3 |
| 180 | 479 | 45 | 1 | 1 | 0 | -100 | 9.8160 | 8.1778 | 45 | 45 | 9.39\% | 100.00\% | 100.00\% | 3 |
| 181 | 479 | 40 | 1 | 1 | 0 | -100 | 9.0110 | 6.0513 | 39 | 39 | 8.14\% | 97.50\% | 100.00\% | 3 |
| 182 | 479 | 40 | 1 | 1 | 0 | -100 | 8.8420 | 6.2750 | 40 | 40 | 8.35\% | 100.00\% | 100.00\% | 3 |
| 183 | 479 | 40 | 1 | 1 | 0 | -100 | 8.8440 | 9.8000 | 40 | 40 | 8.35\% | 100.00\% | 100.00\% | 3 |
| 184 | 479 | 40 | 1 | 1 | 0 | -100 | 8.9490 | 3.6000 | 40 | 40 | 8.35\% | 100.00\% | 100.00\% | 3 |

Table B．1．Computational results of the proposed algorithm．（cont．）

| U | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & \text { 合 } \\ & 0 \\ & \dot{0} \\ & \hline 0 \end{aligned}$ | $\begin{aligned} & 00 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & 00 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { of } \\ & 0 . \\ & 0 . \\ & 0 . \end{aligned}$ | $\left\|\begin{array}{l} 00 \\ 0 \\ 0 \\ 0 \\ 0 \end{array}\right\|$ | $\begin{aligned} & \text { oo } \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { 合 } \\ & 0 \\ & \dot{0} \\ & \hline 0 \end{aligned}$ | $\begin{aligned} & 00 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { so } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { of } \\ & 0 . \\ & 0 . \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { ô } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { of } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { 合 } \\ & 0 \\ & \dot{0} \\ & \hline 0 \end{aligned}$ |  | $\begin{array}{\|c} 00 \\ 0 . \\ 0 . \\ 0.0 \end{array}$ | $\begin{aligned} & \text { so } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { oi } \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { ồ } \\ & \stackrel{0}{0} \\ & 0 \end{aligned}$ | $\begin{aligned} & 0.0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { so } \\ & \text { ob } \\ & \stackrel{0}{0} \end{aligned}$ | $\begin{aligned} & \text { ob } \\ & \text { ob } \\ & \text { B. } \end{aligned}$ | $\begin{aligned} & \text { ô } \\ & \text { O. } \\ & \text { O} \end{aligned}$ | 80 O－ O－ |
|  | $\begin{aligned} & \text { oi } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\left.\begin{aligned} & 00 \\ & 0 \\ & 0 \\ & 0 \\ & \vdots \end{aligned} \right\rvert\,$ | $\begin{aligned} & \text { ol } \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { ol } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\left.\begin{aligned} & 00 \\ & 0 \\ & 0 \\ & 0 \\ & \vdots \end{aligned} \right\rvert\,$ |  | $\begin{aligned} & \text { oi } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\left.\begin{aligned} & 00 \\ & 0 \\ & 0 \\ & 0 \\ & \vdots \end{aligned} \right\rvert\,$ | $\begin{aligned} & 80 \\ & 8 . \\ & 0 . \\ & 0 . \end{aligned}$ | $\begin{aligned} & \text { ol } \\ & 0 \\ & 0 \\ & 0 \\ & \hline-1 \end{aligned}$ | $\begin{aligned} & \text { ol } \\ & 0 \\ & 0 \\ & 0 \\ & \hline-1 \end{aligned}$ | $\begin{aligned} & 00 \\ & 0 . \\ & 0 . \\ & 0 . \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { oi } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { ô } \\ & \stackrel{0}{\dot{\circ}} \\ & \text { O} \end{aligned}$ | $\begin{aligned} & \text { so } \\ & 0 \\ & 0 . \\ & 0 . \\ & \hline \end{aligned}$ | $\begin{aligned} & 00 \\ & 0 \\ & 0 \\ & \vdots \\ & \vdots \end{aligned}$ | $\begin{aligned} & 80 \\ & 8 \\ & 0 . \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { ô } \\ & \stackrel{0}{0} \\ & \stackrel{i}{9} \end{aligned}$ | $\begin{aligned} & \text { ol } \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & 00 \\ & 0 \\ & 0 \\ & 0 \\ & \vdots \end{aligned}$ | $\begin{aligned} & \text { ô } \\ & \text { O. } \\ & \text { O} \end{aligned}$ | $\begin{aligned} & \text { ồ } \\ & \text { ob } \\ & \text { in } \end{aligned}$ | $\begin{aligned} & \text { ol } \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ |
|  | $\begin{aligned} & \text { 合 } \\ & \stackrel{0}{\infty} \\ & \infty \end{aligned}$ | $\begin{array}{\|c} \substack{0 \\ \underset{\sim}{n} \\ \stackrel{1}{2}} \end{array}$ | $\begin{gathered} \stackrel{0}{2} \\ \stackrel{\rightharpoonup}{p} \\ \stackrel{n}{2} \end{gathered}$ | $\begin{aligned} & \stackrel{0}{\mathrm{O}} \\ & \stackrel{y}{n} \end{aligned}$ |  | $\begin{aligned} & \stackrel{\circ}{0} \\ & \stackrel{\sim}{0} \end{aligned}$ | $\begin{aligned} & \text { O} \\ & \stackrel{0}{0} \\ & \text { ín } \end{aligned}$ | $\left\|\begin{array}{c} 0 \\ \stackrel{0}{0} \\ \underset{c}{0} \end{array}\right\|$ | $\begin{gathered} 0 \\ \substack{0 \\ \\ 0} \end{gathered}$ | $\begin{array}{\|c} 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{array}$ | $\begin{aligned} & \text { ơ } \\ & \stackrel{0}{\mathrm{O}} \\ & \mathrm{o} \end{aligned}$ | $\begin{aligned} & \text { 令 } \\ & \text { Nָ } \\ & \text { in } \end{aligned}$ | $\begin{array}{\|c} \substack{\text { No } \\ \text { Ni } \\ \text { in }} \end{array}$ |  | $\begin{array}{\|c} \substack{\text { No } \\ \text { Ǹ } \\ \text { in }} \end{array}$ | $\begin{gathered} \text { ờ } \\ \text { Nu } \\ \text { in } \end{gathered}$ | $\begin{gathered} \infty \\ \stackrel{\infty}{\infty} \\ \underset{f}{7} \end{gathered}$ | $\begin{gathered} 0_{0}^{0} \\ \substack{\infty \\ 7 \\ \hline} \end{gathered}$ | $\begin{gathered} 0 \\ \infty \\ \substack{\infty \\ f \\ 子} \end{gathered}$ | $\begin{gathered} \circ 0 \\ \substack{\infty \\ \underset{子}{\prime}} \end{gathered}$ | $\begin{aligned} & \text { ob } \\ & \stackrel{\infty}{7} \end{aligned}$ | $\begin{aligned} & \stackrel{0}{0} \\ & \stackrel{0}{9} \\ & \infty \end{aligned}$ |  |
|  | 9 | 18 | $\stackrel{1}{8}$ | 19 | $\stackrel{1}{\circ}$ | 18 | － | － | $\stackrel{\circ}{\circ}$ | － | $\stackrel{\sim}{\circ}$ | $\stackrel{18}{\text {－}}$ | $\stackrel{19}{\sim}$ | เค | $\stackrel{19}{\sim}$ | $\stackrel{18}{\text {－}}$ | $\stackrel{\sim}{\sim}$ | $\stackrel{\text { ® }}{ }$ | $\stackrel{\sim}{\sim}$ | $\stackrel{\text { คे }}{ }$ | $\stackrel{\text {－}}{\sim}$ | 12 | $\stackrel{12}{1}$ |
|  | \％ | \％ | $\stackrel{1}{8}$ | $\stackrel{1}{8}$ | $\stackrel{1}{6}$ | $\stackrel{8}{8}$ | ¢ | － | ¢ | ¢ | ¢ | $\stackrel{18}{\text {－}}$ | $\stackrel{1}{\sim}$ | เค | － | － | $\stackrel{\square}{-}$ | $\stackrel{\sim}{\sim}$ | － | － | $\stackrel{1}{2}$ | 12 | $\stackrel{12}{1}$ |
|  | $\begin{aligned} & \underset{8}{8} \\ & \underset{\sim}{1} \\ & 1 \end{aligned}$ | $\left\lvert\, \begin{gathered} \underset{\sim}{9} \\ \underset{\sim}{1} \\ \underset{\sim}{2} \end{gathered}\right.$ | $\left\lvert\, \begin{gathered} \underset{N}{\underset{N}{N}} \underset{\substack{2}}{ } \end{gathered}\right.$ | $\begin{aligned} & \text { F } \\ & 0 \\ & 0 \\ & 1 . \end{aligned}$ | $\begin{array}{\|c\|c} 1 \\ \hline \\ \vdots \\ \vdots \\ 1 \end{array}$ | $\left\|\begin{array}{l} 8 \\ 0 \\ \vdots \\ 0 \\ 0 \end{array}\right\|$ |  | $\left\lvert\, \begin{gathered} \substack{8 \\ 0 \\ \\ 0} \end{gathered}\right.$ | $\begin{aligned} & 8 \\ & \hline 8 \\ & 0 \\ & \infty \\ & \infty \end{aligned}$ | $\begin{aligned} & 8 \\ & \hline \mathbf{6} \\ & \hline \end{aligned}$ | $\stackrel{\text { ® }}{\substack{\infty}}$ | $\left\lvert\, \begin{aligned} & 8 \\ & \hline 0 \\ & 0 \\ & 0 \\ & \infty \end{aligned}\right.$ | $\begin{aligned} & \mathrm{O} \\ & \stackrel{\mathrm{~N}}{1} \\ & \mathrm{~N} \end{aligned}$ | $\begin{gathered} 8 \\ \underset{1}{8} \\ \hline 1 \end{gathered}$ | $\begin{aligned} & \stackrel{O}{0} \\ & \stackrel{0}{0} \\ & - \end{aligned}$ | $\begin{gathered} 8 \\ \hline \end{gathered}$ | $\begin{aligned} & 8 \\ & \stackrel{8}{0} \\ & \underset{子}{2} \end{aligned}$ | $\begin{aligned} & 8 \\ & \stackrel{0}{\infty} \\ & \stackrel{\infty}{\circ} \end{aligned}$ | $\begin{aligned} & \underset{8}{8} \\ & \underset{\sim}{8} \\ & \infty \end{aligned}$ | $\begin{aligned} & 8 \\ & i \\ & \infty \\ & \infty \\ & 0 \end{aligned}$ | $\begin{aligned} & 8 \\ & \stackrel{8}{8} \\ & \stackrel{\circ}{8} \end{aligned}$ | $\begin{aligned} & \text { O} \\ & \text { O} \\ & \dot{-} \end{aligned}$ | ¢ |
|  | $\begin{aligned} & 8 \\ & \hline 8 \\ & 0 . \\ & 0 \\ & \infty \\ & \infty \end{aligned}$ | $\left\|\begin{array}{c} 0 \\ \stackrel{0}{1} \\ 1 \\ 1 \end{array}\right\|$ | $\begin{gathered} \underset{\sim}{\underset{y}{c}} \\ \underset{\sim}{\infty} \end{gathered}$ | $\begin{gathered} \underset{+}{\underset{y}{c}} \\ \underset{\sim}{\infty} \end{gathered}$ | $\begin{aligned} & \underset{\sim}{8} \\ & \underset{\sim}{6} \\ & 1 \end{aligned}$ | $\begin{array}{\|c} \stackrel{\circ}{4} \\ \underset{\sim}{4} \end{array}$ | $\begin{aligned} & \text { O} \\ & \hline 0 \\ & \hline \\ & 1 \end{aligned}$ | $\left\|\begin{array}{c} 9 \\ \infty \\ \infty \\ \infty \\ 0 \end{array}\right\|$ | $\left\|\begin{array}{c} 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{array}\right\|$ | $\underset{\substack{P \\ \infty \\ \infty \\ \dot{O}}}{ }$ | $\begin{gathered} \mathrm{P} \\ \stackrel{0}{\mathrm{O}} \\ \mathrm{~N} \end{gathered}$ | $\begin{aligned} & \stackrel{8}{\mathrm{M}} \\ & \underset{\substack{2}}{ } \end{aligned}$ | $\begin{gathered} \stackrel{\rightharpoonup}{0} \\ \stackrel{C}{6} \\ \hline \end{gathered}$ | $\left\|\begin{array}{c} 0 \\ 0 \\ 0 \\ 0 \end{array}\right\|$ | $\left\lvert\, \begin{gathered} \substack{\infty \\ \infty \\ \infty \\ \infty \\ \dot{L} \\ \hline} \end{gathered}\right.$ | $\left\|\begin{array}{c} o \\ \underset{\infty}{\infty} \\ 10 \end{array}\right\|$ | $\begin{aligned} & 0 \\ & \stackrel{0}{10} \\ & \stackrel{10}{10} \end{aligned}$ | $\begin{gathered} \stackrel{\circ}{\circ} \\ \stackrel{\oplus}{\circ} \end{gathered}$ | $\left\lvert\, \begin{gathered} 9 \\ \underset{4}{1} \\ \underset{0}{2} \end{gathered}\right.$ | $\left\|\begin{array}{c} 9 \\ \hline 6 \\ \hdashline 1 \\ i 0 \end{array}\right\|$ | $\begin{aligned} & \stackrel{P}{9} \\ & \stackrel{0}{7} \end{aligned}$ | $\begin{gathered} 0 \\ \underset{0}{0} \\ \underset{\sim}{2} \end{gathered}$ | $\xrightarrow{\circ}$ |
| $\cdots$ | $\stackrel{8}{7}$ | $\stackrel{8}{9}$ | $\underset{\substack{8 \\ \hline}}{ }$ | $\underset{1}{8}$ | $\stackrel{\otimes}{7}$ | $\stackrel{8}{7}$ | $\underset{1}{8}$ | $\stackrel{8}{9}$ | $\stackrel{8}{7}$ | $\underset{\sim}{8}$ | $\stackrel{8}{7}$ | $\underset{\underset{1}{\circ}}{8}$ | $\stackrel{\otimes}{9}$ | $\stackrel{\underset{1}{7}}{8}$ | $\underset{7}{8}$ | $\underset{\substack{8 \\ \hline}}{2}$ | $\stackrel{8}{7}$ | $\stackrel{\otimes}{1}$ | $\begin{array}{\|c} 8 \\ 1 \end{array}$ | $\underset{1}{8}$ | $\underset{7}{8}$ | $\underset{\substack{8 \\ \hline}}{ }$ | $\stackrel{8}{1}$ |
|  | 0 | － | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | － | 0 | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | 0 | $\bigcirc$ | $\bigcirc$ | － | $\bigcirc$ | $\bigcirc$ | 0 | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
|  | $\rightarrow$ | $\checkmark$ | $-$ | $-$ | $\checkmark$ | $\checkmark$ | $\rightarrow$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\rightarrow$ | $-$ | $\rightarrow$ | $\checkmark$ | $\checkmark$ | $-$ | $\rightarrow$ | $\rightarrow$ | $\checkmark$ | $-$ | － |
| $\begin{aligned} & \text { 訁े } \\ & \text { たた } \\ & \text { だ } \end{aligned}$ | $\rightarrow$ | $\rightarrow$ | $-$ | $\rightarrow$ | $\rightarrow$ | － | － | $\rightarrow$ | $\rightarrow$ | － | $\rightarrow$ | $\rightarrow$ | － | $-$ | － | － | $\rightarrow$ | $-$ | $-$ | $-$ | $-$ | $-$ | $-$ |
|  | q | $\stackrel{8}{8}$ | 낭 | $\stackrel{1}{8}$ | $\stackrel{18}{\circ}$ | $\stackrel{1}{8}$ | ¢ | － | ¢ | ¢ | ¢ | $\stackrel{18}{\text {－}}$ | $\stackrel{1}{\text {－}}$ | $\stackrel{18}{\text { ¢ }}$ | － | $\stackrel{1}{\text { ® }}$ | $\stackrel{\sim}{\sim}$ | 간 | $\stackrel{\sim}{\sim}$ | ลิ | － | 12 | $\stackrel{12}{9}$ |
|  | 8 | $\stackrel{8}{4}$ | $\stackrel{8}{4}$ | $\stackrel{9}{4}$ | $\stackrel{9}{9}$ | $\stackrel{8}{4}$ | $\stackrel{9}{7}$ | $\stackrel{9}{4}$ | 8 | $\stackrel{9}{7}$ | 8 | $\stackrel{9}{7}$ | $\stackrel{9}{4}$ | $\stackrel{9}{4}$ | $\stackrel{9}{9}$ | $\stackrel{9}{7}$ | 8 | 8 | 8 | $\stackrel{8}{4}$ | 8 | $\stackrel{8}{4}$ | $\stackrel{9}{7}$ |
| 皆 | $\stackrel{10}{\sim}$ | $\stackrel{\otimes}{\sim}$ | $\stackrel{\sim}{\sim}$ | $\stackrel{\infty}{\infty}$ | $\stackrel{\otimes}{\sim}$ | $\stackrel{\circ}{1}$ | $\stackrel{\rightharpoonup}{9}$ | － | $\stackrel{\%}{\circ}$ | － | $\stackrel{2}{9}$ | $\stackrel{\circ}{9}$ | $\stackrel{\text { ® }}{\text {－}}$ | $\stackrel{\infty}{9}$ | $\stackrel{8}{9}$ | $\stackrel{\circ}{\text { ¢ }}$ | $\stackrel{\rightharpoonup}{\sim}$ | $\stackrel{\mathrm{N}}{\mathrm{~N}}$ | \％ | － | － | － | － |

Table B.1. Computational results of the proposed algorithm. (cont.)

