# UNSUPERVISED JOINT PART-OF-SPEECH TAGGING AND STEMMING FOR AGGLUTINATIVE LANGUAGES 

# SONDAN EKLEMELİ DİLLERDE GÖZETİMSİZ EŞZAMANLI SÖZCÜK TÜRÜ İŞARETLEME VE GÖVDELEME 

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# ABSTRACT <br> Unsupervised Joint Part-of-Speech Tagging and Stemming For Agglutinative Languages 

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Part of Speech (PoS) tagging is the task of assigning each word an appropriate part of speech tag in a given sentence regarding its syntactic role such as verb, noun, adjective etc. Various approaches have already been proposed for this task. However, the number of word forms in morphologically rich and productive agglutinative languages is theoretically infinite. This variety in word forms causes sparsity problem in the tagging task for agglutinative languages. In this thesis, we aim to deal with this problem in agglutinative languages by performing PoS tagging and stemming simultaneously. Stemming is the process of finding the stem of a word by removing its suffixes. Joint PoS tagging and stemming reduces sparsity by using stems and suffixes instead of words. Furthermore, we incorporate semantic features to capture similarity between stems and their derived forms by using neural word embeddings.

In this thesis, we present a fully unsupervised Bayesian model using Hidden Markov Model (HMM) for joint PoS tagging and stemming for agglutinative languages. The results indicate that using stems and suffixes rather than full words outperforms a simple word-based Bayesian HMM model for especially agglutinative languages. Combining semantic features yields a significant improvement in stemming.

Anahtar Kelimeler: unsupervised learning, part-of-speech (PoS) tagging, stemming, Bayesian learning, Hidden Markov model (HMM), semantic, neural word embeddings

## ÖZET

# Sondan Eklemeli Dillerde Gözetimsiz Eşzamanlı Sözcük Türü̈ İşaretleme ve Gövdeleme 

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Sözcük türü işaretleme, cümledeki fiil, isim, sıfat v.b. sözdizimsel rolüne bakarak her bir sözcüğe uygun etiketin atanmasıdır. Bu işlem için çeşitli yöntemler önerilmiştir. Morfolojik olarak zengin ve üretken sondan eklemeli dillerde sözcük formlarının sayısı teorik olarak sonsuzdur. Sözcük formlarındaki bu çeşitlilik, sondan eklemeli dillerde etiketleme işleminde seyreklik problemi yaratmaktadır. Bu tezde sözcük türü işaretleme ve gövdeleme işlemlerini eşzamanlı gerçekleştirerek sondan eklemeli dillerde bu problemin üstesinden gelmeyi amaçlamaktayız. Gövdeleme, bir sözcüğü eklerinden ayırarak gövdeyi bulma işlemidir. Birleşik sözcük türü işaretleme ve gövdeleme, sözcükler yerine gövde ve ekler kullanarak seyreklik problemini azaltmaktadır. Ayrıca, gövde ve gövdeden türetilmiş sözcük arasındaki benzerliği yakalamak için anlamsal özelliklerden yararlanmaktayız.

Bu tezde, sondan eklemeli dillerde birleşik sözcük türü işaretleme ve gövdeleme işlemi gerçekleştirmek için tamamen gözetimsiz Bayesian Saklı Markov modeli sunulmuştur. Sonuçlar, özellikle sondan eklemeli diller için sözcükler yerine gövdeler ve eklerinin kullanılmasının sözcük tabanlı Bayesian HMM modelinden daha iyi olduğunu göstermektedir. Anlamsal özelliklerin eklenmesi ise gövdelemede belirgin bir iyileşme göstermektedir.

Keywords: gözetimsiz öğrenme,sözcük türü işaretleyici, gövdeleme, Bayesian öğrenme, saklı Markov model

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## ABBREVIATIONS

| CRF | Conditional Random Fields |
| :--- | :--- |
| CRP | Chinese Restaurant Process |
| CW | Chinese Whispers |
| ddCRP | distance independent CRP |
| DP | Drichlet Process |
| EM | Expectation Maximization |
| FSM | Frakes and Fox Similarity Metric |
| GRAS | GRaph-based Stemmer |
| HDP | Hierarchical Drichlet Process |
| HMM | Hidden Markov Model |
| HPS | High Precision Stemmer |
| ICF | Index Compression Factor |
| iHMM | infinite HMM |
| IR | Information Retrieval |
| KL | Kullback-Leibler |
| LSA | Latent Semantic Analysis |
| MAP | Maximuml a Posteriori |
| MCMC | Markov Chain Monte Carlo |
| MCRS | Mean Number of Characters and Removed in forming Stems |
| MDL | Minimum Description Length |
| MEM | Maximum Entropy Model |
| MHD | Mean and Median Modified Hamming Distance |
| ML | Maximum Likelihood |