| Iteration \# | Number <br> of <br> Riders | Number of Drivers | Capacity | Rider <br> Count | Number of Riders Rejecting First Match | $\begin{gathered} \text { JSS } \\ \text { Limit } \end{gathered}$ | Computation <br> Time | Average JSS of Matched Pairs | Number <br> of <br> Matched <br> Riders | $\begin{gathered} \text { Number } \\ \text { of } \\ \text { Matched } \\ \text { Drivers } \end{gathered}$ | $\begin{gathered} \text { Ratio } \\ \text { of } \\ \text { Matched } \\ \text { Riders } \end{gathered}$ | Ratio of <br> Matched <br> Drivers | Ratio of <br> Riders <br> Accepting <br> First Match | $\begin{gathered} \text { Case } \\ \# \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 208 | 479 | 15 | 1 | 1 | 0 | -100 | 4.2790 | 10.6000 | 15 | 15 | 3.13\% | 100.00\% | 100.00\% | 3 |
| 209 | 479 | 15 | 1 | 1 | 0 | -100 | 4.2470 | 6.4000 | 15 | 15 | 3.13\% | 100.00\% | 100.00\% | 3 |
| 210 | 479 | 15 | 1 | 1 | 0 | -100 | 4.4540 | 1.0667 | 15 | 15 | 3.13\% | 100.00\% | 100.00\% | 3 |
| 211 | 479 | 10 | 1 | 1 | 0 | -100 | 3.5130 | 7.2000 | 10 | 10 | 2.09\% | 100.00\% | 100.00\% | 3 |
| 212 | 479 | 10 | 1 | 1 | 0 | -100 | 3.5640 | 5.6000 | 10 | 10 | 2.09\% | 100.00\% | 100.00\% | 3 |
| 213 | 479 | 10 | 1 | 1 | 0 | -100 | 3.4910 | 12.2000 | 10 | 10 | 2.09\% | 100.00\% | 100.00\% | 3 |
| 214 | 479 | 10 | 1 | 1 | 0 | -100 | 3.4870 | 9.5000 | 10 | 10 | 2.09\% | 100.00\% | 100.00\% | 3 |
| 215 | 479 | 10 | 1 | 1 | 0 | -100 | 3.4970 | 11.1000 | 10 | 10 | 2.09\% | 100.00\% | 100.00\% | 3 |
| 216 | 479 | 5 | 1 | 1 | 0 | -100 | 2.9330 | 17.4000 | 5 | 5 | 1.04\% | 100.00\% | 100.00\% | 3 |
| 217 | 479 | 5 | 1 | 1 | 0 | -100 | 2.8360 | 18.8000 | 5 | 5 | 1.04\% | 100.00\% | 100.00\% | 3 |
| 218 | 479 | 5 | 1 | 1 | 0 | -100 | 2.7010 | -1.6000 | 5 | 5 | 1.04\% | 100.00\% | 100.00\% | 3 |
| 219 | 479 | 5 | 1 | 1 | 0 | -100 | 2.7020 | 0.2000 | 5 | 5 | 1.04\% | 100.00\% | 100.00\% | 3 |
| 220 | 479 | 5 | 1 | 1 | 0 | -100 | 2.7820 | 4.6000 | 5 | 5 | 1.04\% | 100.00\% | 100.00\% | 3 |
| 221 | 479 | 1 | 1 | 1 | 0 | -100 | 2.1690 | 10.0000 | 1 | 1 | 0.21\% | 100.00\% | 100.00\% | 3 |
| 222 | 479 | 1 | 1 | 1 | 0 | -100 | 2.1700 | 0.0000 | 1 | 1 | 0.21\% | 100.00\% | 100.00\% | 3 |
| 223 | 479 | 1 | 1 | 1 | 0 | -100 | 2.4050 | 10.0000 | 1 | 1 | 0.21\% | 100.00\% | 100.00\% | 3 |
| 224 | 479 | 1 | 1 | 1 | 0 | -100 | 2.5580 | 30.0000 | 1 | 1 | 0.21\% | 100.00\% | 100.00\% | 3 |
| 225 | 479 | 1 | 1 | 1 | 0 | -100 | 2.1660 | 2.0000 | 1 | 1 | 0.21\% | 100.00\% | 100.00\% | 3 |
| 226 | 450 | 69 | 3 | 1 | 0 | -100 | 21.9600 | 8.2670 | 191 | 64 | 42.44\% | 92.75\% | 100.00\% | 4 |
| 227 | 450 | 69 | 3 | 1 | 0 | -100 | 21.9920 | 8.0209 | 191 | 64 | 42.44\% | 92.75\% | 100.00\% | 4 |
| 228 | 450 | 69 | 3 | 1 | 0 | -100 | 21.9510 | 9.0262 | 191 | 64 | 42.44\% | 92.75\% | 100.00\% | 4 |
| 229 | 450 | 69 | 3 | 1 | 0 | -100 | 21.8250 | 8.8011 | 191 | 64 | 42.44\% | 92.75\% | 100.00\% | 4 |
| 230 | 450 | 69 | 3 | 1 | 0 | -100 | 21.7760 | 8.2827 | 191 | 64 | 42.44\% | 92.75\% | 100.00\% | 4 |

Table B.1. Computational results of the proposed algorithm. (cont.)

| Iteration \# | Number <br> of <br> Riders | Number of Drivers | Capacity | Rider <br> Count | Number of Riders Rejecting First Match | $\begin{gathered} \text { JSS } \\ \text { Limit } \end{gathered}$ | Computation Time | Average JSS of Matched Pairs | Number <br> of <br> Matched <br> Riders | $\begin{gathered} \text { Number } \\ \text { of } \\ \text { Matched } \\ \text { Drivers } \end{gathered}$ | $\begin{gathered} \text { Ratio } \\ \text { of } \\ \text { Matched } \\ \text { Riders } \end{gathered}$ | Ratio of <br> Matched <br> Drivers | Ratio of <br> Riders <br> Accepting <br> First Match | $\begin{gathered} \text { Case } \\ \# \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 231 | 400 | 69 | 3 | 1 | 0 | -100 | 20.8280 | 9.1474 | 190 | 64 | 47.50\% | 92.75\% | 100.00\% | 4 |
| 232 | 400 | 69 | 3 | 1 | 0 | -100 | 21.0580 | 7.7790 | 190 | 64 | 47.50\% | 92.75\% | 100.00\% | 4 |
| 233 | 400 | 69 | 3 | 1 | 0 | -100 | 20.9480 | 9.3895 | 190 | 64 | 47.50\% | 92.75\% | 100.00\% | 4 |
| 234 | 400 | 69 | 3 | 1 | 0 | -100 | 20.3260 | 8.6421 | 190 | 64 | 47.50\% | 92.75\% | 100.00\% | 4 |
| 235 | 400 | 69 | 3 | 1 | 0 | -100 | 20.7900 | 9.5079 | 189 | 64 | 47.25\% | 92.75\% | 100.00\% | 4 |
| 236 | 350 | 69 | 3 | 1 | 0 | -100 | 19.3230 | 8.5479 | 188 | 64 | 53.71\% | 92.75\% | 100.00\% | 4 |
| 237 | 350 | 69 | 3 | 1 | 0 | -100 | 19.3730 | 8.6667 | 189 | 64 | 54.00\% | 92.75\% | 100.00\% | 4 |
| 238 | 350 | 69 | 3 | 1 | 0 | -100 | 19.3430 | 9.0267 | 187 | 63 | 53.43\% | 91.30\% | 100.00\% | 4 |
| 239 | 350 | 69 | 3 | 1 | 0 | -100 | 19.0010 | 8.1543 | 188 | 64 | 53.71\% | 92.75\% | 100.00\% | 4 |
| 240 | 350 | 69 | 3 | 1 | 0 | -100 | 19.5660 | 8.1170 | 188 | 64 | 53.71\% | 92.75\% | 100.00\% | 4 |
| 241 | 300 | 69 | 3 | 1 | 0 | -100 | 18.0780 | 9.1405 | 185 | 63 | 61.67\% | 91.30\% | 100.00\% | 4 |
| 242 | 300 | 69 | 3 | 1 | 0 | -100 | 18.5720 | 10.2120 | 184 | 63 | 61.33\% | 91.30\% | 100.00\% | 4 |
| 243 | 300 | 69 | 3 | 1 | 0 | -100 | 18.2050 | 9.7796 | 186 | 63 | 62.00\% | 91.30\% | 100.00\% | 4 |
| 244 | 300 | 69 | 3 | 1 | 0 | -100 | 18.2150 | 9.2842 | 183 | 63 | 61.00\% | 91.30\% | 100.00\% | 4 |
| 245 | 300 | 69 | 3 | 1 | 0 | -100 | 18.3500 | 9.1862 | 188 | 63 | 62.67\% | 91.30\% | 100.00\% | 4 |
| 246 | 250 | 69 | 3 | 1 | 0 | -100 | 17.2790 | 11.8802 | 167 | 58 | 66.80\% | 84.06\% | 100.00\% | 4 |
| 247 | 250 | 69 | 3 | 1 | 0 | -100 | 17.0290 | 11.2429 | 177 | 62 | 70.80\% | 89.86\% | 100.00\% | 4 |
| 248 | 250 | 69 | 3 | 1 | 0 | -100 | 16.8360 | 11.2428 | 173 | 60 | 69.20\% | 86.96\% | 100.00\% | 4 |
| 249 | 250 | 69 | 3 | 1 | 0 | -100 | 16.5130 | 10.0824 | 170 | 59 | 68.00\% | 85.51\% | 100.00\% | 4 |
| 250 | 250 | 69 | 3 | 1 | 0 | -100 | 16.9530 | 10.8187 | 171 | 61 | 68.40\% | 88.41\% | 100.00\% | 4 |
| 251 | 200 | 69 | 3 | 1 | 0 | -100 | 14.4100 | 10.9932 | 147 | 53 | 73.50\% | 76.81\% | 100.00\% | 4 |
| 252 | 200 | 69 | 3 | 1 | 0 | -100 | 15.1930 | 11.2089 | 158 | 56 | 79.00\% | 81.16\% | 100.00\% | 4 |
| 253 | 200 | 69 | 3 | 1 | 0 | -100 | 14.4040 | 13.3862 | 145 | 53 | 72.50\% | 76.81\% | 100.00\% | 4 |

Table B.1. Computational results of the proposed algorithm. (cont.)

| Iteration \# |  |  | Capacity | Rider <br> Count | Number <br> of Riders <br> Rejecting <br> First Match | $\begin{gathered} \text { JSS } \\ \text { Limit } \end{gathered}$ | Computation Time | Average JSS of Matched Pairs | Number <br> of <br> Matched <br> Riders | Number <br> of <br> Matched <br> Drivers | ```Ratio of Matched Riders``` | $\begin{gathered} \text { Ratio } \\ \text { of } \\ \text { Matched } \\ \text { Drivers } \end{gathered}$ | Ratio of <br> Riders <br> Accepting <br> First Match | $\begin{gathered} \text { Case } \\ \# \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 254 | 200 | 69 | 3 | 1 | 0 | -100 | 14.4330 | 11.4713 | 157 | 57 | 78.50\% | 82.61\% | 100.00\% | 4 |
| 255 | 200 | 69 | 3 | 1 | 0 | -100 | 14.5010 | 12.3113 | 151 | 53 | 75.50\% | 76.81\% | 100.00\% | 4 |
| 256 | 150 | 69 | 3 | 1 | 0 | -100 | 11.0490 | 14.0840 | 131 | 49 | 87.33\% | 71.01\% | 100.00\% | 4 |
| 257 | 150 | 69 | 3 | 1 | 0 | -100 | 11.5460 | 11.3566 | 129 | 50 | 86.00\% | 72.46\% | 100.00\% | 4 |
| 258 | 150 | 69 | 3 | 1 | 0 | -100 | 11.5550 | 11.9225 | 129 | 50 | 86.00\% | 72.46\% | 100.00\% | 4 |
| 259 | 150 | 69 | 3 | 1 | 0 | -100 | 11.6560 | 13.8240 | 125 | 47 | 83.33\% | 68.12\% | 100.00\% | 4 |
| 260 | 150 | 69 | 3 | 1 | 0 | -100 | 11.6080 | 12.1860 | 129 | 47 | 86.00\% | 68.12\% | 100.00\% | 4 |
| 261 | 100 | 69 | 3 | 1 | 0 | -100 | 9.1530 | 13.3478 | 92 | 38 | 92.00\% | 55.07\% | 100.00\% | 4 |
| 262 | 100 | 69 | 3 | 1 | 0 | -100 | 8.3800 | 12.9158 | 95 | 41 | 95.00\% | 59.42\% | 100.00\% | 4 |
| 263 | 100 | 69 | 3 | 1 | 0 | -100 | 10.7130 | 15.0000 | 91 | 39 | 91.00\% | 56.52\% | 100.00\% | 4 |
| 264 | 100 | 69 | 3 | 1 | 0 | -100 | 9.2490 | 16.0851 | 94 | 38 | 94.00\% | 55.07\% | 100.00\% | 4 |
| 265 | 100 | 69 | 3 | 1 | 0 | -100 | 8.7390 | 15.6250 | 96 | 39 | 96.00\% | 56.52\% | 100.00\% | 4 |
| 266 | 50 | 69 | 3 | 1 | 0 | -100 | 4.4130 | 20.6122 | 49 | 21 | 98.00\% | 30.43\% | 100.00\% | 4 |
| 267 | 50 | 69 | 3 | 1 | 0 | -100 | 4.7740 | 15.7400 | 50 | 23 | 100.00\% | 33.33\% | 100.00\% | 4 |
| 268 | 50 | 69 | 3 | 1 | 0 | -100 | 4.1040 | 13.4444 | 45 | 20 | 90.00\% | 28.99\% | 100.00\% | 4 |
| 269 | 50 | 69 | 3 | 1 | 0 | -100 | 4.6920 | 22.8542 | 48 | 22 | 96.00\% | 31.88\% | 100.00\% | 4 |
| 270 | 50 | 69 | 3 | 1 | 0 | -100 | 4.9860 | 17.8571 | 49 | 22 | 98.00\% | 31.88\% | 100.00\% | 4 |
| 271 | 1 | 69 | 3 | 1 | 0 | -100 | 0.0850 | 30.0000 | 1 | 1 | 100.00\% | 1.45\% | 100.00\% | 4 |
| 272 | 1 | 69 | 3 | 1 | 0 | -100 | 0.1690 | 45.0000 | 1 | 1 | 100.00\% | 1.45\% | 100.00\% | 4 |
| 273 | 1 | 69 | 3 | 1 | 0 | -100 | 0.1890 | 65.0000 | 1 | 1 | 100.00\% | 1.45\% | 100.00\% | 4 |
| 274 | 1 | 69 | 3 | 1 | 0 | -100 | 0.0680 | 21.0000 | 1 | 1 | 100.00\% | 1.45\% | 100.00\% | 4 |
| 275 | 1 | 69 | 3 | 1 | 0 | -100 | 0.0880 | 0.0000 | 1 | 1 | 100.00\% | 1.45\% | 100.00\% | 4 |
| 276 | 450 | 69 | 2 | 1 | 0 | -100 | 17.7350 | 8.5078 | 128 | 64 | 28.44\% | 92.75\% | 100.00\% | 5 |

Table B.1. Computational results of the proposed algorithm. (cont.)

| $\begin{gathered} \text { Iteration } \\ \quad \# \end{gathered}$ | Number <br> of <br> Riders | Number of Drivers | Capacity | Rider <br> Count | Number of Riders Rejecting First Match | $\begin{gathered} \text { JSS } \\ \text { Limit } \end{gathered}$ | Computation <br> Time | Average JSS of Matched Pairs | Number <br> of <br> Matched <br> Riders | $\begin{gathered} \text { Number } \\ \text { of } \\ \text { Matched } \\ \text { Drivers } \end{gathered}$ | $\begin{gathered} \text { Ratio } \\ \text { of } \\ \text { Matched } \\ \text { Riders } \end{gathered}$ | Ratio of <br> Matched <br> Drivers | Ratio of <br> Riders <br> Accepting <br> First Match | $\begin{gathered} \text { Case } \\ \# \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 277 | 450 | 69 | 2 | 1 | 0 | -100 | 17.3830 | 7.9147 | 129 | 65 | 28.67\% | 94.20\% | 100.00\% | 5 |
| 278 | 450 | 69 | 2 | 1 | 0 | -100 | 17.1780 | 7.6094 | 128 | 65 | 28.44\% | 94.20\% | 100.00\% | 5 |
| 279 | 450 | 69 | 2 | 1 | 0 | -100 | 17.2770 | 8.1563 | 128 | 65 | 28.44\% | 94.20\% | 100.00\% | 5 |
| 280 | 450 | 69 | 2 | 1 | 0 | -100 | 17.1420 | 8.4961 | 129 | 65 | 28.67\% | 94.20\% | 100.00\% | 5 |
| 281 | 400 | 69 | 2 | 1 | 0 | -100 | 16.3300 | 8.8217 | 129 | 65 | 32.25\% | 94.20\% | 100.00\% | 5 |
| 282 | 400 | 69 | 2 | 1 | 0 | -100 | 15.9190 | 8.4341 | 129 | 65 | 32.25\% | 94.20\% | 100.00\% | 5 |
| 283 | 400 | 69 | 2 | 1 | 0 | -100 | 16.2130 | 8.8062 | 129 | 65 | 32.25\% | 94.20\% | 100.00\% | 5 |
| 284 | 400 | 69 | 2 | 1 | 0 | -100 | 16.1450 | 8.9531 | 128 | 64 | 32.00\% | 92.75\% | 100.00\% | 5 |
| 285 | 400 | 69 | 2 | 1 | 0 | -100 | 16.6190 | 8.4109 | 129 | 65 | 32.25\% | 94.20\% | 100.00\% | 5 |
| 286 | 350 | 69 | 2 | 1 | 0 | -100 | 15.1680 | 7.6328 | 128 | 65 | 36.57\% | 94.20\% | 100.00\% | 5 |
| 287 | 350 | 69 | 2 | 1 | 0 | -100 | 15.7430 | 8.7266 | 128 | 65 | 36.57\% | 94.20\% | 100.00\% | 5 |
| 288 | 350 | 69 | 2 | 1 | 0 | -100 | 15.7300 | 8.3047 | 128 | 65 | 36.57\% | 94.20\% | 100.00\% | 5 |
| 289 | 350 | 69 | 2 | 1 | 0 | -100 | 15.3910 | 8.3594 | 128 | 64 | 36.57\% | 92.75\% | 100.00\% | 5 |
| 290 | 350 | 69 | 2 | 1 | 0 | -100 | 15.8440 | 7.7222 | 126 | 64 | 36.00\% | 92.75\% | 100.00\% | 5 |
| 291 | 300 | 69 | 2 | 1 | 0 | -100 | 14.4830 | 7.8583 | 127 | 64 | 42.33\% | 92.75\% | 100.00\% | 5 |
| 292 | 300 | 69 | 2 | 1 | 0 | -100 | 14.4660 | 8.2813 | 128 | 64 | 42.67\% | 92.75\% | 100.00\% | 5 |
| 293 | 300 | 69 | 2 | 1 | 0 | -100 | 14.7830 | 9.2598 | 127 | 64 | 42.33\% | 92.75\% | 100.00\% | 5 |
| 294 | 300 | 69 | 2 | 1 | 0 | -100 | 14.5340 | 7.5276 | 127 | 64 | 42.33\% | 92.75\% | 100.00\% | 5 |
| 295 | 300 | 69 | 2 | 1 | 0 | -100 | 14.5330 | 9.2835 | 127 | 64 | 42.33\% | 92.75\% | 100.00\% | 5 |
| 296 | 250 | 69 | 2 | 1 | 0 | -100 | 13.4040 | 10.0635 | 126 | 64 | 50.40\% | 92.75\% | 100.00\% | 5 |
| 297 | 250 | 69 | 2 | 1 | 0 | -100 | 13.2020 | 9.4206 | 126 | 64 | 50.40\% | 92.75\% | 100.00\% | 5 |
| 298 | 250 | 69 | 2 | 1 | 0 | -100 | 12.9400 | 9.5276 | 127 | 64 | 50.80\% | 92.75\% | 100.00\% | 5 |
| 299 | 250 | 69 | 2 | 1 | 0 | -100 | 13.3010 | 8.9921 | 127 | 64 | 50.80\% | 92.75\% | 100.00\% | 5 |

Table B.1. Computational results of the proposed algorithm. (cont.)

| $\begin{gathered} \text { Iteration } \\ \quad \# \end{gathered}$ | Number <br> of <br> Riders | Number of Drivers | Capacity | Rider <br> Count | Number of Riders Rejecting First Match | $\begin{gathered} \text { JSS } \\ \text { Limit } \end{gathered}$ | Computation <br> Time | Average JSS of Matched Pairs | Number <br> of <br> Matched <br> Riders | $\begin{gathered} \text { Number } \\ \text { of } \\ \text { Matched } \\ \text { Drivers } \end{gathered}$ | $\begin{gathered} \text { Ratio } \\ \text { of } \\ \text { Matched } \\ \text { Riders } \end{gathered}$ | Ratio of <br> Matched <br> Drivers | Ratio of <br> Riders <br> Accepting <br> First Match | $\begin{gathered} \text { Case } \\ \# \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 300 | 250 | 69 | 2 | 1 | 0 | -100 | 13.1980 | 9.4206 | 126 | 64 | 50.40\% | 92.75\% | 100.00\% | 5 |
| 301 | 200 | 69 | 2 | 1 | 0 | -100 | 12.0140 | 7.2581 | 124 | 62 | 62.00\% | 89.86\% | 100.00\% | 5 |
| 302 | 200 | 69 | 2 | 1 | 0 | -100 | 12.1000 | 9.3360 | 125 | 63 | 62.50\% | 91.30\% | 100.00\% | 5 |
| 303 | 200 | 69 | 2 | 1 | 0 | -100 | 11.9460 | 10.0439 | 114 | 58 | 57.00\% | 84.06\% | 100.00\% | 5 |
| 304 | 200 | 69 | 2 | 1 | 0 | -100 | 12.1120 | 9.9508 | 122 | 62 | 61.00\% | 89.86\% | 100.00\% | 5 |
| 305 | 200 | 69 | 2 | 1 | 0 | -100 | 12.6720 | 9.3600 | 125 | 63 | 62.50\% | 91.30\% | 100.00\% | 5 |
| 306 | 150 | 69 | 2 | 1 | 0 | -100 | 10.5390 | 12.3529 | 102 | 54 | 68.00\% | 78.26\% | 100.00\% | 5 |
| 307 | 150 | 69 | 2 | 1 | 0 | -100 | 10.3440 | 9.6132 | 106 | 54 | 70.67\% | 78.26\% | 100.00\% | 5 |
| 308 | 150 | 69 | 2 | 1 | 0 | -100 | 10.6530 | 9.5913 | 115 | 59 | 76.67\% | 85.51\% | 100.00\% | 5 |
| 309 | 150 | 69 | 2 | 1 | 0 | -100 | 10.8130 | 9.0357 | 112 | 59 | 74.67\% | 85.51\% | 100.00\% | 5 |
| 310 | 150 | 69 | 2 | 1 | 0 | -100 | 10.3110 | 10.7383 | 107 | 55 | 71.33\% | 79.71\% | 100.00\% | 5 |
| 311 | 100 | 69 | 2 | 1 | 0 | -100 | 8.0250 | 11.7841 | 88 | 48 | 88.00\% | 69.57\% | 100.00\% | 5 |
| 312 | 100 | 69 | 2 | 1 | 0 | -100 | 7.8760 | 15.7000 | 80 | 43 | 80.00\% | 62.32\% | 100.00\% | 5 |
| 313 | 100 | 69 | 2 | 1 | 0 | -100 | 7.5740 | 12.8861 | 79 | 43 | 79.00\% | 62.32\% | 100.00\% | 5 |
| 314 | 100 | 69 | 2 | 1 | 0 | -100 | 8.4900 | 10.7872 | 94 | 51 | 94.00\% | 73.91\% | 100.00\% | 5 |
| 315 | 100 | 69 | 2 | 1 | 0 | -100 | 8.4800 | 11.9775 | 89 | 49 | 89.00\% | 71.01\% | 100.00\% | 5 |
| 316 | 50 | 69 | 2 | 1 | 0 | -100 | 4.3460 | 16.3913 | 46 | 29 | 92.00\% | 42.03\% | 100.00\% | 5 |
| 317 | 50 | 69 | 2 | 1 | 0 | -100 | 4.1560 | 13.0732 | 41 | 26 | 82.00\% | 37.68\% | 100.00\% | 5 |
| 318 | 50 | 69 | 2 | 1 | 0 | -100 | 4.4920 | 15.7234 | 47 | 28 | 94.00\% | 40.58\% | 100.00\% | 5 |
| 319 | 50 | 69 | 2 | 1 | 0 | -100 | 4.4040 | 15.5319 | 47 | 27 | 94.00\% | 39.13\% | 100.00\% | 5 |
| 320 | 50 | 69 | 2 | 1 | 0 | -100 | 4.1650 | 17.1458 | 48 | 28 | 96.00\% | 40.58\% | 100.00\% | 5 |
| 321 | 1 | 69 | 2 | 1 | 0 | -100 | 0.1790 | 40.0000 | 1 | 1 | 100.00\% | 1.45\% | 100.00\% | 5 |
| 322 | 1 | 69 | 2 | 1 | 0 | -100 | 0.0570 | 34.0000 | 1 | 1 | 100.00\% | 0.00\% | 100.00\% | 5 |

Table B.1. Computational results of the proposed algorithm. (cont.)

| $\begin{gathered} \text { Iteration } \\ \quad \# \end{gathered}$ | Number <br> of <br> Riders | Number of Drivers | Capacity | Rider <br> Count | Number of Riders Rejecting First Match | $\begin{gathered} \text { JSS } \\ \text { Limit } \end{gathered}$ | Computation <br> Time | Average JSS of Matched Pairs | Number <br> of <br> Matched <br> Riders | $\begin{gathered} \text { Number } \\ \text { of } \\ \text { Matched } \\ \text { Drivers } \end{gathered}$ | $\begin{gathered} \text { Ratio } \\ \text { of } \\ \text { Matched } \\ \text { Riders } \end{gathered}$ | Ratio of <br> Matched <br> Drivers | Ratio of <br> Riders <br> Accepting <br> First Match | $\begin{gathered} \text { Case } \\ \# \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 323 | 1 | 69 | 2 | 1 | 0 | -100 | 0.0920 | 0.0000 | 1 | 1 | 100.00\% | 1.45\% | 100.00\% | 5 |
| 324 | 1 | 69 | 2 | 1 | 0 | -100 | 0.0880 | 0.0000 | 1 | 1 | 100.00\% | 1.45\% | 100.00\% | 5 |
| 325 | 1 | 69 | 2 | 1 | 0 | -100 | 0.0880 | 30.0000 | 1 | 1 | 100.00\% | 1.45\% | 100.00\% | 5 |
| 326 | 450 | 69 | 1 | 1 | 0 | -100 | 14.1530 | 8.1194 | 67 | 67 | 14.89\% | 97.10\% | 100.00\% | 6 |
| 327 | 450 | 69 | 1 | 1 | 0 | -100 | 14.0540 | 8.0746 | 67 | 67 | 14.89\% | 97.10\% | 100.00\% | 6 |
| 328 | 450 | 69 | 1 | 1 | 0 | -100 | 14.2890 | 7.6212 | 66 | 66 | 14.67\% | 95.65\% | 100.00\% | 6 |
| 329 | 450 | 69 | 1 | 1 | 0 | -100 | 13.8980 | 5.8508 | 67 | 67 | 14.89\% | 97.10\% | 100.00\% | 6 |
| 330 | 450 | 69 | 1 | 1 | 0 | -100 | 14.2600 | 6.6866 | 67 | 67 | 14.89\% | 97.10\% | 100.00\% | 6 |
| 331 | 400 | 69 | 1 | 1 | 0 | -100 | 13.0380 | 6.1940 | 67 | 67 | 16.75\% | 97.10\% | 100.00\% | 6 |
| 332 | 400 | 69 | 1 | 1 | 0 | -100 | 12.8860 | 7.2424 | 66 | 66 | 16.50\% | 95.65\% | 100.00\% | 6 |
| 333 | 400 | 69 | 1 | 1 | 0 | -100 | 12.8020 | 6.2576 | 66 | 66 | 16.50\% | 95.65\% | 100.00\% | 6 |
| 334 | 400 | 69 | 1 | 1 | 0 | -100 | 15.3820 | 7.0597 | 67 | 67 | 16.75\% | 97.10\% | 100.00\% | 6 |
| 335 | 400 | 69 | 1 | 1 | 0 | -100 | 15.0920 | 6.5385 | 65 | 65 | 16.25\% | 94.20\% | 100.00\% | 6 |
| 336 | 350 | 69 | 1 | 1 | 0 | -100 | 12.3980 | 6.1250 | 64 | 64 | 18.29\% | 92.75\% | 100.00\% | 6 |
| 337 | 350 | 69 | 1 | 1 | 0 | -100 | 12.2170 | 7.6769 | 65 | 65 | 18.57\% | 94.20\% | 100.00\% | 6 |
| 338 | 350 | 69 | 1 | 1 | 0 | -100 | 13.0650 | 5.2388 | 67 | 67 | 19.14\% | 97.10\% | 100.00\% | 6 |
| 339 | 350 | 69 | 1 | 1 | 0 | -100 | 13.7210 | 7.9242 | 66 | 66 | 18.86\% | 95.65\% | 100.00\% | 6 |
| 340 | 350 | 69 | 1 | 1 | 0 | -100 | 12.1100 | 6.7576 | 66 | 66 | 18.86\% | 95.65\% | 100.00\% | 6 |
| 341 | 300 | 69 | 1 | 1 | 0 | -100 | 10.4170 | 4.8000 | 65 | 65 | 21.67\% | 94.20\% | 100.00\% | 6 |
| 342 | 300 | 69 | 1 | 1 | 0 | -100 | 10.3620 | 6.3030 | 66 | 66 | 22.00\% | 95.65\% | 100.00\% | 6 |
| 343 | 300 | 69 | 1 | 1 | 0 | -100 | 10.4340 | 9.6094 | 64 | 64 | 21.33\% | 92.75\% | 100.00\% | 6 |
| 344 | 300 | 69 | 1 | 1 | 0 | -100 | 10.7850 | 5.7463 | 67 | 67 | 22.33\% | 97.10\% | 100.00\% | 6 |
| 345 | 300 | 69 | 1 | 1 | 0 | -100 | 10.2320 | 5.1385 | 65 | 65 | 21.67\% | 94.20\% | 100.00\% | 6 |

Table B.1. Computational results of the proposed algorithm. (cont.)

| Iteration \# | Number <br> of <br> Riders | Number of Drivers | Capacity | Rider <br> Count | Number of Riders Rejecting First Match | $\begin{gathered} \text { JSS } \\ \text { Limit } \end{gathered}$ | Computation Time | Average JSS of Matched Pairs | Number <br> of <br> Matched <br> Riders | $\begin{gathered} \text { Number } \\ \text { of } \\ \text { Matched } \\ \text { Drivers } \end{gathered}$ | Ratio of Matched Riders | Ratio of <br> Matched <br> Drivers | Ratio of <br> Riders <br> Accepting <br> First Match | $\begin{gathered} \text { Case } \\ \# \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 346 | 250 | 69 | 1 | 1 | 0 | -100 | 9.3850 | 6.9231 | 65 | 65 | 26.00\% | 94.20\% | 100.00\% | 6 |
| 347 | 250 | 69 | 1 | 1 | 0 | -100 | 9.3660 | 8.8333 | 66 | 66 | 26.40\% | 95.65\% | 100.00\% | 6 |
| 348 | 250 | 69 | 1 | 1 | 0 | -100 | 9.3200 | 8.2727 | 66 | 66 | 26.40\% | 95.65\% | 100.00\% | 6 |
| 349 | 250 | 69 | 1 | 1 | 0 | -100 | 9.4680 | 6.8125 | 64 | 64 | 25.60\% | 92.75\% | 100.00\% | 6 |
| 350 | 250 | 69 | 1 | 1 | 0 | -100 | 9.0840 | 4.7121 | 66 | 66 | 26.40\% | 95.65\% | 100.00\% | 6 |
| 351 | 200 | 69 | 1 | 1 | 0 | -100 | 8.3470 | 7.5938 | 64 | 64 | 32.00\% | 92.75\% | 100.00\% | 6 |
| 352 | 200 | 69 | 1 | 1 | 0 | -100 | 8.1660 | 8.4844 | 64 | 64 | 32.00\% | 92.75\% | 100.00\% | 6 |
| 353 | 200 | 69 | 1 | 1 | 0 | -100 | 7.8970 | 7.2923 | 65 | 65 | 32.50\% | 94.20\% | 100.00\% | 6 |
| 354 | 200 | 69 | 1 | 1 | 0 | -100 | 7.9200 | 7.8254 | 63 | 63 | 31.50\% | 91.30\% | 100.00\% | 6 |
| 355 | 200 | 69 | 1 | 1 | 0 | -100 | 8.0090 | 6.0156 | 64 | 64 | 32.00\% | 92.75\% | 100.00\% | 6 |
| 356 | 150 | 69 | 1 | 1 | 0 | -100 | 7.2910 | 8.2188 | 64 | 64 | 42.67\% | 92.75\% | 100.00\% | 6 |
| 357 | 150 | 69 | 1 | 1 | 0 | -100 | 7.1510 | 8.8254 | 63 | 63 | 42.00\% | 91.30\% | 100.00\% | 6 |
| 358 | 150 | 69 | 1 | 1 | 0 | -100 | 6.7410 | 6.3438 | 64 | 64 | 42.67\% | 92.75\% | 100.00\% | 6 |
| 359 | 150 | 69 | 1 | 1 | 0 | -100 | 7.1490 | 6.7344 | 64 | 64 | 42.67\% | 92.75\% | 100.00\% | 6 |
| 360 | 150 | 69 | 1 | 1 | 0 | -100 | 7.3490 | 6.5238 | 63 | 63 | 42.00\% | 91.30\% | 100.00\% | 6 |
| 361 | 100 | 69 | 1 | 1 | 0 | -100 | 5.8550 | 7.4677 | 62 | 62 | 62.00\% | 89.86\% | 100.00\% | 6 |
| 362 | 100 | 69 | 1 | 1 | 0 | -100 | 6.0050 | 8.8889 | 63 | 63 | 63.00\% | 91.30\% | 100.00\% | 6 |
| 363 | 100 | 69 | 1 | 1 | 0 | -100 | 6.0180 | 8.7742 | 62 | 62 | 62.00\% | 89.86\% | 100.00\% | 6 |
| 364 | 100 | 69 | 1 | 1 | 0 | -100 | 5.9810 | 6.6721 | 61 | 61 | 61.00\% | 88.41\% | 100.00\% | 6 |
| 365 | 100 | 69 | 1 | 1 | 0 | -100 | 5.8770 | 7.6129 | 62 | 62 | 62.00\% | 89.86\% | 100.00\% | 6 |
| 366 | 50 | 69 | 1 | 1 | 0 | -100 | 3.4340 | 12.2381 | 42 | 42 | 84.00\% | 60.87\% | 100.00\% | 6 |
| 367 | 50 | 69 | 1 | 1 | 0 | -100 | 4.0420 | 12.0930 | 43 | 43 | 86.00\% | 62.32\% | 100.00\% | 6 |
| 368 | 50 | 69 | 1 | 1 | 0 | -100 | 3.8220 | 9.2750 | 40 | 40 | 80.00\% | 57.97\% | 100.00\% | 6 |

Table B.1. Computational results of the proposed algorithm. (cont.)

| $\begin{gathered} \text { Iteration } \\ \quad \# \end{gathered}$ | Number <br> of <br> Riders | Number <br> of <br> Drivers | Capacity | Rider <br> Count | Number of Riders Rejecting First Match | $\begin{gathered} \text { JSS } \\ \text { Limit } \end{gathered}$ | Computation <br> Time | Average JSS of Matched Pairs | Number <br> of <br> Matched <br> Riders | $\begin{gathered} \text { Number } \\ \text { of } \\ \text { Matched } \\ \text { Drivers } \end{gathered}$ | Ratio of Matched Riders | Ratio of <br> Matched <br> Drivers | Ratio of <br> Riders <br> Accepting <br> First Match | $\begin{gathered} \text { Case } \\ \# \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 369 | 50 | 69 | 1 | 1 | 0 | -100 | 3.7310 | 9.0270 | 37 | 37 | 74.00\% | 53.62\% | 100.00\% | 6 |
| 370 | 50 | 69 | 1 | 1 | 0 | -100 | 3.9600 | 10.0233 | 43 | 43 | 86.00\% | 62.32\% | 100.00\% | 6 |
| 371 | 1 | 69 | 1 | 1 | 0 | -100 | 0.1030 | 25.0000 | 1 | 1 | 100.00\% | 1.45\% | 100.00\% | 6 |
| 372 | 1 | 69 | 1 | 1 | 0 | -100 | 0.0770 | 10.0000 | 1 | 1 | 100.00\% | 1.45\% | 100.00\% | 6 |
| 373 | 1 | 69 | 1 | 1 | 0 | -100 | 0.1770 | 55.0000 | 1 | 1 | 100.00\% | 1.45\% | 100.00\% | 6 |
| 374 | 1 | 69 | 1 | 1 | 0 | -100 | 0.0840 | 0.0000 | 1 | 1 | 100.00\% | 1.45\% | 100.00\% | 6 |
| 375 | 1 | 69 | 1 | 1 | 0 | -100 | 0.0860 | 0.0000 | 1 | 1 | 100.00\% | 1.45\% | 100.00\% | 6 |
| 376 | 479 | 69 | 3 | 2 | 0 | -100 | 14.7960 | 7.8657 | 67 | 67 | 13.99\% | 97.10\% | 100.00\% | 7 |
| 377 | 479 | 69 | 3 | 2 | 0 | -100 | 14.8030 | 7.8657 | 67 | 67 | 13.99\% | 97.10\% | 100.00\% | 7 |
| 378 | 479 | 69 | 3 | 2 | 0 | -100 | 14.8490 | 7.8657 | 67 | 67 | 13.99\% | 97.10\% | 100.00\% | 7 |
| 379 | 479 | 69 | 3 | 2 | 0 | -100 | 14.8490 | 7.8657 | 67 | 67 | 13.99\% | 97.10\% | 100.00\% | 7 |
| 380 | 479 | 69 | 3 | 2 | 0 | -100 | 14.8960 | 7.8657 | 67 | 67 | 13.99\% | 97.10\% | 100.00\% | 7 |
| 381 | 479 | 65 | 3 | 2 | 0 | -100 | 13.9660 | 7.0318 | 63 | 63 | 13.15\% | 96.92\% | 100.00\% | 7 |
| 382 | 479 | 65 | 3 | 2 | 0 | -100 | 13.9560 | 7.8413 | 63 | 63 | 13.15\% | 96.92\% | 100.00\% | 7 |
| 383 | 479 | 65 | 3 | 2 | 0 | -100 | 14.0360 | 7.8906 | 64 | 64 | 13.36\% | 98.46\% | 100.00\% | 7 |
| 384 | 479 | 65 | 3 | 2 | 0 | -100 | 13.8060 | 7.6719 | 64 | 64 | 13.36\% | 98.46\% | 100.00\% | 7 |
| 385 | 479 | 65 | 3 | 2 | 0 | -100 | 14.1300 | 8.3651 | 63 | 63 | 13.15\% | 96.92\% | 100.00\% | 7 |
| 386 | 479 | 60 | 3 | 2 | 0 | -100 | 12.9300 | 7.0690 | 58 | 58 | 12.11\% | 96.67\% | 100.00\% | 7 |
| 387 | 479 | 60 | 3 | 2 | 0 | -100 | 13.1460 | 6.3104 | 58 | 58 | 12.11\% | 96.67\% | 100.00\% | 7 |
| 388 | 479 | 60 | 3 | 2 | 0 | -100 | 12.9960 | 8.8644 | 59 | 59 | 12.32\% | 98.33\% | 100.00\% | 7 |
| 389 | 479 | 60 | 3 | 2 | 0 | -100 | 13.3350 | 7.7241 | 58 | 58 | 12.11\% | 96.67\% | 100.00\% | 7 |
| 390 | 479 | 60 | 3 | 2 | 0 | -100 | 13.0910 | 7.1525 | 59 | 59 | 12.32\% | 98.33\% | 100.00\% | 7 |
| 391 | 479 | 55 | 3 | 2 | 0 | -100 | 12.0460 | 7.0741 | 54 | 54 | 11.27\% | 98.18\% | 100.00\% | 7 |