MLE Maximum Likelihood Estimation
MMI Maximum Mutual Information
MWC Mean Number of Words per Conflation Class
NLP Natural Language Processing
NMI Normalized Mutual Information
NWSF Number of Words and Stems diFfer
OOV out-of-Vcabulary
PMF Probability Mass Function
PoS Part of Speech
RF Relative Frequency
SVD Singular Value Decomposition
TTS Text to Speech
VI Variation of Information
WSJ Wall Street Journal
YASS Yet Another Suffix Striper

## 1. INTRODUCTION

### 1.1. Overview

Parts of speech play a crucial role in defining the structure and meaning of a sentence in any language. Words can be labeled with different parts of speech depending their syntactic roles in the sentence. Assigning each word a part of speech such as noun, verb, adjective, etc. is called Part of Speech (PoS) tagging task in Natural Language Processing (NLP). It is one of the early tasks in NLP. PoS taggers take a sentence as input and generate a list of tuples (word/tag) as output, where each word is assigned to related tag.

Example The sentence
Bunu zaten biliyordum. (I have already known that.) is tagged as:

## Bunu/Pron zaten/Adv biliyordum/Verb ./Punc

This task determines the syntactic features of the words such as gender, tense, etc. [3].

Stemming is the process of removing inflectional affixes from a word. The aim of stemming is to reduce the morphological variants to a linguistically correct stem from which all different word forms are derived.

Example : kitaplar (books), kitapta (in the book), kitaplarm (my books) have the same stem kitap (book)

PoS tagging and stemming have been playing significant roles in several NLP applications. Thus, small improvements on these tasks have the potential to yield larger improvements in many NLP tasks like Information Retrieval (IR), Linguistic Research, Text to Speech (TTS), Information Extraction and Shallow Parsing.

One of the challenges of PoS tagging is ambiguity. Many words can take several parts of speech. For example booking can be a noun (e.g. We made the booking three months ago.) or a verb (e.g. She is booking a table for four at their favorite restaurant.). Such a problem is common in many languages. The other challenge is out-of-vocabulary ( OOV ) problem. There will be many words which have not been seen in training.

### 1.2. Motivation

Agglutinative languages like Turkish are morphologically rich and productive. Turkish has nearly 23,000 stems and words formed by gluing suffixes to stems. Therefore, infinite number of words can be formed theoretically [4]. Due to rich morphology, these languages raises several challenges in PoS tagging and stemming.

There is a strong mutual relation between stemming and PoS tagging. Modeling joint PoS tagging and stemming helps to solve these challenges. Joint PoS tagging and stemming helps tackle the OOV problem by reducing the lexicon size. For instance, the words kitaplarda (in books), kitaplar (books), kitap (book), kitapta (in the book), kitaplarım (my books), kitaptan (from the book), kitapları ((their) books), kitapla (with the book), kitaplara (to the books) are inflected from the stem kitap (book). By mapping the different word forms to the same stem, we can reduce the word forms to a single stem by also reducing the dictionary size and increasing the frequency of occurrence of the words. Joint PoS tagging and stemming also helps to determine how to split a word as a stem and a affix. For example, the words koyun can be split as koy+un (put) or koyun+\# (sheep) depending on its tag. PoS tag of the word helps to choose the correct stem.

Pipeline approaches solve tasks in order, for example stemming after then PoS tagging. One drawback of pipeline approaches is the error propagation where the errors accumulate in all stages. Joint models can avoid this kind of problem and achieve a better performance on both sub-tasks.

This is why a joint model would be more effective to handle PoS tagging and stemming instead of a pipeline approach [5].

Although supervised PoS tagging and stemming models perform better than unsupervised models, supervised models are applicable only to a set of well-studied languages that have labeled corpora available. However, more than $99 \%$ of the languages in the world are still considered less-studied and resource scarce [6]. Therefore, it indicates that developing unsupervised models is crucially needed for these languages.

In this thesis, we extend the fully unsupervised Bayesian PoS tagging model [7] for agglutinative languages. Instead of using words, we enhance the model by using stems, affixes and
semantic features. We primarily focus on Turkish as an agglutinative language. However, the models will be applicable to all languages.

### 1.3. Research Questions

These are the research questions that are aimed to be answered in this thesis:

- Can unsupervised PoS tagging be improved by integrating the stemming task jointly to the same learning mechanism? Does joint model help to reduce the sparsity problem in PoS tagging?
- Can we enhance stemming and PoS tagging results by integrating semantic features to the joint model?


### 1.3.1. Thesis Structure

The structure of the thesis is as follows:
Chapter 2 details essential background knowledge to understand the thesis. It starts with linguistic background, describes agglutinative languages and challenges of these languages. Then, we explain machine learning methods that we used in this thesis.