Table B.1. Computational results of the proposed algorithm. (cont.)

| $\begin{gathered} \text { Iteration } \\ \quad \# \end{gathered}$ | Number <br> of <br> Riders | Number <br> of <br> Drivers | Capacity | Rider <br> Count | Number <br> of Riders <br> Rejecting <br> First Match | $\begin{gathered} \text { JSS } \\ \text { Limit } \end{gathered}$ | Computation Time | Average JSS of Matched Pairs | Number <br> of <br> Matched <br> Riders | Number <br> of <br> Matched <br> Drivers | Ratio of Matched Riders | Ratio of <br> Matched <br> Drivers | Ratio of <br> Riders <br> Accepting <br> First Match | $\begin{gathered} \text { Case } \\ \# \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 392 | 479 | 55 | 3 | 2 | 0 | -100 | 11.9470 | 6.6182 | 55 | 55 | 11.48\% | 100.00\% | 100.00\% | 7 |
| 393 | 479 | 55 | 3 | 2 | 0 | -100 | 13.1470 | 8.7925 | 53 | 53 | 11.06\% | 96.36\% | 100.00\% | 7 |
| 394 | 479 | 55 | 3 | 2 | 0 | -100 | 13.1160 | 6.0377 | 53 | 53 | 11.06\% | 96.36\% | 100.00\% | 7 |
| 395 | 479 | 55 | 3 | 2 | 0 | -100 | 12.4520 | 7.2593 | 54 | 54 | 11.27\% | 98.18\% | 100.00\% | 7 |
| 396 | 479 | 50 | 3 | 2 | 0 | -100 | 12.0560 | 6.1000 | 50 | 50 | 10.44\% | 100.00\% | 100.00\% | 7 |
| 397 | 479 | 50 | 3 | 2 | 0 | -100 | 12.2900 | 7.7959 | 49 | 49 | 10.23\% | 98.00\% | 100.00\% | 7 |
| 398 | 479 | 50 | 3 | 2 | 0 | -100 | 11.3720 | 5.3400 | 50 | 50 | 10.44\% | 100.00\% | 100.00\% | 7 |
| 399 | 479 | 50 | 3 | 2 | 0 | -100 | 12.4870 | 7.4400 | 50 | 50 | 10.44\% | 100.00\% | 100.00\% | 7 |
| 400 | 479 | 50 | 3 | 2 | 0 | -100 | 11.7710 | 6.6600 | 50 | 50 | 10.44\% | 100.00\% | 100.00\% | 7 |
| 401 | 479 | 45 | 3 | 2 | 0 | -100 | 9.7230 | 4.6000 | 45 | 45 | 9.39\% | 100.00\% | 100.00\% | 7 |
| 402 | 479 | 45 | 3 | 2 | 0 | -100 | 9.9350 | 7.2500 | 44 | 44 | 9.19\% | 97.78\% | 100.00\% | 7 |
| 403 | 479 | 45 | 3 | 2 | 0 | -100 | 9.8720 | 4.7556 | 45 | 45 | 9.39\% | 100.00\% | 100.00\% | 7 |
| 404 | 479 | 45 | 3 | 2 | 0 | -100 | 9.8710 | 6.2667 | 45 | 45 | 9.39\% | 100.00\% | 100.00\% | 7 |
| 405 | 479 | 45 | 3 | 2 | 0 | -100 | 9.7990 | 5.4000 | 45 | 45 | 9.39\% | 100.00\% | 100.00\% | 7 |
| 406 | 479 | 40 | 3 | 2 | 0 | -100 | 8.8360 | 5.9250 | 40 | 40 | 8.35\% | 100.00\% | 100.00\% | 7 |
| 407 | 479 | 40 | 3 | 2 | 0 | -100 | 8.9120 | 6.0250 | 40 | 40 | 8.35\% | 100.00\% | 100.00\% | 7 |
| 408 | 479 | 40 | 3 | 2 | 0 | -100 | 8.9820 | 7.4750 | 40 | 40 | 8.35\% | 100.00\% | 100.00\% | 7 |
| 409 | 479 | 40 | 3 | 2 | 0 | -100 | 9.1940 | 8.6053 | 38 | 38 | 7.93\% | 95.00\% | 100.00\% | 7 |
| 410 | 479 | 40 | 3 | 2 | 0 | -100 | 9.1750 | 9.2051 | 39 | 39 | 8.14\% | 97.50\% | 100.00\% | 7 |
| 411 | 479 | 35 | 3 | 2 | 0 | -100 | 8.0320 | 7.1429 | 35 | 35 | 7.31\% | 100.00\% | 100.00\% | 7 |
| 412 | 479 | 35 | 3 | 2 | 0 | -100 | 7.8660 | 8.7429 | 35 | 35 | 7.31\% | 100.00\% | 100.00\% | 7 |
| 413 | 479 | 35 | 3 | 2 | 0 | -100 | 7.9890 | 6.2571 | 35 | 35 | 7.31\% | 100.00\% | 100.00\% | 7 |
| 414 | 479 | 35 | 3 | 2 | 0 | -100 | 8.0240 | 4.8571 | 35 | 35 | 7.31\% | 100.00\% | 100.00\% | 7 |

Table B.1. Computational results of the proposed algorithm. (cont.)

| Iteration \# | Number <br> of <br> Riders | Number of Drivers | Capacity | Rider <br> Count | Number of Riders Rejecting First Match | $\begin{gathered} \text { JSS } \\ \text { Limit } \end{gathered}$ | Computation <br> Time | Average JSS of Matched Pairs | Number <br> of <br> Matched <br> Riders | $\begin{gathered} \text { Number } \\ \text { of } \\ \text { Matched } \\ \text { Drivers } \end{gathered}$ | Ratio of Matched Riders | Ratio of <br> Matched <br> Drivers | Ratio of <br> Riders <br> Accepting <br> First Match | $\begin{gathered} \text { Case } \\ \# \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 415 | 479 | 35 | 3 | 2 | 0 | -100 | 8.2350 | 5.3714 | 35 | 35 | 7.31\% | 100.00\% | 100.00\% | 7 |
| 416 | 479 | 30 | 3 | 2 | 0 | -100 | 7.9430 | 7.9000 | 30 | 30 | 6.26\% | 100.00\% | 100.00\% | 7 |
| 417 | 479 | 30 | 3 | 2 | 0 | -100 | 7.5630 | 8.4000 | 30 | 30 | 6.26\% | 100.00\% | 100.00\% | 7 |
| 418 | 479 | 30 | 3 | 2 | 0 | -100 | 7.3660 | 9.0667 | 30 | 30 | 6.26\% | 100.00\% | 100.00\% | 7 |
| 419 | 479 | 30 | 3 | 2 | 0 | -100 | 7.4140 | 7.0000 | 30 | 30 | 6.26\% | 100.00\% | 100.00\% | 7 |
| 420 | 479 | 30 | 3 | 2 | 0 | -100 | 7.4570 | 9.1000 | 30 | 30 | 6.26\% | 100.00\% | 100.00\% | 7 |
| 421 | 479 | 25 | 3 | 2 | 0 | -100 | 6.2670 | 14.4000 | 25 | 25 | 5.22\% | 100.00\% | 100.00\% | 7 |
| 422 | 479 | 25 | 3 | 2 | 0 | -100 | 6.3320 | 7.8000 | 25 | 25 | 5.22\% | 100.00\% | 100.00\% | 7 |
| 423 | 479 | 25 | 3 | 2 | 0 | -100 | 6.4980 | 7.8400 | 25 | 25 | 5.22\% | 100.00\% | 100.00\% | 7 |
| 424 | 479 | 25 | 3 | 2 | 0 | -100 | 6.3770 | 3.8400 | 25 | 25 | 5.22\% | 100.00\% | 100.00\% | 7 |
| 425 | 479 | 25 | 3 | 2 | 0 | -100 | 6.5470 | 3.2400 | 25 | 25 | 5.22\% | 100.00\% | 100.00\% | 7 |
| 426 | 479 | 20 | 3 | 2 | 0 | -100 | 5.7850 | 5.9500 | 20 | 20 | 4.18\% | 100.00\% | 100.00\% | 7 |
| 427 | 479 | 20 | 3 | 2 | 0 | -100 | 5.7650 | 6.5000 | 20 | 20 | 4.18\% | 100.00\% | 100.00\% | 7 |
| 428 | 479 | 20 | 3 | 2 | 0 | -100 | 5.6930 | 12.5000 | 20 | 20 | 4.18\% | 100.00\% | 100.00\% | 7 |
| 429 | 479 | 20 | 3 | 2 | 0 | -100 | 5.6330 | 2.0000 | 20 | 20 | 4.18\% | 100.00\% | 100.00\% | 7 |
| 430 | 479 | 20 | 3 | 2 | 0 | -100 | 5.4630 | 1.8000 | 20 | 20 | 4.18\% | 100.00\% | 100.00\% | 7 |
| 431 | 479 | 15 | 3 | 2 | 0 | -100 | 4.4240 | 3.4000 | 15 | 15 | 3.13\% | 100.00\% | 100.00\% | 7 |
| 432 | 479 | 15 | 3 | 2 | 0 | -100 | 4.4380 | 3.8667 | 15 | 15 | 3.13\% | 100.00\% | 100.00\% | 7 |
| 433 | 479 | 15 | 3 | 2 | 0 | -100 | 4.3210 | 3.8000 | 15 | 15 | 3.13\% | 100.00\% | 100.00\% | 7 |
| 434 | 479 | 15 | 3 | 2 | 0 | -100 | 4.2560 | 5.2000 | 15 | 15 | 3.13\% | 100.00\% | 100.00\% | 7 |
| 435 | 479 | 15 | 3 | 2 | 0 | -100 | 4.3720 | 14.0667 | 15 | 15 | 3.13\% | 100.00\% | 100.00\% | 7 |
| 436 | 479 | 10 | 3 | 2 | 0 | -100 | 3.4960 | 4.3000 | 10 | 10 | 2.09\% | 100.00\% | 100.00\% | 7 |
| 437 | 479 | 10 | 3 | 2 | 0 | -100 | 3.5580 | 6.6000 | 10 | 10 | 2.09\% | 100.00\% | 100.00\% | 7 |

Table B.1. Computational results of the proposed algorithm. (cont.)

| Iteration \# |  |  | Capacity | Rider <br> Count | Number <br> of Riders <br> Rejecting <br> First Match | $\begin{gathered} \text { JSS } \\ \text { Limit } \end{gathered}$ | Computation Time | Average JSS of Matched Pairs | Number <br> of <br> Matched <br> Riders | Number <br> of <br> Matched <br> Drivers | ```Ratio of Matched Riders``` | $\begin{gathered} \text { Ratio } \\ \text { of } \\ \text { Matched } \\ \text { Drivers } \end{gathered}$ | Ratio of <br> Riders <br> Accepting <br> First Match | $\begin{gathered} \text { Case } \\ \# \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 438 | 479 | 10 | 3 | 2 | 0 | -100 | 3.7420 | 10.5000 | 10 | 10 | 2.09\% | 100.00\% | 100.00\% | 7 |
| 439 | 479 | 10 | 3 | 2 | 0 | -100 | 3.4180 | 0.7000 | 10 | 10 | 2.09\% | 100.00\% | 100.00\% | 7 |
| 440 | 479 | 10 | 3 | 2 | 0 | -100 | 3.4460 | 11.0000 | 10 | 10 | 2.09\% | 100.00\% | 100.00\% | 7 |
| 441 | 479 | 5 | 3 | 2 | 0 | -100 | 3.1060 | 7.6000 | 5 | 5 | 1.04\% | 100.00\% | 100.00\% | 7 |
| 442 | 479 | 5 | 3 | 2 | 0 | -100 | 2.9580 | 2.0000 | 5 | 5 | 1.04\% | 100.00\% | 100.00\% | 7 |
| 443 | 479 | 5 | 3 | 2 | 0 | -100 | 2.7070 | 12.2000 | 5 | 5 | 1.04\% | 100.00\% | 100.00\% | 7 |
| 444 | 479 | 5 | 3 | 2 | 0 | -100 | 2.7840 | 4.4000 | 5 | 5 | 1.04\% | 100.00\% | 100.00\% | 7 |
| 445 | 479 | 5 | 3 | 2 | 0 | -100 | 2.7520 | 5.4000 | 5 | 5 | $1.04 \%$ | 100.00\% | 100.00\% | 7 |
| 446 | 479 | 1 | 3 | 2 | 0 | -100 | 2.1650 | 25.0000 | 1 | 1 | 0.21\% | 100.00\% | 100.00\% | 7 |
| 447 | 479 | 1 | 3 | 2 | 0 | -100 | 2.1800 | 10.0000 | 1 | 1 | 0.21\% | 100.00\% | 100.00\% | 7 |
| 448 | 479 | 1 | 3 | 2 | 0 | -100 | 2.1750 | -5.0000 | 1 | 1 | 0.21\% | 100.00\% | 100.00\% | 7 |
| 449 | 479 | 1 | 3 | 2 | 0 | -100 | 2.2530 | -20.0000 | 1 | 1 | 0.21\% | 100.00\% | 100.00\% | 7 |
| 450 | 479 | 1 | 3 | 2 | 0 | -100 | 2.0710 | 2.0000 | 1 | 1 | 0.21\% | 100.00\% | 100.00\% | 7 |
| 451 | 479 | 69 | 3 | 2 | 0 | -100 | 14.7980 | 7.8657 | 67 | 67 | 13.99\% | 97.10\% | 100.00\% | 8 |
| 452 | 479 | 69 | 3 | 2 | 0 | -100 | 14.9710 | 7.8657 | 67 | 67 | 13.99\% | 97.10\% | 100.00\% | 8 |
| 453 | 479 | 69 | 3 | 2 | 0 | -100 | 14.8170 | 7.8657 | 67 | 67 | 13.99\% | 97.10\% | 100.00\% | 8 |
| 454 | 479 | 69 | 3 | 2 | 0 | -100 | 14.8130 | 7.8657 | 67 | 67 | 13.99\% | 97.10\% | 100.00\% | 8 |
| 455 | 479 | 69 | 3 | 2 | 0 | -100 | 14.7620 | 7.8657 | 67 | 67 | 13.99\% | 97.10\% | 100.00\% | 8 |
| 456 | 450 | 69 | 3 | 2 | 0 | -100 | 14.1550 | 5.7424 | 66 | 66 | 14.67\% | 95.65\% | 100.00\% | 8 |
| 457 | 450 | 69 | 3 | 2 | 0 | -100 | 14.1660 | 7.6667 | 66 | 66 | 14.67\% | 95.65\% | 100.00\% | 8 |
| 458 | 450 | 69 | 3 | 2 | 0 | -100 | 14.0230 | 5.5522 | 67 | 67 | 14.89\% | 97.10\% | 100.00\% | 8 |
| 459 | 450 | 69 | 3 | 2 | 0 | -100 | 14.1840 | 8.5672 | 67 | 67 | 14.89\% | 97.10\% | 100.00\% | 8 |
| 460 | 450 | 69 | 3 | 2 | 0 | -100 | 14.1410 | 7.0597 | 67 | 67 | 14.89\% | 97.10\% | 100.00\% | 8 |

Table B.1. Computational results of the proposed algorithm. (cont.)

| Iteration \# | Number <br> of <br> Riders | Number of Drivers | Capacity | Rider <br> Count | Number of Riders Rejecting First Match | $\begin{gathered} \text { JSS } \\ \text { Limit } \end{gathered}$ | Computation <br> Time | Average JSS of Matched Pairs | Number <br> of <br> Matched <br> Riders | $\begin{gathered} \text { Number } \\ \text { of } \\ \text { Matched } \\ \text { Drivers } \end{gathered}$ | $\begin{gathered} \text { Ratio } \\ \text { of } \\ \text { Matched } \\ \text { Riders } \end{gathered}$ | Ratio of <br> Matched <br> Drivers | Ratio of <br> Riders <br> Accepting <br> First Match | $\begin{gathered} \text { Case } \\ \# \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 461 | 400 | 69 | 3 | 2 | 0 | -100 | 13.2040 | 7.9105 | 67 | 67 | 16.75\% | 97.10\% | 100.00\% | 8 |
| 462 | 400 | 69 | 3 | 2 | 0 | -100 | 13.8880 | 5.5455 | 66 | 66 | 16.50\% | 95.65\% | 100.00\% | 8 |
| 463 | 400 | 69 | 3 | 2 | 0 | -100 | 12.9930 | 6.5075 | 67 | 67 | 16.75\% | 97.10\% | 100.00\% | 8 |
| 464 | 400 | 69 | 3 | 2 | 0 | -100 | 13.4020 | 6.2424 | 66 | 66 | 16.50\% | 95.65\% | 100.00\% | 8 |
| 465 | 400 | 69 | 3 | 2 | 0 | -100 | 12.6560 | 8.1406 | 64 | 64 | 16.00\% | 92.75\% | 100.00\% | 8 |
| 466 | 350 | 69 | 3 | 2 | 0 | -100 | 12.8500 | 8.0769 | 65 | 65 | 18.57\% | 94.20\% | 100.00\% | 8 |
| 467 | 350 | 69 | 3 | 2 | 0 | -100 | 11.6190 | 6.6061 | 66 | 66 | 18.86\% | 95.65\% | 100.00\% | 8 |
| 468 | 350 | 69 | 3 | 2 | 0 | -100 | 11.6660 | 7.6406 | 64 | 64 | 18.29\% | 92.75\% | 100.00\% | 8 |
| 469 | 350 | 69 | 3 | 2 | 0 | -100 | 11.6090 | 6.5152 | 66 | 66 | 18.86\% | 95.65\% | 100.00\% | 8 |
| 470 | 350 | 69 | 3 | 2 | 0 | -100 | 11.5610 | 8.2000 | 65 | 65 | 18.57\% | 94.20\% | 100.00\% | 8 |
| 471 | 300 | 69 | 3 | 2 | 0 | -100 | 10.2460 | 5.5455 | 66 | 66 | 22.00\% | 95.65\% | 100.00\% | 8 |
| 472 | 300 | 69 | 3 | 2 | 0 | -100 | 10.0120 | 6.8906 | 64 | 64 | 21.33\% | 92.75\% | 100.00\% | 8 |
| 473 | 300 | 69 | 3 | 2 | 0 | -100 | 10.2720 | 6.9539 | 65 | 65 | 21.67\% | 94.20\% | 100.00\% | 8 |
| 474 | 300 | 69 | 3 | 2 | 0 | -100 | 10.3900 | 6.6769 | 65 | 65 | 21.67\% | 94.20\% | 100.00\% | 8 |
| 475 | 300 | 69 | 3 | 2 | 0 | -100 | 10.3770 | 6.6923 | 65 | 65 | 21.67\% | 94.20\% | 100.00\% | 8 |
| 476 | 250 | 69 | 3 | 2 | 0 | -100 | 9.1580 | 9.0938 | 64 | 64 | 25.60\% | 92.75\% | 100.00\% | 8 |
| 477 | 250 | 69 | 3 | 2 | 0 | -100 | 9.2400 | 5.5556 | 63 | 63 | 25.20\% | 91.30\% | 100.00\% | 8 |
| 478 | 250 | 69 | 3 | 2 | 0 | -100 | 8.6880 | 5.7656 | 64 | 64 | 25.60\% | 92.75\% | 100.00\% | 8 |
| 479 | 250 | 69 | 3 | 2 | 0 | -100 | 9.3650 | 6.0635 | 63 | 63 | 25.20\% | 91.30\% | 100.00\% | 8 |
| 480 | 250 | 69 | 3 | 2 | 0 | -100 | 9.0770 | 7.6615 | 65 | 65 | 26.00\% | 94.20\% | 100.00\% | 8 |
| 481 | 200 | 69 | 3 | 2 | 0 | -100 | 7.8090 | 10.9516 | 62 | 62 | 31.00\% | 89.86\% | 100.00\% | 8 |
| 482 | 200 | 69 | 3 | 2 | 0 | -100 | 7.8590 | 7.7344 | 64 | 64 | 32.00\% | 92.75\% | 100.00\% | 8 |
| 483 | 200 | 69 | 3 | 2 | 0 | -100 | 8.0190 | 8.2857 | 63 | 63 | 31.50\% | 91.30\% | 100.00\% | 8 |

Table B.1. Computational results of the proposed algorithm. (cont.)

| $\begin{gathered} \text { Iteration } \\ \quad \# \end{gathered}$ | Number <br> of <br> Riders | Number of Drivers | Capacity | Rider <br> Count | Number of Riders Rejecting First Match | $\begin{gathered} \text { JSS } \\ \text { Limit } \end{gathered}$ | Computation Time | Average JSS of Matched Pairs | Number <br> of <br> Matched <br> Riders | $\begin{gathered} \text { Number } \\ \text { of } \\ \text { Matched } \\ \text { Drivers } \end{gathered}$ | Ratio of Matched Riders | Ratio of <br> Matched <br> Drivers | Ratio of <br> Riders <br> Accepting <br> First Match | $\begin{gathered} \text { Case } \\ \# \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 484 | 200 | 69 | 3 | 2 | 0 | -100 | 7.7630 | 8.0923 | 65 | 65 | 32.50\% | 94.20\% | 100.00\% | 8 |
| 485 | 200 | 69 | 3 | 2 | 0 | -100 | 8.0700 | 9.4923 | 65 | 65 | 32.50\% | 94.20\% | 100.00\% | 8 |
| 486 | 150 | 69 | 3 | 2 | 0 | -100 | 6.8580 | 7.7424 | 66 | 66 | 44.00\% | 95.65\% | 100.00\% | 8 |
| 487 | 150 | 69 | 3 | 2 | 0 | -100 | 6.8860 | 8.3692 | 65 | 65 | 43.33\% | 94.20\% | 100.00\% | 8 |
| 488 | 150 | 69 | 3 | 2 | 0 | -100 | 6.9920 | 10.3968 | 63 | 63 | 42.00\% | 91.30\% | 100.00\% | 8 |
| 489 | 150 | 69 | 3 | 2 | 0 | -100 | 7.2000 | 6.1846 | 65 | 65 | 43.33\% | 94.20\% | 100.00\% | 8 |
| 490 | 150 | 69 | 3 | 2 | 0 | -100 | 7.4600 | 10.3333 | 63 | 63 | 42.00\% | 91.30\% | 100.00\% | 8 |
| 491 | 100 | 69 | 3 | 2 | 0 | -100 | 5.6600 | 10.0645 | 62 | 62 | 62.00\% | 89.86\% | 100.00\% | 8 |
| 492 | 100 | 69 | 3 | 2 | 0 | -100 | 5.7700 | 10.1905 | 63 | 63 | 63.00\% | 91.30\% | 100.00\% | 8 |
| 493 | 100 | 69 | 3 | 2 | 0 | -100 | 5.9150 | 9.0164 | 61 | 61 | 61.00\% | 88.41\% | 100.00\% | 8 |
| 494 | 100 | 69 | 3 | 2 | 0 | -100 | 6.7670 | 8.4906 | 53 | 53 | 53.00\% | 76.81\% | 100.00\% | 8 |
| 495 | 100 | 69 | 3 | 2 | 0 | -100 | 6.2620 | 9.8500 | 60 | 60 | 60.00\% | 86.96\% | 100.00\% | 8 |
| 496 | 50 | 69 | 3 | 2 | 0 | -100 | 3.6530 | 10.8537 | 41 | 41 | 82.00\% | 59.42\% | 100.00\% | 8 |
| 497 | 50 | 69 | 3 | 2 | 0 | -100 | 3.5030 | 11.5385 | 39 | 39 | 78.00\% | 56.52\% | 100.00\% | 8 |
| 498 | 50 | 69 | 3 | 2 | 0 | -100 | 3.8900 | 10.8500 | 40 | 40 | 80.00\% | 57.97\% | 100.00\% | 8 |
| 499 | 50 | 69 | 3 | 2 | 0 | -100 | 3.4380 | 9.1081 | 37 | 37 | 74.00\% | 53.62\% | 100.00\% | 8 |
| 500 | 50 | 69 | 3 | 2 | 0 | -100 | 3.7700 | 12.9524 | 42 | 42 | 84.00\% | 60.87\% | 100.00\% | 8 |
| 501 | 1 | 69 | 3 | 2 | 0 | -100 | 0.1720 | 15.0000 | 1 | 1 | 100.00\% | 1.45\% | 100.00\% | 8 |
| 502 | 1 | 69 | 3 | 2 | 0 | -100 | 0.1910 | 30.0000 | 1 | 1 | 100.00\% | 1.45\% | 100.00\% | 8 |
| 503 | 1 | 69 | 3 | 2 | 0 | -100 | 0.1870 | 0.0000 | 1 | 1 | 100.00\% | 1.45\% | 100.00\% | 8 |
| 504 | 1 | 69 | 3 | 2 | 0 | -100 | 0.2020 | 25.0000 | 1 | 1 | 100.00\% | 1.45\% | 100.00\% | 8 |
| 505 | 1 | 69 | 3 | 2 | 0 | -100 | 0.0780 | 15.0000 | 1 | 1 | 100.00\% | 1.45\% | 100.00\% | 8 |
| 506 | 479 | 69 | 3 | 1 | 0 | -100 | 22.3780 | 8.2513 | 191 | 64 | 39.87\% | 92.75\% | 100.00\% | 9 |

Table B．1．Computational results of the proposed algorithm．（cont．）

| U | $\bigcirc$ | $\infty$ | 0 | $\sigma$ | $の$ | 0 | $\infty$ | $\bigcirc$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | の | $\infty$ | $\infty$ | $\bigcirc$ | $\infty$ | $\infty$ | 0 | $\infty$ | 0 | $\theta$ | $\infty$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & \text { 合 } \\ & 0 \\ & \dot{0} \\ & \hline 0 \end{aligned}$ | $\begin{aligned} & 00 \\ & 0 \\ & 0 \\ & \dot{0} \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { OO } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { so } \\ & \text { ob } \\ & \stackrel{0}{0} \end{aligned}$ | $\begin{gathered} \circ \\ \infty \\ \stackrel{\circ}{\infty} \\ \dot{\infty} \end{gathered}$ | $\begin{aligned} & \stackrel{\circ}{\infty} \\ & \stackrel{\infty}{\infty} \\ & \stackrel{\infty}{\infty} \end{aligned}$ |  | $\begin{aligned} & \underset{\sim}{\infty} \\ & \underset{\sim}{\infty} \\ & \underset{\infty}{\infty} \end{aligned}$ | $\begin{gathered} \infty \\ \infty \\ \infty \\ \infty \\ \infty \\ \infty \end{gathered}$ |  |  | $\begin{array}{\|c} 00 \\ 0 \\ 0 \\ 0 \end{array}$ |  | $\begin{gathered} \stackrel{\circ}{\circ} \\ \stackrel{\circ}{\circ} \\ \stackrel{\circ}{\mathrm{i}} \end{gathered}$ | $\begin{aligned} & \text { So } \\ & \underset{\vdots}{6} \\ & \underset{O}{2} \end{aligned}$ |  | $\begin{aligned} & 00 \\ & \underset{\vdots}{0} \\ & \dot{\theta} \end{aligned}$ | $\begin{aligned} & \stackrel{\circ}{\circ} \\ & \stackrel{+}{\dot{6}} \\ & \dot{6} \end{aligned}$ | $\begin{array}{\|c} \substack{0 \\ \stackrel{y}{0} \\ \dot{\theta} \\ \hline} \end{array}$ | $\begin{aligned} & \text { so } \\ & \text { む } \\ & \underset{\sim}{\circ} \end{aligned}$ | $\begin{aligned} & \text { so } \\ & \text { No } \\ & \dot{\circ} \end{aligned}$ |  |  |
|  | $\begin{array}{\|c} 00 \\ N \\ N \\ \end{array}$ |  |  | $\begin{aligned} & \text { so } \\ & \stackrel{0}{\circ} \\ & \text { Ni } \end{aligned}$ | $\begin{aligned} & \text { oi } \\ & \stackrel{1}{N} \\ & \underset{\circ}{\circ} \end{aligned}$ | $\begin{aligned} & \text { ô } \\ & \text { N } \\ & \text { むi } \end{aligned}$ | $\begin{array}{\|c} 00 \\ N \\ N \\ \end{array}$ | $\begin{array}{\|c} \substack{0 \\ N \\ N \\ 1 \\ d \\ j} \end{array}$ |  |  | $$ |  | $\begin{aligned} & \text { so } \\ & \stackrel{0}{N} \\ & \underset{\text { in }}{ } \end{aligned}$ |  | $\begin{aligned} & \text { o̊ } \\ & \text { N } \\ & \text { Ni } \\ & \text { od } \end{aligned}$ |  | $\begin{array}{\|l} \text { 合 } \\ \stackrel{y}{0} \\ 1 \end{array}$ | $\begin{aligned} & \text { ô } \\ & \text { ले } \\ & \dot{\circ} \end{aligned}$ | $\begin{aligned} & \text { So } \\ & \text { M } \\ & \text { ju} \end{aligned}$ |  | 合 <br> $\vdots$ <br> $\vdots$ | $\begin{aligned} & \text { SO } \\ & \text { O} \\ & \stackrel{0}{0} \end{aligned}$ | So |
|  | $\left\|\begin{array}{c} 0 \\ 10 \\ \infty \\ 0 \\ 0 \end{array}\right\|$ | $\left\|\begin{array}{c} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{array}\right\|$ | $\left\lvert\, \begin{gathered} 0 \\ 0 \\ \infty \\ \infty \\ 0 \\ 0 \end{gathered}\right.$ | $\begin{aligned} & \circ 0 \\ & 0 \\ & \infty \\ & 0 \\ & 0 \end{aligned}$ | $\left.\begin{array}{\|c} 0 \\ 1 \\ \infty \\ 0 \\ 0 \end{array} \right\rvert\,$ | $\begin{gathered} \text { oo } \\ 0 \\ \infty \\ 0 \\ \hline \end{gathered}$ | $\begin{array}{\|c} \substack{0 \\ 1 \\ \infty \\ \infty \\ 0 \\ \hline} \end{array}$ | $\begin{array}{\|c} 00 \\ 0 \\ \infty \\ 0 \\ 0 \end{array}$ | $\begin{gathered} \text { o̊ } \\ 1 \\ \infty \\ 0 \\ \end{gathered}$ | $\left\lvert\, \begin{gathered} \substack{0 \\ 1 \\ \infty \\ 0 \\ 0 \\ 0} \end{gathered}\right.$ | $\begin{gathered} \text { oo } \\ 0 \\ \infty \\ \infty \\ \infty \end{gathered}$ | $\begin{aligned} & \text { ol } \\ & 1 \\ & \infty \\ & \infty \\ & 0 \\ & \end{aligned}$ | $\begin{aligned} & \text { oo } \\ & 0 \\ & \infty \\ & \infty \\ & \hline \end{aligned}$ | $\begin{aligned} & \circ \\ & \stackrel{\circ}{1} \\ & \infty \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { o̊ } \\ & 0 \\ & \infty \\ & \infty \\ & \infty \end{aligned}$ | $\begin{gathered} 00 \\ i \\ \infty \\ 0 \\ 0 \end{gathered}$ | $\begin{aligned} & \substack{\circ \\ 1 \\ \infty \\ \infty \\ \underset{\sim}{0} \\ \hline} \end{aligned}$ | $\begin{aligned} & 0 \\ & 0 \\ & \infty \\ & \infty \\ & 0 \\ & \hline \end{aligned}$ | $\begin{array}{\|c} \substack{0 \\ 1 \\ \infty \\ 0 \\ 0} \end{array}$ | $\begin{array}{\|c} \text { ol } \\ \hat{1} \\ \stackrel{\rightharpoonup}{\dot{~}} \end{array}$ | $\begin{aligned} & \text { かo } \\ & \infty \\ & \infty \\ & \dot{\infty} \end{aligned}$ | $\left\lvert\, \begin{gathered} \substack{0 \\ 0 \\ \infty \\ 0 \\ 0} \end{gathered}\right.$ |  |
|  | ぜ | ¢ | \＃ | ¢ | ¢ | 48 | \＃ | \＃ | 18 | \％ | \＃ | 4 | む | 4 | ¢ | 18 | 8 | 4 | 18 | 4 | $\stackrel{\square}{6}$ | 8 | \＃ |
|  | $\stackrel{\rightharpoonup}{9}$ | $\stackrel{\rightharpoonup}{9}$ | $\stackrel{\rightharpoonup}{9}$ | $\stackrel{\rightharpoonup}{9}$ | $\stackrel{\rightharpoonup}{9}$ | $\stackrel{\rightharpoonup}{9}$ | $\stackrel{\rightharpoonup}{9}$ | $\stackrel{\rightharpoonup}{9}$ | $\stackrel{\rightharpoonup}{9}$ | $\stackrel{\rightharpoonup}{9}$ | $\stackrel{\rightharpoonup}{7}$ | $\stackrel{3}{9}$ | $\stackrel{\rightharpoonup}{\square}$ | $\stackrel{\rightharpoonup}{9}$ | $\stackrel{\rightharpoonup}{\sigma}$ | $\stackrel{\rightharpoonup}{9}$ | $\stackrel{\rightharpoonup}{2}$ | $\stackrel{\rightharpoonup}{9}$ | $\stackrel{\square}{9}$ | $\stackrel{8}{9}$ | $\stackrel{\rightharpoonup}{9}$ | $\stackrel{\rightharpoonup}{9}$ | $\stackrel{\rightharpoonup}{9}$ |
|  |  | $\left\|\begin{array}{c} \infty \\ \underset{\sim}{0} \\ \underset{\sim}{\infty} \\ \infty \end{array}\right\|$ | $\begin{aligned} & \underset{\sim}{\infty} \\ & \stackrel{\rightharpoonup}{0} \\ & \underset{\sim}{\infty} \end{aligned}$ | $\begin{gathered} \stackrel{m}{10} \\ \stackrel{\sim}{1} \\ \infty \end{gathered}$ | $\left\|\begin{array}{c} 1 \\ 0 \\ 0 \\ 0 \\ \infty \end{array}\right\|$ | $\stackrel{\stackrel{10}{7}}{\stackrel{\infty}{\sim}}$ | $\begin{aligned} & \underset{\sim}{\otimes} \\ & \underset{\sim}{\circ} \\ & \underset{\infty}{2} \end{aligned}$ | $\left\|\begin{array}{c} o \\ 0 \\ 0 \\ 0 \\ \infty \end{array}\right\|$ |  | $\begin{aligned} & 9 \\ & \stackrel{9}{0} \\ & \stackrel{0}{1} \end{aligned}$ | $\stackrel{\text { ® }}{\stackrel{\text { ® }}{\stackrel{1}{1}}}$ | $\begin{aligned} & 0 \\ & \underset{7}{7} \\ & 1 \end{aligned}$ | $\stackrel{\stackrel{10}{6}}{\substack{-1 \\ \infty}}$ | $\begin{aligned} & \stackrel{\ddots}{\circ} \mathrm{e} \\ & \stackrel{e}{0} \\ & 1 \end{aligned}$ | $\begin{aligned} & \stackrel{8}{8} \\ & \infty \\ & \stackrel{\infty}{1} \end{aligned}$ | $\begin{array}{\|c} \hline 0 \\ \stackrel{y}{4} \\ \underset{~}{2} \end{array}$ | $\begin{gathered} \underset{\sim}{\infty} \\ \stackrel{\infty}{\infty} \\ \stackrel{p}{1} \end{gathered}$ | $\begin{aligned} & \infty \\ & \stackrel{20}{\infty} \\ & \underset{\sim}{1} \end{aligned}$ | $$ | $\stackrel{\substack{\tilde{N} \\ \underset{N}{n}\\}}{ }$ | $\begin{aligned} & \text { O} \\ & \underset{\sim}{1} \end{aligned}$ | $\begin{aligned} & 0 \\ & \underset{7}{7} \\ & \stackrel{8}{4} \end{aligned}$ |  |
|  |  | $\left\lvert\, \begin{aligned} & \infty \\ & \infty \\ & \bullet \\ & \stackrel{\rightharpoonup}{i} \\ & \stackrel{1}{2} \end{aligned}\right.$ | $\left\lvert\, \begin{gathered} \underset{\sim}{0} \\ \infty \\ \stackrel{\infty}{\dot{N}} \\ \mid \end{gathered}\right.$ | $\begin{aligned} & \stackrel{\rightharpoonup}{\mathrm{N}} \\ & \underset{\sim}{\mathrm{~N}} \end{aligned}$ | $\left\|\begin{array}{c} \stackrel{\rightharpoonup}{N} \\ \underset{~}{4} \\ \stackrel{\rightharpoonup}{1} \end{array}\right\|$ |  | $\begin{aligned} & \stackrel{O}{\hat{N}} \\ & \underset{\sim}{2} \\ & \dot{\sim} \end{aligned}$ |  | $\begin{gathered} \underset{\sim}{8} \\ \underset{1}{0} \\ \underset{\sim}{2} \end{gathered}$ |  |  |  | $\begin{aligned} & \stackrel{\circ}{0} \\ & \stackrel{\leftrightarrow}{\bullet} \\ & \stackrel{\sim}{1} \end{aligned}$ | $\left\lvert\, \begin{aligned} & \circ \\ & \stackrel{0}{0} \\ & \stackrel{1}{i} \\ & \text { in } \end{aligned}\right.$ |  | $\left\|\begin{array}{c} 0 \\ 0 \\ 1 \\ \underset{N}{1} \end{array}\right\|$ | $\left\lvert\, \begin{gathered} 0 \\ \underset{7}{1} \\ \underset{\sim}{2} \end{gathered}\right.$ |  | $\begin{aligned} & 0 \\ & 0 \\ & 0 \\ & \\ & \stackrel{1}{2} \end{aligned}$ | $\left\|\begin{array}{c} 0 \\ \underset{\sim}{1} \\ \infty \\ \underset{\sim}{i} \end{array}\right\|$ | $\begin{aligned} & \stackrel{\circ}{\circ} \\ & \stackrel{\rightharpoonup}{\circ} \\ & \stackrel{1}{1} \end{aligned}$ | $\left\lvert\, \begin{aligned} & 0 \\ & \stackrel{\rightharpoonup}{0} \\ & \infty \\ & \stackrel{\rightharpoonup}{\mathrm{~N}} \end{aligned}\right.$ | $\xrightarrow{\text { O}}$ |
| $\cdots$ | $\stackrel{8}{7}$ | $\underset{\substack{8 \\ \hline \\ \hline}}{ }$ | $\stackrel{8}{1}$ | $\underset{1}{8}$ | $\stackrel{8}{7}$ | $\underset{\substack{\circ \\ \hline}}{ }$ | $\stackrel{\otimes}{9}$ | $\stackrel{8}{9}$ | $\stackrel{8}{7}$ | $\underset{\sim}{8}$ | $\underset{\substack{8 \\ \hline}}{ }$ | $\underset{\substack{8 \\ \hline \\ \hline}}{ }$ | $\underset{1}{8}$ | $\stackrel{\underset{1}{7}}{8}$ | $\underset{7}{8}$ | $\underset{\substack{8 \\ \hline}}{2}$ | $\stackrel{\otimes}{7}$ | $\stackrel{\otimes}{1}$ | $\begin{array}{\|c} 8 \\ 1 \end{array}$ | $\underset{1}{8}$ | $\underset{7}{8}$ | $\underset{\substack{8 \\ \hline 1 \\ \hline}}{ }$ | $\stackrel{8}{1}$ |
|  | 0 | $\bigcirc$ | － | $\bigcirc$ | $\stackrel{\sim}{\square}$ | $\stackrel{\infty}{\sim}$ | $\stackrel{\infty}{\square}$ | $\stackrel{\infty}{\square}$ | $\stackrel{\infty}{\square}$ | ¢ | ¢ | 8 | \＆ | 8 | $\underset{\sim}{4}$ | $\mathbb{Z}$ | $\pm$ | $\underset{-}{\text { J }}$ | $\pm$ | ® | － | ® | ® |
|  | $\checkmark$ | $-$ | － | $-$ | $-$ | $-$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\rightarrow$ | － | $-$ | $-$ | $\checkmark$ | $\checkmark$ | $-$ | $\rightarrow$ | $\rightarrow$ | $-$ | $-$ | － |
| $\begin{aligned} & \text { 訁े } \\ & \text { たた } \\ & \text { だ } \end{aligned}$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ |
|  | g | 8 | 8 | 8 | ¢ 8 | 8 | ¢ 8 | 앙 | 8 | 앙 | 9 | 8 | 8 | 8 | ¢ 8 | 앙 | ¢ 8 | 8 | 8 | 8 | 8 | 8 | 8 |
|  | 8 | $\stackrel{8}{7}$ | $\stackrel{9}{9}$ | $\stackrel{8}{4}$ | $\stackrel{8}{7}$ | 9 | $\stackrel{8}{7}$ | $\stackrel{9}{4}$ | 8 | $\stackrel{9}{7}$ | $\stackrel{9}{4}$ | $\stackrel{8}{7}$ | 9 | 4 | 9 | $\stackrel{8}{4}$ | 8 | 8 | 8 | $\stackrel{8}{4}$ | 8 | $\stackrel{9}{9}$ | $\stackrel{9}{7}$ |
| 皆 | $\stackrel{\circ}{8}$ | $\stackrel{\infty}{\circ}$ | 앙 | $\frac{0}{20}$ | $\overline{2}$ | $\stackrel{1}{20}$ | $\begin{aligned} & \ddot{2} \\ & \end{aligned}$ | $\pi$ | $\begin{array}{\|l\|l} 10 \\ 20 \end{array}$ | $\stackrel{9}{20}$ | $\stackrel{1}{2}$ | $\left\|\begin{array}{c} \infty \\ 20 \end{array}\right\|$ | $\stackrel{9}{2}$ | $\stackrel{\sim}{0}$ | 근 | N | in | $\underset{\sim}{\sim}$ | 䫆 | $\left.\begin{array}{\|c} 0 \\ i 0 \end{array} \right\rvert\,$ | N | $\stackrel{\sim}{\circ}$ | 긍 |