Chapter 3 provides an overview of the previous studies on PoS tagging and stemming. We focus on HMM for PoS tagging and unsupervised methods on stemming. We also discuss evaluation algorithms for PoS tagging and stemming. This chapter also presents studies on Turkish PoS tagging and stemming.

Chapter 4 describes a novel joint model in which PoS tagging and stemming are learned cooperatively and simultaneously. First, we present the baseline model that constructed on. Finally, the inference algorithm is described.

Chapter 5 reports our experimental results and compare PoS tagging and stemming results with other approaches in the literature for agglutinative languages and morphologically poor languages. We end this chapter with the analysis of parameters.

Finally, Chapter 6 concludes this thesis with a brief summary of our work with contributions made to the fields of PoS tagging and stemming and proposes future topics to be studied based on the the study in both fields.

## 2. BACKGROUND

In this chapter, we review background information to follow the approaches presented in this thesis. We start by explaining the linguistic background in Section 2.1. Then, we focus on the machine learning background in Section 2.2.

### 2.1. Linguistic Background

"There are close on 7,000 languages in the world, and half of them have fewer than 7,000 Speakers each, less than a village. What is more, $80 \%$ of the world's languages have fewer than 100,000 speakers."(Ostler 2008)

The spoken languages in the world can be classified as follows: Inflective languages, agglutinative languages, isolating languages, and incorporating languages.

Inflective languages consist of stems with variable terminations or suffixes which were once independent words like Latin. Agglutinative languages consist of more than one, and possibly many morphemes. Examples of agglutinative languages are Turkish and Hungarian. Isolating language is a language in which meaning is created by supplemental words. Thus, almost every word consists of a single morpheme in the language. Latin, Spanish, English, Chinese, and Mandarin are examples of isolating languages. Incorporating languages are referred as polysynthetic languages. A single - though extensively long - word may represent an entire phrase, or even a sentence, including a verb, an adjective and even an object in incorporating. This language is often used to refer to Native American languages such as Alabama, Dakota.

In this chapter, we provide a brief description of the morphological structure of Turkish as an agglutinative language to ease the understanding of this thesis.

### 2.1.1. Morphology

Morphology is about the internal structure of words and operates with the subword units called morphemes. It is also an interface between phonology and syntax, where morphological forms as constituents carry both syntactic and phonetic information. For example, word
kitapçılar (booksellers) is composed from root kitap (book), and two bound morphemes -çı and -lar.

Agglutinative languages are morphologically productive languages that contain a set of rules for morphological composition that generate a considerable amount of word forms by the concatenation of morphemes [8].

Morphemes can be either roots or affixes. Affixes can be either inflectional or derivational. Roots can take derivational and inflectional affixes; therefore, a root can be seen in a large number of different word forms. Various suffixes and their combinations make a complex problem to find stems in agglutinative languages.

Example Some of the word forms that are built from the root basar(-mak) ((to) succeed) are as follows:
başar(-mak) - ((to) succeed)
başarı-(success)
başarısız - (unsuccessful)
başarısızlaş(-mak) - ((to) become unsuccessful)
başarısızlaştır(-mak) - ((to) make one unsuccessful)
başarısızlaştırıcı - (maker of unsuccessful ones)
başarısızlaştrııcılaş(-mak) - ((to) become a maker of unsuccessful ones)
başarısızlaştırıcılaştır(-mak) - ((to) make one a maker of unsuccessful ones)
Inflectional suffixes add appropriate syntactic features such as gender, tense, etc. [3] to the word whereas derivational suffixes change the meaning of the word. For instance, the suffix -ler in the word kalemler (pencils) is inflectional because it marks the plurality of the word kalem (pencil) and kalem (pencil) and kalemler (pencils) share the same meaning. The suffix -gi in the word silgi (eraser) is derivational because it changes the meaning of the word from an action to a tool. Here, the derivational suffix also changes the PoS tag of the word.

A stem is the base of an inflected word. The stem of a word does not necessarily have to be indivisible and can consist of a root that has derivational suffixes attached to it.


Figure 2.1. Structure of a typical word in an agglutinative language

Figure 2.1. shows how a word is generated through inflection and derivation. Roots are transformed into stems with derivational suffixes.

For example, the word kitapçı (bookseller) is a stem and it can be used to derive the plural form kitapçılar (booksellers) by adding the inflectional suffix -lar.

One of the challenging problem of agglutinative languages is that a word may have multiple meanings according to the stem and its PoS tag. For example geçmiş in Turkish may mean past as adjective or passed as verb depending on the context. In the adjective case, the stem is geçmiş whereas, in the verb case the stem is geç (see Figure 2.2.).


Figure 2.2. Stem of word geçmiş according to different PoS

### 2.1.2. Syntax

Syntax is a set of rules, principles and processes that govern the structure of sentences in a given language. According to the theory of universal grammar that originates from the work of Chomsky (1965) [9], "Every language has its own syntax, however languages share a common set of properties which are limited in the human brain, and that makes them universal".