Table B．1．Computational results of the proposed algorithm．（cont．）

| U | の | $\infty$ | $\infty$ | $\bigcirc$ | $\bigcirc$ | $\infty$ | の | $\bigcirc$ | 0 | $\bigcirc$ | $\bigcirc$ | $\infty$ | $\infty$ | $\square$ | $\infty$ | $\bigcirc$ | $\bigcirc$ | $\sigma$ | $\infty$ | o | $\bigcirc$ | $\infty$ | $\infty$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & \text { 合 } \\ & \text { 内 } \\ & \dot{\circ} \end{aligned}$ |  | $\begin{aligned} & \text { ઠి } \\ & \stackrel{\rightharpoonup}{9} \\ & \dot{\sim} \end{aligned}$ |  |  |  | $\begin{aligned} & \text { ol } \\ & \infty \\ & \infty \\ & \infty \\ & \end{aligned}$ | $\begin{aligned} & \text { ol } \\ & 0 \\ & \infty \\ & \dot{\infty} \end{aligned}$ | $\begin{array}{\|c} 00 \\ 1 \\ 0 \\ 0 \\ 0 \end{array}$ | $\begin{array}{\|c} \substack{0 \\ 1 \\ \infty \\ \infty \\ 0} \end{array}$ | $\begin{aligned} & \text { so } \\ & \hat{0} \\ & \infty \\ & \dot{c} \end{aligned}$ | $\begin{aligned} & \text { so } \\ & \infty \\ & \infty \\ & \text { ci } \end{aligned}$ |  | $\begin{aligned} & \text { so } \\ & \infty \\ & \infty \\ & \dot{\circ} \end{aligned}$ | $\begin{aligned} & \text { So } \\ & 0 \\ & \infty \\ & \dot{\sim} \end{aligned}$ | $\begin{aligned} & \text { ol } \\ & \stackrel{0}{0} \\ & \infty \\ & \dot{0} \end{aligned}$ |  |  | $\begin{aligned} & \text { が } \\ & \\ & \underset{\sim}{\circ} \end{aligned}$ |  | $\begin{aligned} & \text { SO } \\ & \AA \\ & \stackrel{\infty}{\circ} \end{aligned}$ | $\begin{aligned} & \infty \\ & \infty \\ & \infty \\ & \infty \end{aligned}$ | － |
|  | $\begin{array}{\|c} 80 \\ 0 \\ 0 \\ \hline 0 \\ 1 \end{array}$ | $\left\lvert\, \begin{array}{\|c\|c} \substack{0 \\ 0 \\ 0 \\ 0 \\ \hline \\ \hline} \end{array}\right.$ | $\begin{aligned} & \text { S0 } \\ & \text { N } \\ & \text { Oi } \end{aligned}$ | $\begin{aligned} & \text { B̀ } \\ & \text { ì } \\ & \text { ín } \end{aligned}$ | $\begin{gathered} \text { so } \\ \stackrel{1}{1} \\ \dot{O} \end{gathered}$ | $\begin{array}{\|l} 80 \\ \stackrel{0}{0} \\ 0 \\ 0 \end{array}$ | $\begin{aligned} & 00 \\ & 0.0 \\ & 0.0 \\ & 0.8 \end{aligned}$ |  | $\begin{array}{\|l\|l} 00 \\ 0 \\ 1 \\ 0 \end{array}$ | $\begin{gathered} \text { so } \\ \stackrel{y}{c} \\ \dot{O} \end{gathered}$ | $\begin{aligned} & \text { so } \\ & \stackrel{N}{i} \\ & \text { cid } \end{aligned}$ | $\begin{aligned} & \text { ô } \\ & \text { ì } \\ & \text { ji } \end{aligned}$ | $\begin{aligned} & \text { so } \\ & 6 . \\ & \stackrel{0}{0} \end{aligned}$ | $\begin{aligned} & \text { o̊ } \\ & \stackrel{1}{i} \\ & \text { ci } \end{aligned}$ | $\begin{aligned} & \text { ò } \\ & \stackrel{1}{1} \\ & \dot{O} \end{aligned}$ | $\begin{array}{\|c} 00 \\ \vdots \\ \vdots \\ 0 \end{array}$ | $\begin{aligned} & \text { LO} \\ & \stackrel{0}{6} \\ & \stackrel{1}{\circ} \end{aligned}$ |  | $\begin{aligned} & \text { 会 } \\ & \stackrel{0}{0} \end{aligned}$ | $\begin{gathered} \text { Ò } \\ \text { N} \\ \text { Oi } \end{gathered}$ | $\begin{aligned} & \text { so } \\ & \text { N } \\ & \text { ڭi } \end{aligned}$ | $\begin{aligned} & \text { 合 } \\ & \underset{\sim}{1} \end{aligned}$ | b̀ M Oid |
|  | $\begin{aligned} & \text { ol } \\ & 0 \\ & \infty \\ & \dot{\infty} \end{aligned}$ | $\left\|\begin{array}{c} 0 \\ 0 \\ \infty \\ 0 \\ 0 \\ 0 \end{array}\right\|$ | $\begin{array}{\|c} \substack{0 \\ 1 \\ \infty \\ 0 \\ 0} \end{array}$ | $\begin{aligned} & \text { so } \\ & 0 \\ & \infty \\ & 0 \\ & 0 \end{aligned}$ | $\begin{gathered} \substack{0 \\ 1 \\ \infty \\ \infty \\ 0 \\ \hline} \end{gathered}$ | $\begin{aligned} & \text { ol } \\ & \stackrel{0}{\infty} \\ & \infty \\ & \dot{\sim} \end{aligned}$ | $\begin{aligned} & 0 \\ & \stackrel{0}{6} \\ & 0 . \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { ol } \\ & \infty \\ & \infty \\ & \infty \\ & \infty \end{aligned}$ | $\begin{aligned} & \substack{8 \\ 1 \\ \infty \\ \infty \\ 0 \\ \\ \hline} \end{aligned}$ | $\begin{array}{\|l\|l} \substack{0 \\ 0 \\ \infty \\ 0 \\ 0} \end{array}$ | $\begin{aligned} & \text { so } \\ & \stackrel{0}{\infty} \\ & \infty \\ & \dot{\sim} \end{aligned}$ | $\begin{aligned} & \text { ơo } \\ & \stackrel{y}{\circ} \\ & \underset{\sim}{\circ} \end{aligned}$ | $\begin{aligned} & \text { o̊ } \\ & 1 \\ & \infty \\ & \dot{\infty} \end{aligned}$ |  | $\begin{aligned} & \text { so } \\ & \infty \\ & \infty \\ & \infty \\ & \dot{\infty} \end{aligned}$ | $\begin{array}{\|l\|l} \substack{0 \\ 0 \\ \infty \\ 0 \\ 0} \end{array}$ | $\begin{aligned} & \text { 九o } \\ & \stackrel{0}{0} \\ & \text {. } \end{aligned}$ |  | $\begin{aligned} & \text { so } \\ & \stackrel{0}{0} \\ & \text {. } \end{aligned}$ | $\begin{gathered} \text { O} \\ \stackrel{0}{0} \\ \dot{0} \end{gathered}$ |  | $\begin{aligned} & \text { ol } \\ & \stackrel{0}{\infty} \\ & \dot{\infty} \\ & \underset{\sim}{2} \end{aligned}$ | 合 |
|  | 8 | ¢ | 18 | 18 | 18 | 8 | 8 | 18 | $\stackrel{\leftarrow}{6}$ | 18 | \＃ | 48 | 8 | ¢ | 4.8 | $\stackrel{\leftarrow}{6}$ | $\stackrel{\square}{8}$ | \＃ | 8 | 48 | 18 | $\stackrel{\square}{6}$ | 4 |
|  | $\stackrel{\rightharpoonup}{\square}$ | $\stackrel{\rightharpoonup}{9}$ | $\stackrel{\rightharpoonup}{9}$ | $\stackrel{\rightharpoonup}{9}$ | $\stackrel{\rightharpoonup}{9}$ | $\stackrel{\rightharpoonup}{\square}$ | $\stackrel{8}{7}$ | $\stackrel{\rightharpoonup}{9}$ | $\stackrel{\rightharpoonup}{9}$ | $\stackrel{\rightharpoonup}{9}$ | $\stackrel{\rightharpoonup}{9}$ | $\stackrel{\infty}{\sim}$ | $\stackrel{\rightharpoonup}{9}$ | $\underset{\sim}{\otimes}$ | $\stackrel{\rightharpoonup}{\square}$ | $\stackrel{\rightharpoonup}{9}$ | $\stackrel{\circ}{9}$ | $\stackrel{\otimes}{\infty}$ | $\stackrel{8}{9}$ | $\stackrel{8}{9}$ | $\stackrel{\rightharpoonup}{9}$ | $\stackrel{\rightharpoonup}{\square}$ | $\stackrel{8}{9}$ |
|  | $\begin{gathered} \underset{i}{i} \\ \dot{\infty} \\ \dot{O} \end{gathered}$ | $\left\|\begin{array}{c} \infty \\ \infty \\ \underset{y}{0} \\ \dot{0} \end{array}\right\|$ | $\begin{aligned} & \infty \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ |  | $\begin{gathered} \mathrm{I} \\ \underset{7}{7} \\ \underset{1}{2} \end{gathered}$ |  | $\begin{gathered} \infty \\ \stackrel{\infty}{0} \\ \underset{\sim}{0} \end{gathered}$ | $\left\|\begin{array}{c} \underset{8}{0} \\ \vdots \\ 1 \\ 1 \end{array}\right\|$ | $\begin{gathered} \infty \\ \stackrel{\infty}{\oplus} \\ \stackrel{\sim}{\circ} \\ \hline \end{gathered}$ | $\begin{aligned} & \underset{Z}{Z} \\ & \substack{0 \\ 0} \end{aligned}$ | $\begin{aligned} & 1 \\ & \substack{2 \\ \\ 0} \end{aligned}$ | $\begin{aligned} & \underset{\infty}{\boldsymbol{\infty}} \\ & \underset{\circ}{6} \end{aligned}$ | $\begin{gathered} \underset{\sim}{\underset{N}{2}} \\ \underset{广}{\circ} \end{gathered}$ | $\begin{gathered} \underset{N}{N} \\ \underset{\sim}{0} \end{gathered}$ | $\begin{aligned} & \text { R } \\ & \stackrel{\text { in }}{\stackrel{1}{6}} \end{aligned}$ | $$ | $\begin{aligned} & \text { 오 } \\ & \stackrel{1}{1} \\ & \stackrel{1}{1} \end{aligned}$ | $\begin{aligned} & \underset{\mathrm{O}}{\mathrm{O}} \\ & \text { in } \end{aligned}$ | $\begin{aligned} & \underset{\sim}{\mathrm{N}} \\ & \text { ¢ } \end{aligned}$ |  | $\begin{aligned} & \substack{\infty \\ \underset{\sim}{c} \\ \\ \hline} \end{aligned}$ |  | ¢ |
|  | $\begin{aligned} & \stackrel{8}{4} \\ & \underset{\sim}{1} \\ & \underset{\sim}{2} \end{aligned}$ | $\left\|\begin{array}{c} 0 \\ \\ \stackrel{\infty}{1} \\ \underset{\sim}{2} \end{array}\right\|$ |  |  | $\left\|\begin{array}{l} \stackrel{O}{1} \\ \stackrel{1}{0} \\ \underset{i}{v} \end{array}\right\|$ |  |  | $\left\|\begin{array}{c} O \\ \underset{1}{2} \\ \underset{\sim}{\dot{N}} \end{array}\right\|$ | $\begin{aligned} & 0 \\ & 0 \\ & \\ & \\ & \stackrel{1}{2} \end{aligned}$ | $\left.\begin{array}{\|l\|} \hline \\ \stackrel{0}{0} \\ \stackrel{3}{2} \\ \stackrel{~}{2} \end{array} \right\rvert\,$ | $\begin{aligned} & \stackrel{0}{0} \\ & \stackrel{1}{9} \\ & \stackrel{1}{i} \end{aligned}$ | $\begin{aligned} & \circ \\ & \ddot{\circ} \\ & \stackrel{\circ}{\circ} \\ & \stackrel{1}{\mathrm{~N}} \end{aligned}$ |  |  | $\begin{aligned} & \stackrel{\circ}{\circ} \\ & \stackrel{y}{0} \\ & \underset{N}{N} \end{aligned}$ | $\left\|\begin{array}{c} \circ \\ \underset{\sim}{\mathrm{N}} \\ \underset{\sim}{\mathrm{~N}} \end{array}\right\|$ | $\begin{aligned} & \stackrel{\circ}{\circ} \\ & \stackrel{0}{2} \\ & \stackrel{\rightharpoonup}{\mathrm{~N}} \end{aligned}$ |  |  | $\begin{gathered} \text { B } \\ \text { N } \\ \text { N } \\ \text { N } \end{gathered}$ |  | $\begin{aligned} & \text { 俞 } \\ & \text { N } \\ & \text { Ni } \end{aligned}$ | ® ¢ ¢ ล̀ |
| 法 莫 | $\underset{1}{8}$ | $\stackrel{8}{9}$ | $\underset{\substack{8 \\ \hline}}{ }$ | $\stackrel{8}{7}$ | $\stackrel{8}{9}$ | $\stackrel{\underset{1}{0}}{\substack{1}}$ | $\underset{1}{8}$ | $\stackrel{8}{9}$ | $\underset{\substack{8 \\ \hline}}{ }$ | $\underset{1}{8}$ | $\underset{7}{8}$ | $\underset{\substack{8 \\ \hline}}{2}$ | $\stackrel{8}{1}$ | $\underset{i}{8}$ | $\stackrel{8}{9}$ | $\underset{\substack{8 \\ \hline \\ \hline}}{ }$ | $\underset{7}{8}$ | $\underset{\substack{8 \\ \hline}}{2}$ | $\underset{-1}{8}$ | $\stackrel{8}{7}$ | $\stackrel{8}{7}$ | $\stackrel{8}{7}$ | $\stackrel{8}{4}$ |
|  | $\stackrel{\text { ® }}{\text { ® }}$ | $\left\|\begin{array}{c} \underset{\sim}{2} \end{array}\right\|$ | $\begin{array}{\|c\|} \hline \\ \underset{N}{2} \end{array}$ | $\begin{aligned} & \underset{\sim}{9} \\ & \text { an } \end{aligned}$ | $\left\|\begin{array}{c} 9 \\ \underset{N}{2} \end{array}\right\|$ | $\begin{array}{\|c} 9 \\ \mathrm{~N} \end{array}$ | $\underset{\sim}{\infty}$ | $\left\|\begin{array}{c} \infty \\ \underset{\sim}{\infty} \end{array}\right\|$ | $\left.\begin{array}{\|c\|c} \infty \\ \underset{\sim}{\infty} \end{array} \right\rvert\,$ | $\stackrel{\infty}{\infty} \underset{\sim}{\infty}$ | $\left\|\begin{array}{c} \infty \\ \underset{\sim}{\infty} \end{array}\right\|$ | $\stackrel{\circ}{\circ}$ | $\stackrel{\circ}{\circ}$ | $\stackrel{\circ}{\circ}$ | $\stackrel{\circ}{\infty}$ | $\ddot{\circ}$ | $\underset{\infty}{+\infty}$ | $\underset{\infty}{+\infty}$ | － | $\underset{\infty}{\infty}$ | － | \％ | ※ |
| نِ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $-$ | $\sim$ | $\cdots$ | $\cdots$ | $-$ | $-$ | $-$ | $\rightarrow$ | － | － | $-$ | $\checkmark$ | $\rightarrow$ | － | $-$ | $\rightarrow$ | － | $-$ | $-$ | $-$ |
| $\begin{aligned} & \stackrel{\rightharpoonup}{\mathrm{N}} \\ & \text { た } \\ & \text { だ } \end{aligned}$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ |
|  | 8 | 8 | 8 | 8 | 8 | 8 | 9 | 앙 | 8 | 8 | 8 | 8 | 8 | 8 | 8 | 8 | 8 | 8 | 8 | 앙 | 8 | 8 | 앙 |
|  | 8 | $\stackrel{8}{4}$ | $\stackrel{9}{7}$ | $\stackrel{8}{4}$ | 8 | 9 | 9 | $\stackrel{9}{4}$ | 8 | $\stackrel{8}{4}$ | 8 | 8 | $\stackrel{8}{4}$ | $\stackrel{8}{7}$ | 8 | $\stackrel{8}{4}$ | 4 | 8 | $\stackrel{8}{7}$ | $\stackrel{9}{7}$ | $\stackrel{8}{4}$ | $\stackrel{8}{4}$ | $\stackrel{9}{7}$ |
|  | \％ | 告 | 资 | $\underset{i}{\infty}$ | $\underset{\sim}{n}$ | $\begin{array}{\|l\|} \hline 8 \\ 8 \\ 8 \end{array}$ | $\ddot{\sim}$ | $\stackrel{r}{0}$ | $\begin{array}{\|c} \infty \\ \\ \end{array}$ | R | $\left.\begin{array}{\|c} 9 \\ 40 \end{array} \right\rvert\,$ | $\underset{10}{7}$ | $\stackrel{\text { ¢ }}{1}$ | $\left\lvert\, \begin{gathered} \underset{1}{2} \\ \hline \end{gathered}\right.$ | $\underset{\substack{7 \\ \hline}}{ }$ | $\left.\begin{array}{\|c\|c\|} \hline 98 \\ 48 \end{array} \right\rvert\,$ | $\left.\begin{array}{\|c\|} \hline 0 \\ 40 \end{array} \right\rvert\,$ | $\stackrel{\rightharpoonup}{4}$ | $\underset{\substack{\infty \\ 0 \\ \hline}}{ }$ | $\stackrel{8}{4}$ | 号 | 菏 | N |

Table B．1．Computational results of the proposed algorithm．（cont．）

| U | の | $\infty$ | $\sigma$ | 0 | $\bigcirc$ | $\bigcirc$ | の | $\infty$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | 9 | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | 9 | $\bigcirc$ | 앙 | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & \stackrel{\rightharpoonup}{\circ} \\ & \infty \\ & \infty \\ & \hline \end{aligned}$ | $\left\|\begin{array}{c} 0 \\ \stackrel{\rightharpoonup}{\infty} \\ \infty \\ \hline \end{array}\right\|$ | $\begin{aligned} & \Delta 0 \\ & \infty \\ & \infty \\ & \dot{\omega} \end{aligned}$ | $\begin{aligned} & \text { so } \\ & \stackrel{0}{0} \\ & 0 . \end{aligned}$ | $\left\|\begin{array}{l} 00 \\ 0 \\ 0 \\ 0 \end{array}\right\|$ | $\begin{array}{\|c} 00 \\ 0 \\ 0 \\ 0 \end{array}$ | $\begin{aligned} & 00 \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & 00 \\ & 0 \\ & 0 . \\ & 0 . \end{aligned}$ | $\begin{aligned} & \text { so } \\ & \text { © } \\ & \text { O} \end{aligned}$ | $\begin{aligned} & \text { of } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { ô } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { so } \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { 合 } \\ & 0 \\ & \dot{0} \\ & \hline 0 \end{aligned}$ | $\begin{aligned} & \text { so } \\ & \text { ob } \\ & \stackrel{0}{6} \end{aligned}$ | $\begin{aligned} & \text { ờ } \\ & \text { O. } \\ & \text { O} \end{aligned}$ | $\begin{aligned} & \text { so } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { oi } \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { ồ } \\ & \stackrel{0}{0} \\ & 0 \end{aligned}$ | $\begin{aligned} & 0.0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { so } \\ & \text { ob } \\ & \stackrel{0}{6} \end{aligned}$ | $\begin{aligned} & \text { ob } \\ & \text { ob } \\ & \text { B. } \end{aligned}$ |  | 80 O－ O－ |
|  |  | $\left\lvert\, \begin{array}{\|c} \substack{0 \\ N \\ N \\ i \\ j \\ \hline} \end{array}\right.$ | $\begin{aligned} & \text { So } \\ & \text { N } \\ & \text { ڭi } \end{aligned}$ | $\begin{aligned} & \text { so } \\ & \stackrel{0}{\circ} \\ & \text { Ni } \end{aligned}$ | $\begin{array}{\|c} \substack{0 \\ N \\ N \\ i \\ d} \end{array}$ | $\begin{array}{\|c} \substack{0 \\ N \\ N \\ \hat{1} \\ \mathrm{j} \\ \hline} \end{array}$ | $\begin{array}{\|c} 00 \\ N \\ N \\ \end{array}$ | $\begin{aligned} & \text { so } \\ & \stackrel{0}{N} \\ & \dot{N} \\ & \text { d } \end{aligned}$ | $\begin{aligned} & \text { ol } \\ & \stackrel{1}{0} \\ & \text { di } \end{aligned}$ | $\begin{aligned} & \text { 合 } \\ & \mathrm{N} \\ & \mathrm{~N} \\ & \mathrm{o} \end{aligned}$ | $$ | $\begin{aligned} & \text { oo } \\ & \text { 只 } \\ & \text { di } \\ & \text { o } \end{aligned}$ | $\begin{array}{\|c} 00 \\ N \\ N \\ \end{array}$ |  | $\begin{aligned} & \text { o̊ } \\ & \text { N } \\ & \text { Ni } \\ & \text { od } \end{aligned}$ | $\begin{aligned} & \text { oo } \\ & \stackrel{0}{0} \\ & \underset{1}{\mathrm{o}} \end{aligned}$ | $\begin{aligned} & \text { o̊ } \\ & \stackrel{1}{0} \\ & \text { A. } \\ & \text { of } \end{aligned}$ | $\begin{aligned} & \text { o̊ } \\ & \stackrel{0}{N} \\ & \text { ㅅㅇ } \end{aligned}$ | $\left.\begin{array}{\|c} S O \\ N \\ 0 \\ i \end{array} \right\rvert\,$ | $\begin{aligned} & 80 \\ & N \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { so } \\ & \underset{N}{2} \end{aligned}$ | $\begin{aligned} & s 0 \\ & N \\ & \underset{\sim}{\circ} \end{aligned}$ | － |
|  | $\left\|\begin{array}{c} 0 \\ 10 \\ \infty \\ 0 \\ 0 \end{array}\right\|$ | $\left\|\begin{array}{c} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{array}\right\|$ | $\begin{aligned} & \text { Bo } \\ & \dot{0} \\ & \dot{0} \end{aligned}$ | $\begin{array}{\|c} \substack{0 \\ \stackrel{1}{0} \\ \underset{\sim}{\circ} \\ \hline} \end{array}$ | $\begin{array}{\|c} 00 \\ 10 \\ 0 \\ 0 \\ \underset{\sim}{2} \end{array}$ | $\begin{array}{\|c} \substack{0 \\ 0 \\ 0 \\ 0 \\ 0\\ } \end{array}$ | $\begin{aligned} & \text { ol } \\ & \text { N } \\ & \text { Non } \end{aligned}$ | $\begin{aligned} & \text { ol } \\ & \stackrel{0}{0} \\ & \underset{\sim}{\circ} \end{aligned}$ | $\begin{aligned} & \text { oి } \\ & \infty \\ & \infty \\ & \text { oj } \end{aligned}$ | $\left\lvert\, \begin{gathered} 0 \\ 1 \\ \infty \\ 0 \\ 0 \end{gathered}\right.$ | $\begin{gathered} \text { oo } \\ 0 \\ \infty \\ \infty \\ \infty \end{gathered}$ | $\begin{aligned} & \text { o̊ } \\ & \text { م } \\ & \infty \\ & \dot{\infty} \end{aligned}$ | $\begin{array}{\|c} \substack{0 \\ 1 \\ \infty \\ \infty \\ 0 \\ \hline} \end{array}$ | $\begin{aligned} & \circ \\ & \stackrel{\circ}{1} \\ & \infty \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { o̊ } \\ & 0 \\ & \infty \\ & \infty \\ & \infty \end{aligned}$ | $\begin{gathered} 00 \\ i \\ \infty \\ 0 \\ 0 \end{gathered}$ | $\begin{aligned} & \text { ol } \\ & \stackrel{0}{\infty} \\ & \infty \\ & \dot{\sim} \end{aligned}$ | $\begin{aligned} & 0 \\ & 0 \\ & \infty \\ & \infty \\ & 0 \\ & \hline \end{aligned}$ | $\begin{array}{\|c} \substack{0 \\ e \\ 0 \\ 0 \\ 0} \end{array}$ | $\begin{aligned} & \text { se } \\ & 0 \\ & \text { ei } \\ & \text { on } \end{aligned}$ | $\begin{aligned} & \text { so } \\ & \text { 厄i } \\ & \text { oi } \end{aligned}$ | $\begin{array}{\|c} \substack{0 \\ 0 \\ 0 \\ 0 \\ 0} \end{array}$ | coio |
|  | 48 | ¢ | 48 | ¢ | \＃ | \＃ | \＃ | \％ | ¢ | ¢ | \＃ | \＃ | \＃ | ¢ | ¢ | \＃ | \＃ | む | 绍 | 15 | 沼 | 뇽 | $\stackrel{18}{18}$ |
|  | $\stackrel{\rightharpoonup}{9}$ | $\stackrel{\otimes}{\sim}$ | $\stackrel{\otimes}{\sim}$ | $\underset{\sim}{\infty}$ | $\stackrel{\infty}{\sim}$ | $\stackrel{\infty}{\infty}$ | $\begin{aligned} & \infty \\ & \infty \\ & \sim \end{aligned}$ | $\begin{aligned} & \infty \\ & \infty \end{aligned}$ | $\stackrel{\rightharpoonup}{\square}$ | $\stackrel{\rightharpoonup}{9}$ | $\stackrel{\rightharpoonup}{7}$ | $\stackrel{\rightharpoonup}{7}$ | $\stackrel{\rightharpoonup}{9}$ | $\stackrel{\rightharpoonup}{9}$ | $\stackrel{\rightharpoonup}{\sigma}$ | $\underset{\sim}{9}$ | $\stackrel{\rightharpoonup}{9}$ | $\stackrel{\rightharpoonup}{9}$ | $\stackrel{10}{9}$ | $\stackrel{10}{\sim}$ | 适 | $\stackrel{18}{2}$ | $\stackrel{18}{\sim}$ |
|  | $\left\lvert\, \begin{aligned} & \text { H } \\ & \stackrel{1}{0} \\ & \dot{0} \end{aligned}\right.$ | $\left\|\begin{array}{c} \tilde{N} \\ \underset{\sim}{e} \\ \underset{o}{2} \end{array}\right\|$ | $\begin{aligned} & \otimes \infty \\ & \infty \\ & \infty \\ & \infty \\ & \dot{\circ} \end{aligned}$ | $\begin{aligned} & \text { Lo } \\ & 0 \\ & 0 \\ & 0 \\ & \\ & \hline 1 \end{aligned}$ | $\begin{aligned} & 10 \\ & 0 \\ & 0 \\ & 0 \\ & i \\ & 10 \end{aligned}$ | $\begin{aligned} & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & 10 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 10 \end{aligned}$ | $\begin{aligned} & 10 \\ & 0 \\ & 0 \\ & 0 \\ & i \\ & i \end{aligned}$ | $\begin{aligned} & \infty \\ & \stackrel{\infty}{\circ} \\ & \stackrel{\sim}{=} \\ & = \end{aligned}$ | $\begin{gathered} \infty \\ \stackrel{\infty}{0} \\ \stackrel{1}{=} \\ \underset{\sim}{2} \end{gathered}$ | $\begin{aligned} & \infty \\ & \stackrel{\infty}{\circ} \\ & \underset{\sim}{-} \\ & \hline \end{aligned}$ | $\begin{aligned} & \stackrel{\infty}{\stackrel{\circ}{\circ}} \\ & \stackrel{1}{=} \\ & \hline \end{aligned}$ | $\begin{aligned} & \infty \\ & \underset{\sim}{0} \\ & \underset{\sim}{9} \\ & = \end{aligned}$ | $\begin{gathered} \underset{\sim}{\underset{\infty}{\infty}} \\ \underset{\sim}{\dot{~}} \end{gathered}$ |  | $\begin{gathered} \underset{\sim}{\underset{\sim}{\alpha}} \\ \underset{\sim}{\dot{~}} \end{gathered}$ | $\begin{aligned} & \underset{\sim}{\underset{\sim}{\infty}} \\ & \underset{\sim}{\dot{I}} \end{aligned}$ | $\begin{aligned} & \stackrel{\rightharpoonup}{0} \\ & \underset{\sim}{\infty} \\ & \underset{\sim}{1} \end{aligned}$ | $\left\|\begin{array}{l} \underset{1}{\hat{1}} \\ \infty \\ \infty \\ \underset{\sim}{\infty} \end{array}\right\|$ | $\left\|\begin{array}{c} 0 \\ \underset{\infty}{\infty} \\ \infty \\ \underset{\infty}{\infty} \end{array}\right\|$ | $\begin{aligned} & 0 \\ & \underset{\infty}{\infty} \\ & \underset{\sim}{\infty} \end{aligned}$ | $\left\lvert\, \begin{aligned} & 0 \\ & \hat{1} \\ & \infty \\ & \infty \\ & \infty \end{aligned}\right.$ | $\begin{aligned} & 0 \\ & 1 \\ & \infty \\ & \infty \\ & \infty \end{aligned}$ |
|  |  | $\left\lvert\, \begin{aligned} & \mathrm{O} \\ & \mathrm{O} \\ & \mathrm{O} \\ & \text { ̇ㅓ } \end{aligned}\right.$ | $\begin{aligned} & \text { ه} \\ & \underset{\text { N}}{1} \\ & \text { N } \end{aligned}$ |  | $\left\|\begin{array}{c} 0 \\ \stackrel{0}{0} \\ \stackrel{0}{0} \\ \dot{i} \end{array}\right\|$ | $\left\lvert\, \begin{aligned} & 0 \\ & \underset{\substack{0 \\ ~}}{\text { i }} \end{aligned}\right.$ | $\begin{array}{r} \underset{\sim}{\circ} \\ \infty \\ \infty \\ \underset{\sim}{\dot{N}} \end{array}$ |  | $\begin{aligned} & \substack{0 \\ \infty \\ 0 \\ \underset{\sim}{c} \\ \underset{\sim}{c} \\ \hline} \end{aligned}$ |  | $\begin{aligned} & \stackrel{\circ}{\circ} \\ & \stackrel{0}{4} \\ & \underset{\sim}{\mathrm{~N}} \end{aligned}$ | $\begin{aligned} & \stackrel{\circ}{0} \\ & \stackrel{\rightharpoonup}{M} \\ & \stackrel{\rightharpoonup}{N} \\ & \hline \end{aligned}$ |  | $\left.\begin{gathered} \infty \\ \infty \\ \\ \underset{\sim}{1} \\ \underset{\sim}{2} \end{gathered} \right\rvert\,$ | $\begin{aligned} & \stackrel{\circ}{0} \\ & \infty \\ & \\ & \stackrel{N}{N} \end{aligned}$ | $\left\|\begin{array}{c} 0 \\ \hat{N} \\ 0 \\ \vdots \\ \underset{\sim}{n} \end{array}\right\|$ | $\begin{gathered} \infty \\ \otimes \\ \underset{\sim}{4} \\ \underset{\sim}{1} \end{gathered}$ | $\begin{aligned} & \stackrel{\rightharpoonup}{1} \\ & \hat{6} \\ & \stackrel{\sim}{\mathrm{~N}} \end{aligned}$ | $\begin{array}{\|c} \stackrel{\rightharpoonup}{0} \\ \stackrel{\sim}{e} \\ \stackrel{\sim}{0} \end{array}$ | $\left\|\begin{array}{l} \stackrel{\circ}{0} \\ \stackrel{1}{0} \\ \stackrel{\circ}{0} \end{array}\right\|$ | $\begin{aligned} & 0 \\ & \stackrel{\rightharpoonup}{0} \\ & \underset{\sim}{\circ} \\ & \stackrel{\sim}{1} \end{aligned}$ |  | － |
| 法 | $\stackrel{8}{9}$ | $\underset{\substack{8 \\ \hline \\ \hline}}{ }$ | $\underset{\substack{8 \\ \hline}}{ }$ | $\stackrel{8}{1}$ | $\underset{\substack{8 \\ \hline \\ \hline}}{ }$ | $\begin{aligned} & 0 \\ & \vdots \\ & \hline \end{aligned}$ | $\underset{1}{8}$ | $\underset{-1}{8}$ | $\stackrel{\text { ¢ }}{1}$ | $\stackrel{\text { ® }}{\substack{1}}$ | $\stackrel{\text { ¢ }}{\substack{1}}$ | $\stackrel{\text { ¢ }}{+}$ | ¢ | $\stackrel{\square}{7}$ | $\bigcirc$ | $\stackrel{1}{7}$ | $\stackrel{\square}{1}$ | $\stackrel{1}{1}$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | － | $\bigcirc$ |
|  | ～ั | $\stackrel{\sim}{\mathscr{f}} \mid$ | ก | $8$ | $\stackrel{8}{4}$ | $\stackrel{1}{4}$ | $\stackrel{9}{4}$ | $\stackrel{9}{7}$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | － | $\bigcirc$ | 0 | $\bigcirc$ | $\bigcirc$ | 0 | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | － | $\bigcirc$ |
|  | $\checkmark$ | $\checkmark$ | $-$ | $-$ | $\checkmark$ | $\checkmark$ | $\rightarrow$ | $\checkmark$ | $-$ | $-$ | $\checkmark$ | $-$ | $\rightarrow$ | $\checkmark$ | $-$ | $\checkmark$ | $\checkmark$ | $-$ | $-$ | $\rightarrow$ | $\checkmark$ | $-$ | － |
| $\begin{aligned} & \text { 訁े } \\ & \text { たた } \\ & \text { だ } \end{aligned}$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ |
|  | g | ¢ 8 | 8 | 8 | 8 | 8 | 앙 | 앙 | 8 | 8 | 8 | 8 | 앙 | ¢ | ¢ 8 | 8 | 8 | 8 | 8 | 8 | 8 | 8 | 8 |
|  | 8 | 8 | 8 | $\stackrel{8}{4}$ | 8 | $\stackrel{8}{4}$ | $\stackrel{9}{7}$ | 9 | 4 | 8 | $\stackrel{8}{4}$ | $\stackrel{8}{7}$ | $\stackrel{9}{4}$ | 8 | 9 | $\stackrel{9}{7}$ | 8 | 8 | 8 | $\stackrel{8}{4}$ | 8 | $\stackrel{9}{9}$ | $\stackrel{9}{7}$ |
| 皆 | 濄 | 令 | 迢 | $\begin{aligned} & \circ \\ & \stackrel{0}{n} \end{aligned}$ | 合 | ${ }_{0}^{\infty}$ | 尔 | 앙 | $\stackrel{\rightharpoonup}{6}$ | 앙 | : | 合 | $\stackrel{18}{8}$ | ¢ | $\begin{aligned} & \text { 合 } \end{aligned}$ | $\stackrel{\infty}{\circ}$ | 8 | 앙 | N | $\stackrel{N}{N}$ | $\stackrel{9}{0}$ | 去 | $1 \stackrel{10}{5}$ |