Under syntactic rules, part of speech categories such as noun, verb or preposition designate a group of words with certain morphosyntactic properties. These can be divided into two

Table 2.1. PoS tag list proposed by Petrol et al. [2]

| Tag | Definition | Example <br> gitmiş, gelecek, yüzüyor |
| :--- | :--- | :--- |
| VERB | Verbs (all tenses and modes) | kitap, Ahmet, gözlük |
| NOUN | Nouns (Common and proper) | Ben, onlar |
| PRON | Pronouns | sicak, genç, küçük |
| ADJ | Adjectives | içeri, hizlıca |
| ADV | Adverbs | gibi, değil, üzere |
| ADP | Adpositions (prepositions and postpositions | fakat, oysaki, üstelik |
| CONJ | Conjunctions | bir, bu |
| DET | Determiners | onbeş, ,iki |
| NUM | Cardinal numbers | göre, kadar |
| PRT | particles or other function words | TDK, THY |
| X | Other (foreign words, types, abbreviations) | TDK |
| . | Punctiation | ?, : |

categories: closed class types and open class types. Closed classes have fixed number of members, whereas open classes may accept many members, thereby they can infinite number of members.

There are four main open classes; noun, verb, adjective, adverb.
Noun class includes the words that mostly correspond to people, places, or other things.
The verb class includes the words referring to actions e.g. git(mek) ((to) go), bil(mek) ((to) know), $\operatorname{konuş}^{(m a k)}$ ((to) talk).

The adverb class describes and gives information about a verb, adjective, adverb or phrase. For instance, in sentence "Hizll konuşurum." ("I speak fast"), the adverb hizlı modifies the verb konuşurum.

The adjective class modifies nouns and pronouns by describing a particular quality of the word. For example, in noun phrase çalışkan öğrenci (hardworking student), çalışkan modifies student.

Closed classes differ from language to language differently from open classes. Major closed classes are prepositions, determiners, pronouns, conjunctions, participles, numerals.

Petrov et al. (2011) [2] propose a Universal PoS tag set that defines 12 universal categories.

### 2.2. Machine Learning Background

### 2.2.1. Hidden Markov Models

A Hidden Markov Model (HMM) is a method for representing probability distributions over sequences of observations. A sequence of hidden states $\left(S_{1}, S_{2}, \ldots.\right)$ is generated according to a Markov process. Conditioned on the hidden states, we observe $\left(Y_{1}, Y_{2}, \ldots.\right)$ where it is assumed that the $Y_{i}$ is conditionally independent of everything else given the $S_{i}$ and the $S_{i+1}$ is conditionally independent of everything else given the $S_{i}$.


Figure 2.3. A Bayesian network specifying conditional independence relations for a hidden Markov model.

### 2.2.2. Bayesian Modeling

Bayesian modeling defines the probability of an instance with respect to value of parameters, latent variables or hypotheses. A Bayesian model can be parametric or non-parametric. The Bayesian parametric models have predefined number of parameters. The Bayesian nonparametric models have countably infinite parameters that grows with data. Bayesian modeling derives from Bayes' theorem:

$$
\begin{equation*}
p(\theta \mid S)=\frac{p(S \mid \theta) p(\theta)}{p(S)} \tag{1}
\end{equation*}
$$

where $p(\theta \mid S)$ is posterior distribution of the parameters $\theta, p(S \mid \theta)$ is the likelihood and $P(\theta)$ is the prior probability. The normalization constant is given as follows:

$$
\begin{equation*}
p(S)=\int p(S, \theta) p(\theta) \tag{2}
\end{equation*}
$$

It is also called the marginal likelihood.

### 2.2.2.1. Conjugate Priors

Given a likelihood, the conjugate prior is the prior distribution such that the prior and posterior are in the same family of distributions. For example, given a likelihood $p(x \mid \theta)$, we choose a a family of prior distributions such that

$$
\begin{equation*}
p(x)=\int p(X \mid \theta) p(\theta) d(\theta) \tag{3}
\end{equation*}
$$

where $\theta$ is a set of parameters that are integrated out without being estimated. Additionally, we choose prior to posterior updating yields a posterior which is in this family.

Conjugate priors reduce Bayesian updating by modifying the parameters of prior distribution rather than computing integrals. Thus, they are widely used in practice. Dirichlet distribution is the conjugate prior for Multinomial distributions.