Table B．1．Computational results of the proposed algorithm．（cont．）

| U | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | 9 | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & \text { 合 } \\ & 0 \\ & \dot{0} \\ & \hline 0 \end{aligned}$ | $\begin{aligned} & 00 \\ & 0 \\ & 0 \\ & \dot{0} \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { so } \\ & \text { © } \\ & \text { O} \end{aligned}$ | $\begin{aligned} & \text { so } \\ & \text { ob } \\ & \stackrel{0}{0} \end{aligned}$ |  |  | $\begin{aligned} & \text { 合 } \\ & 0 \\ & \dot{0} \\ & \hline 0 \end{aligned}$ | $\begin{aligned} & \text { so } \\ & 0 . \\ & 0 . \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { ô } \\ & \text { O} \\ & \text { O} \end{aligned}$ | $\begin{aligned} & \text { ồ } \\ & 0 \\ & 0 . \\ & 0 . \end{aligned}$ | $\begin{aligned} & 00 \\ & 0 \\ & 0 \\ & \dot{O} \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { so } \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { 合 } \\ & 0 \\ & \dot{0} \\ & \hline 0 \end{aligned}$ | $\begin{aligned} & \text { so } \\ & \text { ob } \\ & \stackrel{0}{0} \end{aligned}$ | $\begin{aligned} & \text { ô } \\ & \text { O} \\ & \text { O} \end{aligned}$ | $\begin{aligned} & 00 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { oi } \\ & 0 \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { ờ } \\ & 0 \\ & 0 . \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { oi } \\ & 0 \\ & 0 \\ & \dot{0} \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { so } \\ & \text { ob } \\ & \stackrel{0}{0} \end{aligned}$ | $\begin{aligned} & \text { ob } \\ & \text { ob } \\ & \text { B } \end{aligned}$ |  | $\begin{aligned} & \text { ồ } \\ & \text { ó } \\ & \text { O} \end{aligned}$ |
|  | $\begin{aligned} & \text { ge } \\ & \text { N} \\ & \text { No } \end{aligned}$ | $\left\lvert\,\right.$ | $\begin{aligned} & \text { SO } \\ & \text { Ǹ } \\ & \text { Hi } \end{aligned}$ | $\begin{aligned} & \text { ôo } \\ & \text { N̦ } \\ & \text { İ } \end{aligned}$ |  | $\begin{aligned} & \text { が } \\ & \text { స్ } \\ & \text { io } \end{aligned}$ |  |  |  |  | $\begin{array}{\|l\|} \hline \stackrel{\circ}{\circ} \\ \text { en } \\ \text { ¢ } \end{array}$ |  |  |  |  | $\begin{gathered} \text { ol } \\ \text { ò } \\ \text { ci } \end{gathered}$ |  |  | $\begin{aligned} & \text { go } \\ & \text { సे } \\ & \text { Nे } \end{aligned}$ |  | $\begin{aligned} & \text { 俞 } \\ & \text { y } \end{aligned}$ | $\begin{aligned} & \text { 合 } \\ & \stackrel{y}{4} \\ & \stackrel{y}{2} \end{aligned}$ | － |
|  | $\begin{aligned} & \text { ô } \\ & \text { ö } \\ & \text { Oi } \end{aligned}$ | $\left\|\right\|$ |  |  | $\begin{array}{\|l\|} \substack{0 \\ 0 \\ \overparen{0} \\ \stackrel{0}{2}} \end{array}$ | $\begin{aligned} & \text { が } \\ & \stackrel{\rightharpoonup}{\mathrm{N}} \\ & \text { ì } \end{aligned}$ |  |  | $\begin{aligned} & \stackrel{\circ}{\circ} \\ & \underset{\mathrm{N}}{1} \\ & \stackrel{\rightharpoonup}{\mathrm{~N}} \end{aligned}$ | $\left\lvert\, \begin{gathered} 0 \\ \substack{0 \\ 0 \\ \text { N } \\ \text { in }} \end{gathered}\right.$ | $\begin{array}{\|c} \substack{0 \\ \\ \stackrel{\rightharpoonup}{\mathrm{j}} \\ \hline} \end{array}$ |  |  | $\begin{array}{\|c} \substack{0 \\ \vdots \\ \underset{\sim}{c} \\ \underset{\sim}{2}} \end{array}$ | $\begin{aligned} & \text { ôo } \\ & \stackrel{\rightharpoonup}{\mathrm{o}} \\ & \underset{\mathrm{j}}{ } \end{aligned}$ | $\begin{aligned} & 00 \\ & \stackrel{0}{0} \\ & \stackrel{6}{6} \end{aligned}$ | $\begin{array}{\|c\|} \hline 0 \\ 00 \\ 0 \\ 0 \\ \hline \end{array}$ | $\begin{array}{\|c\|} \hline 0 \\ 0 \\ 0 \\ 0 \\ \hline \end{array}$ | $\begin{aligned} & 00 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\left\lvert\, \begin{gathered} 00 \\ 0 \\ 0 \\ 0 \\ \hline \end{gathered}\right.$ | $\begin{aligned} & \text { So } \\ & \stackrel{\rightharpoonup}{\mathrm{N}} \end{aligned}$ | $\begin{gathered} \mathrm{So}_{1}^{\mathrm{N}} \\ \mathrm{i} \end{gathered}$ | So |
|  | $\stackrel{18}{4}$ | 18 | 18 | 18 | 18 | 7 | 7 | 7 | 7 | 7 | ๙ | คั | $\stackrel{\square}{\sim}$ | ค | ค | $\pm$ | $\pm$ | ゴ | $\underset{\sim}{-1}$ | J゙ | 15 | 10 | 15 |
|  | $\stackrel{\stackrel{\sim}{\mathrm{a}}}{ }$ | $\stackrel{\sim}{-}$ | $\stackrel{\circ}{-1}$ | $\stackrel{\circ}{9}$ | $\stackrel{\sim}{-}$ | $\stackrel{\sim}{\square}$ | $\stackrel{\rightharpoonup}{0}$ | $\stackrel{\rightharpoonup}{0}$ | $\stackrel{\rightharpoonup}{-1}$ | $\stackrel{1}{-1}$ | 앙 | 용 | 8 | $\bigcirc$ | 앙 | กั | ¢ | ํㅏㅇ | ¢ | ¢ | $\because$ | $\because$ | $\stackrel{1}{7}$ |
|  | $\begin{aligned} & 0 \\ & 0 \\ & 0 \\ & 0 \\ & \stackrel{0}{0} \\ & \stackrel{0}{N} \end{aligned}$ |  | $\begin{aligned} & \text { io } \\ & \text { in } \\ & \stackrel{0}{0} \\ & \stackrel{\sim}{N} \end{aligned}$ | $\begin{aligned} & \stackrel{0}{0} \\ & \stackrel{0}{0} \\ & \stackrel{0}{0} \\ & \stackrel{0}{N} \end{aligned}$ | $\left\|\begin{array}{l} \circ \\ \stackrel{0}{2} \\ \stackrel{0}{0} \\ \stackrel{i}{N} \\ \end{array}\right\|$ |  | $\begin{aligned} & \text { or } \\ & \stackrel{1}{1} \\ & \stackrel{\sim}{2} \end{aligned}$ | $\left\|\begin{array}{c} o \\ \underset{1}{1} \\ \vdots \\ \end{array}\right\|$ | $$ | $\begin{aligned} & \text { n } \\ & \underset{1}{1} \\ & o \\ & \hline \end{aligned}$ | $\left\lvert\, \begin{aligned} & \infty \\ & \stackrel{\infty}{0} \\ & \stackrel{y}{j} \\ & -\neq \end{aligned}\right.$ | $\begin{aligned} & \infty \\ & \stackrel{\infty}{6} \\ & \underset{子}{\dot{F}} \end{aligned}$ | $\begin{aligned} & \infty \\ & \stackrel{\infty}{0} \\ & \stackrel{0}{\dot{f}} \\ & \underset{f}{2} \end{aligned}$ | $\begin{aligned} & \infty \\ & \stackrel{\infty}{\circ} \\ & \stackrel{+}{7} \\ & \hline \end{aligned}$ | $\begin{aligned} & \stackrel{\infty}{仓 ̂} \\ & \stackrel{\ominus}{\dot{\gamma}} \end{aligned}$ | $\begin{array}{\|c\|} \infty \\ \infty \\ \underset{\sim}{1} \\ \propto \\ \propto \end{array}$ | $\begin{gathered} \infty \\ \underset{\sim}{\infty} \\ \underset{\sim}{\infty} \\ \underset{\sim}{2} \end{gathered}$ | $\left.\begin{gathered} \infty \\ \infty \\ \underset{\sim}{\infty} \\ \dot{\sim} \end{gathered} \right\rvert\,$ | $\begin{array}{\|l\|l} \infty \\ \infty \\ \underset{\sim}{1} \\ \dot{\sim} \end{array}$ | $\begin{aligned} & \infty \\ & \underset{\sim}{\infty} \\ & \underset{\sim}{1} \\ & \underset{\sim}{\infty} \end{aligned}$ | $\begin{aligned} & \stackrel{8}{0} \\ & 0 \\ & 0.8 \end{aligned}$ | $\begin{aligned} & 8 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & \hline 0 \end{aligned}$ | $\begin{aligned} & \dot{8} \\ & 0 \\ & 0 \\ & 0 \\ & \hline 0 \end{aligned}$ |
|  | $\begin{aligned} & \stackrel{\rightharpoonup}{\dot{~}} \\ & \underset{\sim}{0} \\ & \dot{\sim} \end{aligned}$ | $\left\|\begin{array}{c} \dot{\otimes} \\ \dot{O} \\ \dot{\sim} \\ \dot{\sim} \end{array}\right\|$ | $\begin{aligned} & \stackrel{\circ}{0} \\ & \stackrel{0}{0} \\ & \stackrel{\rightharpoonup}{\mathrm{~N}} \end{aligned}$ | $\begin{aligned} & \stackrel{\rightharpoonup}{\circ} \\ & \stackrel{0}{0} \\ & \stackrel{\rightharpoonup}{\dot{N}} \end{aligned}$ | $\left\|\begin{array}{c} \infty \\ \infty \\ \dot{1} \\ \dot{~} \\ \dot{N} \end{array}\right\|$ | $\begin{aligned} & \stackrel{\circ}{8} \\ & \stackrel{+}{-} \\ & \stackrel{n}{2} \end{aligned}$ |  | $\left\|\begin{array}{c} 0 \\ \underset{6}{0} \\ \stackrel{-}{m} \end{array}\right\|$ |  | $\left\|\begin{array}{l} 0 \\ 0 \\ \infty \\ \infty \\ \underset{\sim}{2} \end{array}\right\|$ | $\left\|\begin{array}{l} \dot{\theta} \\ \underset{\sim}{1} \\ \underset{\sim}{0} \end{array}\right\|$ |  | $\begin{array}{\|c} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{array}$ | $\left\|\begin{array}{l} o \\ \vdots \\ 0 \\ \vdots \\ \dot{0} \\ 0 \end{array}\right\|$ | $\begin{aligned} & \stackrel{O}{0} \\ & \infty \\ & \stackrel{\infty}{\circ} \\ & \stackrel{e}{2} \end{aligned}$ | $\left.\begin{array}{\|l\|} \hline \\ 1 \\ 1 \\ \\ \dot{e} \end{array} \right\rvert\,$ | $\begin{gathered} 0 \\ \underset{e}{2} \\ \stackrel{y}{c} \\ \stackrel{c}{2} \end{gathered}$ | $\left\|\right\|$ | $\left\lvert\, \begin{aligned} & 0 \\ & 0 \\ & \stackrel{0}{1} \\ & \underset{\sim}{1} \end{aligned}\right.$ |  | $\begin{aligned} & \stackrel{\otimes}{N} \\ & \underset{\sim}{\infty} \\ & \infty \end{aligned}$ | $\left\|\begin{array}{l\|} 0 \\ 0 \\ \underset{\sim}{0} \\ \underset{\sim}{\infty} \\ \hline \end{array}\right\|$ | $\underset{\sim}{\text { N }}$ |
| 没 考 | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\stackrel{\sim}{\sim}$ | $\stackrel{\sim}{\sim}$ | － | － | $\stackrel{\text {－}}{ }$ | $\stackrel{\circ}{\circ}$ | $\stackrel{\circ}{\circ}$ | － | ¢ | $\stackrel{\sim}{\circ}$ | 아 | ¢ | 9 | g | q | 옹 | 앙 | 앙 |
|  | 0 | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | 0 | 0 | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | － | $\bigcirc$ | － | $\bigcirc$ | 0 | $\bigcirc$ | $\bigcirc$ | 0 | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | － | $\bigcirc$ |
|  | $\checkmark$ | $-$ | $-$ | $-$ | $-$ | $-$ | $\checkmark$ | $\checkmark$ | $-$ | $-$ | $\checkmark$ | － | $\rightarrow$ | $\checkmark$ | $-$ | $\checkmark$ | $\rightarrow$ | － | $-$ | $\rightarrow$ | $\checkmark$ | $-$ | － |
| $\begin{aligned} & \text { 訁े } \\ & \text { たた } \\ & \text { だ } \end{aligned}$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ |
|  | g | 8 | 8 | 8 | ¢ 8 | 8 | ¢ 8 | 8 | 8 | ¢ 8 | 앙 | 8 | 앙 | ¢ | ¢ 8 | 앙 | 8 | \％ | 8 | 8 | 8 | 8 | 앙 |
|  | 8 | $\stackrel{8}{7}$ | 8 | $\stackrel{8}{4}$ | $\stackrel{8}{7}$ | 9 | $\stackrel{8}{7}$ | $\stackrel{9}{4}$ | 4 | $\stackrel{9}{7}$ | $\stackrel{9}{7}$ | $\stackrel{8}{7}$ | $\stackrel{9}{7}$ | 8 | 9 | $\stackrel{9}{7}$ | 8 | $\stackrel{8}{7}$ | 8 | $\stackrel{8}{4}$ | 8 | $\stackrel{9}{9}$ | 8 |
| 皆 | $\stackrel{1}{6}$ | N | $\stackrel{\infty}{\sim}$ | $\begin{gathered} 8 \\ 0 \end{gathered}$ | $\stackrel{\circ}{\circ}$ | $\underset{\sim}{\infty}$ | $\underset{\sim}{\infty}$ | $\stackrel{\infty}{\circ}$ | $\stackrel{\text {－}}{ }$ | $\begin{aligned} & \infty \\ & \infty \\ & \infty \end{aligned}$ | $\stackrel{\circ}{\circ}$ | $\begin{array}{\|c} \stackrel{\rightharpoonup}{\infty} \\ \end{array}$ | $\stackrel{\infty}{\infty}$ | $\stackrel{\infty}{\circ}$ | $\stackrel{8}{8}$ | $\stackrel{7}{0}$ | ס্ঠু | ® | 号 | $\begin{aligned} & \text { 哭 } \end{aligned}$ | $\stackrel{\circ}{8}$ | 尔 | $\stackrel{\infty}{\circ}$ |

Table B.1. Computational results of the proposed algorithm. (cont.)

| $\begin{gathered} \text { Iteration } \\ \quad \# \end{gathered}$ | $\begin{aligned} & \text { Number } \\ & \text { of } \\ & \text { Riders } \end{aligned}$ | Number of Drivers | Capacity | Rider <br> Count | Number <br> of Riders <br> Rejecting <br> First Match | $\begin{gathered} \text { JSS } \\ \text { Limit } \end{gathered}$ | Computation Time | Average JSS of Matched Pairs | Number <br> of <br> Matched <br> Riders | Number <br> of <br> Matched <br> Drivers | $\begin{gathered} \text { Ratio } \\ \text { of } \\ \text { Matched } \\ \text { Riders } \end{gathered}$ | Ratio of <br> Matched <br> Drivers | Ratio <br> of <br> Riders <br> Accepting <br> First Match | $\begin{gathered} \text { Case } \\ \# \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 599 | 479 | 69 | 3 | 1 | 0 | 50 | 38.3410 | 60.0769 | 13 | 5 | 2.71\% | 7.25\% | 100.00\% | 10 |
| 600 | 479 | 69 | 3 | 1 | 0 | 50 | 41.0740 | 60.0769 | 13 | 5 | 2.71\% | 7.25\% | 100.00\% | 10 |
| 601 | 479 | 69 | 3 | 1 | 0 | 60 | 43.9120 | 70.0000 | 6 | 2 | 1.25\% | 2.90\% | 100.00\% | 10 |
| 602 | 479 | 69 | 3 | 1 | 0 | 60 | 39.1040 | 70.0000 | 6 | 2 | 1.25\% | 2.90\% | 100.00\% | 10 |
| 603 | 479 | 69 | 3 | 1 | 0 | 60 | 38.8900 | 70.0000 | 6 | 2 | 1.25\% | 2.90\% | 100.00\% | 10 |
| 604 | 479 | 69 | 3 | 1 | 0 | 60 | 38.9620 | 70.0000 | 6 | 2 | 1.25\% | 2.90\% | 100.00\% | 10 |
| 605 | 479 | 69 | 3 | 1 | 0 | 60 | 39.0180 | 70.0000 | 6 | 2 | 1.25\% | 2.90\% | 100.00\% | 10 |
| 606 | 479 | 69 | 3 | 1 | 0 | 70 | 39.1480 | 75.0000 | 3 | 2 | 0.63\% | 2.90\% | 100.00\% | 10 |
| 607 | 479 | 69 | 3 | 1 | 0 | 70 | 39.2240 | 75.0000 | 3 | 2 | 0.63\% | 2.90\% | 100.00\% | 10 |
| 608 | 479 | 69 | 3 | 1 | 0 | 70 | 39.4180 | 75.0000 | 3 | 2 | 0.63\% | 2.90\% | 100.00\% | 10 |
| 609 | 479 | 69 | 3 | 1 | 0 | 70 | 39.2350 | 75.0000 | 3 | 2 | 0.63\% | 2.90\% | 100.00\% | 10 |
| 610 | 479 | 69 | 3 | 1 | 0 | 70 | 43.7970 | 75.0000 | 3 | 2 | 0.63\% | 2.90\% | 100.00\% | 10 |
| 611 | 479 | 69 | 3 | 1 | 0 | 80 | 41.8190 | - | 0 | 0 | 0.00\% | 0.00\% | 100.00\% | 10 |
| 612 | 479 | 69 | 3 | 1 | 0 | 80 | 42.5720 | - | 0 | 0 | 0.00\% | 0.00\% | 100.00\% | 10 |
| 613 | 479 | 69 | 3 | 1 | 0 | 80 | 38.9270 | - | 0 | 0 | 0.00\% | 0.00\% | 100.00\% | 10 |
| 614 | 479 | 69 | 3 | 1 | 0 | 80 | 38.9110 | - | 0 | 0 | 0.00\% | 0.00\% | 100.00\% | 10 |
| 615 | 479 | 69 | 3 | 1 | 0 | 80 | 39.3470 | - | 0 | 0 | 0.00\% | 0.00\% | 100.00\% | 10 |