### 2.2.2.2. Dirichlet-Multinomial

The conjugation of a Multinomial distribution with a Dirichlet prior results in a posterior distribution with a Dirichlet distribution form. Defining a Multinomial distribution on $\{1, \ldots \ldots \ldots . . . \mathrm{N}\}$ possible outcomes and setting $\theta$ helps us to define hyperparameters. Here hyperparameters are parameters of the prior distribution when we assume that $\theta$ is following some prior distribution. For the Dirichlet distribution prior, we can say that $\beta$ is a hyperparameter.

$$
\begin{align*}
x_{i} & \propto \operatorname{Multinomial}(\theta)  \tag{4}\\
\theta & \propto \operatorname{Dirichlet}(\beta)
\end{align*}
$$

where $x_{i}$ is drawn from a Multinomial distribution with parameter $\theta$ and parameter $\theta$ is drawn from a Dirichlet distribution with hyperparameter $\beta$.

### 2.2.2.3. Multinomial Distribution

Multinomial distribution is the probability distribution of the outcomes in a Multinomial experiment. The Multinomial distribution arises when each datum in one of $K$ possible outcomes with a set of probabilities $\left\{x_{1} \ldots x_{k}\right\}$ Multinomial models the distribution that indicates how many times each outcome is observed over N total number of data points:

$$
\begin{equation*}
p(x \mid \theta)=\frac{N!}{\sum_{k=1}^{K} n_{k}!} \prod_{k=1}^{K} \theta_{k}^{x_{k}} \tag{5}
\end{equation*}
$$

Here parameters $\theta_{k}$ are the probabilities of each data point $k$, and $n_{k}$ is the number of occurrences of data point $x_{k}$ and:

$$
\begin{equation*}
N=\sum k=1 K n_{k} \tag{6}
\end{equation*}
$$

### 2.2.2.4. Dirichlet Distribution

Dirichlet distribution is a way to model random Probability Mass Function (PMF) for finite sets. It is often used as the prior distribution in Bayesian inference and it is the conjugate of the Categorical distribution and Multinomial distribution. Dirichlet distribution follows the form:

$$
\begin{equation*}
p(\theta \mid \beta)=\frac{1}{B(\beta)} \prod_{k=1}^{K} \theta_{k}^{\beta_{k}-1} \tag{7}
\end{equation*}
$$

where $\beta=\left(\beta_{1}, \beta_{2}, \ldots, \beta_{K}\right)$ denotes the concatenation parameters, $K \geq 2$ denotes the number of categories, and $B(\beta)$ is a normalizing constant in a Beta function form:

$$
\begin{equation*}
B(\beta)=\frac{\prod_{k=1}^{K} \Gamma\left(\beta_{k}\right)}{\Gamma\left(\sum_{k=1}^{K} \beta_{k}\right)} \tag{8}
\end{equation*}
$$

where $\Gamma$ is the generalization of the factorial function defined as $\Gamma(t)=(t-1)$ ! for positive integers.

### 2.2.2.5. Bayesian Posterior Distribution

In a conjugate Bayesian analysis, we have a Multinomial likelihood with the Dirichlet prior. The posterior distribution of parameters is given in formula 9 This leads to a Bayesian posterior $\operatorname{Dirichlet}\left(n_{k}+\beta_{k}-1\right)$.

$$
\begin{align*}
p(\theta \mid x, \beta) & \propto p(x \mid \theta) p(\theta \mid \beta)  \tag{9}\\
& =\frac{N!}{\prod_{k=1}^{K} n_{k}!} \frac{\prod_{k=1}^{K} \Gamma\left(\beta_{i}\right)}{\Gamma\left(\sum_{k=1}^{K} \beta_{i}\right)} \prod_{k=1}^{K} \theta_{k}^{n_{k}+\beta_{k}-1} \\
& \propto \operatorname{Dirichlet}\left(n_{k}+\beta_{k}-1\right)
\end{align*}
$$

### 2.2.2.6. Predictive Distribution for Dirichlet-Multinomial

The predictive distribution is the distribution of observation $x_{N+1}$ given the observations $X=\left(x_{1}, \ldots, x_{n}\right):$

$$
\begin{align*}
p\left(x_{N+1}=j \mid X, \beta\right) & =\int\left(x_{N+1}=j \mid x, \theta\right)(\theta \mid \beta) d \theta  \tag{10}\\
& =\frac{n_{j}+\beta_{j}}{N+\sum_{k=1}^{K} \beta_{k}}
\end{align*}
$$

This shows a rich-get-richer behavior, where if the frequency of the previous observations in a given category are higher, then the next observation $x_{N+1}$ has a higher probability of being in the same category.

### 2.2.2.7. Chinese restaurant process (CRP)

Chinese Restaurant Process (CRP) is distribution over partitions. It is a random process where there is a Chinese restaurant with infinite number of tables. Each table has a menu to serve. The first customer sits at the first table. The second customer decides either to sit with the first customer or by herself at a new table. In general, $n^{\text {th }}$ customer sits at an occupied table k with probability that is proportional to the number $n_{k}$ of customers who are already sitting at the table or sits at a new table with probability proportional to $\alpha$. While this process continues, tables with preferable menus will acquire a higher number of customers. Thus, the rich-get-richer principle shapes the structure of the tables.






Figure 2.4. An illustration of the CRP

### 2.3. Inference

In machine learning, inference of parameters is an essential part of the learning mechanism. There are various approaches such as Maximum Likelihood (ML) or the Maximum a Posterior (MAP) to perform a point estimation of the parameters. Bayesian inference gives an estimation of distribution over the possible values of the parameters instead of a point estimation. Sampling by drawing random samples from a distribution is one of the approaches in estimating parameters. We use Markov Chain Monte Carlo (MCMC) for the estimation. Following section gives a brief overview about this method.

### 2.3.1. Markov Chain Monte Carlo (MCMC)

A Markov Chain is a mathematical system that experiences transitions from one state to another according to certain probabilistic rules. MCMC is an estimation technique that simulates a Markov Chain to generate samples from a probability distribution in a high dimensional space. This stochastic process is described in terms of a conditional probability:

$$
\begin{equation*}
P\left(X_{n+1}=x \mid X_{1}=x_{1}, X_{2}=x_{2}, \ldots, X_{n}=x_{n}\right)=P\left(X_{n+1}=x \mid X_{n}=x_{n}\right) \tag{11}
\end{equation*}
$$

The possible values of $X_{i}$ are drawn from a countable set S , which is the state space of the chain.

Metropolis-Hastings and Gibbs sampling are two well-known examples of the set of MCMC algorithms.

### 2.3.1.1. Gibbs Sampling

Gibbs sampling is a simple and widely used method for generating random samples from a joint distribution when this distribution is not known or is difficult to calculate. Let $X=$ $\left(x_{1}, x_{2}, \ldots, x_{k}\right)$ is a set of parameters and $D$ is a set of observed data. In each iteration of Gibbs sampling, $x_{k}$ sampled from the conditional distribution given $x_{-k}$ (the set of all variables except $x_{k}$ fork $=1,2, \ldots K$ ).

$$
\begin{equation*}
x_{k} \sim P\left(x_{k} \mid x_{-k}, D\right) \text { fork }=1 \ldots . K \tag{12}
\end{equation*}
$$

This process continues until convergence (the sample values have the same distribution as if they are sampled from the true posterior distribution).

### 2.4. Conclusion

In this chapter, essential background knowledge is presented to be referred throughout the thesis. As the thesis mainly focuses on morphology and syntax for agglutinative languages, a general overview of the two fields is given from the linguistic perspective based on basic terms and their definitions. Additionally, we present some statistical machine learning methods used for PoS tagging and stemming frequently.

## 3. RELATED WORK

### 3.1. Introduction

This chapter presents earlier work on unsupervised stemming and PoS tagging.

### 3.2. Literature Review on Unsupervised Part of Speech Tagging

PoS tagging is the task of assigning a syntactic category, e.g. noun, adjective for each word in a sentence. There are PoS tagging approaches such as Hidden Markov Model [10] , Maximum Entropy Model [11], Decision Trees [12], Log Linear Models [13], clustering [14].

Learning in PoS tagging can be defined by, supervised, unsupervised, or hybrid learning. In this section, we concentrate on unsupervised approaches since the scope of this thesis consists of only unsupervised learning.

### 3.2.1. Clustering

This approach takes the advantage of distributional properties of words (similar words occur in similar contexts) by computing a context vector for each word to cluster into syntactic categories( [14], [15], [16], [17])

Brown et al. (1992) [14] present an approximate greedy hierarchical clustering algorithm that uses a bigram model to assign each word a latent class. Algorithm initializes each word type in separate cluster. Then a cluster pair is merged iteratively that cause a increase in the likelihood of the corpus according to a HMM. The probability of the corpus $w_{1} \ldots w_{n}$ is computed as follows:

$$
\begin{equation*}
P\left(w_{1} \mid c_{1}\right) \prod_{i=2}^{n} P\left(w_{i} \mid c_{i}\right) P\left(c_{i} \mid c_{i-1}\right) \tag{13}
\end{equation*}
$$

where $c_{i}$ is the class of $w_{i}$. The algorithm ends if no cluster pair is merged. At the end of the algorithm, a hierarchy of word types is obtained that can be presented as a binary tree as in Figure 3.1.


Figure 3.1. The binary tree obtained from Brown clustering

Finch and Chater (1992) [15] widen the idea of word clustering and collect global context vectors; i.e. the two preceding and the two following words of target words that are the 150 words with the highest frequency. Hierarchical clustering algorithm is applied on these vectors to acquire syntactic classes by using Spearman Rank Correlation Coefficient to measure linguistic similarity.

Schütze (1993) [18] uses two left and right words as context vectors. After obtaining words vectors, Singular Value Decomposition (SVD) is performed to reduce the dimension of the context matrix and then Buckshot clustering algorithm [10] is applied to build the clusters.

Schütze (1995) [19] applies Latent Semantic Analysis (LSA) with SVD based dimensionality reduction.

Clark (2000) [16] uses the distribution of the context in a flat clustering algorithm. KullbackLeibler (KL) divergence is used to measure the divergence between clusters to decide whether to merge two clusters.

Biemann (2006) [17] uses Chinese Whispers (CW) graph clustering algorithm, based on the similarity in context. Unlike the other systems, this model doesn't need a clustering number as a parameter. Graph is constructed by the most frequent 10.000 words using their context statistics that are extracted from 150-250 feature words that appear immediately on the left or right of a target word.

### 3.2.2. Hidden Markov Models

One of the widely used approaches in PoS tagging is the HMMs( [20]).
HMM assumes that there are $K$ states $T=t_{1}, \ldots, t_{k}$. These tags are hidden during the observation and they generate the word sequence $W=w_{1}, \ldots, w_{n}$ observed in the corpus and the probability of the sentence is computed as follows with a first order assumption:

$$
\begin{equation*}
P(W, T)=P\left(w_{1} \mid t_{1}\right) \prod_{i=2}^{n} P\left(w_{i} \mid t_{i}\right) P\left(t_{i} \mid t_{i-1}\right) \tag{14}
\end{equation*}
$$



Figure 3.2. Bigram HMM

In the second order HMM, each tag is assumed to be dependent on the previous two tags in the history.


Figure 3.3. Trigram HMM

Merialdo (1994) [21] attempts to improve the trigram HMM PoS tagging by using Expectation Maximization (EM). The model uses a dictionary of possible tags for each word. Two different training a pro-supervised (Relative Frequency (RF)) and pro-unsupervised (ML / Forward Backward training) are applied. Two strategies are used for tagging:

- Viterbi computes the most probable tag sequence in a sentence
- EM computes the most probable tag for each word in a sentence

The paper concludes that ML training performs better on a small amount of labeled data, while RF gives more accurate results on a larger set of labeled data.

Banko and Moore (2004) [22] present a Contextualized HMM tagger and also do a comparative performance analysis on pre-existing strategies on the same data. The goal of contextualized HMM tagger is to include more context into tagging to estimate the probability of a word based on the tags immediately preceding and following it.


Figure 3.4. Contextualised HMM Tagger

### 3.2.3. Bayesian

Johnson (2007) [23] criticizes the standard HMM-EM approaches because of their poor performance on the unsupervised POS tagging due to their tendency to emit from each hidden state equal number of words.He adopts a Bayesian learning in an HMM model and compares the estimators used in HMM PoS taggers with the Bayesian estimator. The study shows the
drawbacks of EM [24] compared to Gibbs sampling [25] and Variational Bayes [26] estimators. The results show that training with EM gives poor results because of the distribution of hidden states.

Goldwater and Griffiths (2007) [7] propose a Bayesian approach adopted in a second order HMM with symmetric Dirichlet priors over transition and emission distributions:

$$
\begin{align*}
t_{i} \mid t_{i-1}=t, \tau^{\left(t, t^{\prime}\right)} & \propto \operatorname{Mult}\left(\tau^{\left(t, t^{\prime}\right)}\right)  \tag{15}\\
w_{i} \mid t_{i}=t, \omega^{(t)} & \propto \operatorname{Mult}\left(\omega^{(t)}\right) \\
\tau^{\left(t, t^{\prime}\right)} \mid \alpha & \propto \operatorname{Dirichlet}(\alpha) \\
\omega^{(t)} \mid \beta & \propto \operatorname{Dirichlet}(\beta)
\end{align*}
$$

Gibbs sampling is used to estimate the parameters. Two sets of experiments are performed with fixed values of hyperparameters, and with the hyperparameter inference. The results show that Bayesian HMM increase the accuracy by up to $14 \%$ over Maximum Likelihood Estimation (MLE).

Remark: We adopt the PoS tagging algorithm of [7] for joint PoS tagging and stemming. Description of the algorithm is given in the Chapter 4.

Gao and Johnson (2008) [27] compare different estimators used in HMM PoS taggers and show that while Gibbs sampler performs better on small datasets with few tags, whereas Variational Bayesian performs better on large data sets.

Gael et al. (2009) [28] use the infinite HMM (iHMM) version of the non parametric HMM that also leans the number of hidden states. Dirichlet and Pitman-Yor processes are used on experiments. Shallow parsing task is used as an extrinsic evaluation of PoS tagging.


Figure 3.5. Infinite HMM Tagger

Stratos et al. (2016) [29] assume that each hidden state is linked with an observation state (anchor state). For instance, word "the" can appear only as a determiner tag. For this reason, this HMM model is called as anchor HMM.

### 3.2.4. Other Approaches

Eisner and Smith (2005) [13] use Conditional Random Fields (CRF) with contrastive estimation. They present a diluted dictionary, where infrequent words may have any tag. This method outperforms the EM and Bayesian HMM models.

Christodoulopoulos et al. (2010) [30] compare older systems and show that former one-tag-per word models tended to improve system performance by reducing model flexibility. They use prototype based features based on [31] with automatically induced prototypes.

Berg-Kirkpatrick et al. (2010) [32] use a log-linear model for PoS tagging. the authors use the morphology as a parameter in the sequence model to induce words that share the same tag to have same morphological features.

### 3.3. Literature Review of Cooperative Learning of Part of Speech Tagging

Qiu et al. (2012) [33] present a joint model that integrates two Markov chains for segmentation and PoS tagging. One of the chains is used for segmentation and the other one is used for PoS tagging. Results show that joint model outperforms traditional methods on Chinese segmentation and PoS tagging.

Sirts and Tanel (2012) [1] present a fully unsupervised non-parametric Bayesian model for joint PoS tagging and morphological segmentation. Model generates each word type with its tag and morphological segmentation and then proceed to generate HMM parameters by HDP. Standard HMM procedure is applied to generate the word itself, its tag, its segmentation.


Figure 3.6. Joint PoS tagging and segmentation proposed by Sirts and Tanel [1]

Gibbs sampling is used for tagging and Metropolis-Hastings sampling is used for segmentation.

Sirts et al. (2014) [34] present a new approach that is a joint non-parametric Bayesian model combining morphological and distributional information based on distance independent Chinese Restaurant Process (ddCRP). ddCRP is an extension of CRP and defines a distribution over partitions of data paints. In CRP, each customer chooses a table based on a probability proportional to the number of customers who are already sitting at that table, whereas in ddCRP, a customer follows another customer and sits at the same table with that customer.

Prior is given as:

$$
P\left(c_{i}=j\right) \propto\left\{\begin{array}{ll}
f\left(d_{i j}\right) & \text { ifi } \neq j  \tag{16}\\
\alpha & i f i=j
\end{array}\right\}
$$

where $c_{i}$ is the index of the customer followed by customer $i$, f is a decay function, $d_{i j}$ is the distance between i and j .

Word embeddings are used for distributional features to assess the similarity between words.

### 3.3.1. PoS Tagging of Turkish

Oflazer and Kuruöz (1994) [35] and Oflazer and Tür (1997) [36] propose a rule based approach for Turkish PoS tagging.

Hakkani-Tür et al.(2000) [37] introduce a statistical approach for morphological disambiguation.

Altmyurt et al. (2006) [38] combine rule based and statistical approaches to build a PoS tagger. This tagger uses word frequencies and n-gram statistics.

Dinçer et al. (2008) [39] propose a stochastic PoS tagger for Turkish for information retrieval task. They define seven different lengths of word endings are used in their model. The best accuracy is obtained with 5 letters by $90.2 \%$

Kentool [40] presents a PoS tagger for Turkish based on a full scale two-level morphological specification of Turkish.

### 3.4. Literature Review on Stemming

Stemming is a linguistic process based on removing affixes from a word to produce a common form of the word. For example, the words playing, plays, played might be stemmed to the base form play. Stemming algorithms have been studied since the 1960s. We can categorize stemmers in three classes.

1. Rule-based
2. Statistical
3. Hybrid

We mainly focus on statistical approaches since the scope of this thesis is limited to unsupervised learning.

### 3.4.1. Rule-based Stemmers

Rule-based stemmers rely on specific rules on a given language. This type of stemmers generally remove suffixes from word endings based on manually defined transformation rules.

Some of the well-known rule-based stemmers are by Lovins [41], Dawson [42], Porter [43], Paice/Husk [44], and Krovetz [3]. complicated stemmer due to linguistic morphology.

### 3.4.2. Statistical Stemmers

The recent stemmers are mostly based on statistical methods. The advantage of these stemmers is that they can obviate the language specific knowledge. Therefore, they are usually language independent. A number of studies [45], [46], [47], [48] and [49] have shown that statistical stemmers are good substitutes to language-specific stemmers, especially for languages where linguistic resources are not sufficient.

The statistical stemmers use different methods like HMM, Maximum Entropy Model (MEM), Graph-based methods, Minimum Description Length principal (MDL).

The successor variety approach has been used firstly by $\operatorname{Harris}(1955)$ [50] to determine the suffixes without any prior knowledge of the language. The method calculates the number of distinct letters following a successor letter in a word to find the break-point where the successor variety increases sharply. The main idea behind this is that the letter at any position is dependent on the letters preceding it and dependency increases as we move towards the stem. Once the count of the successor and predecessor letters are available, different features are used to find the stem, such as peak and plateau, successor/predecessor entropies.

Xu et. al. (1998) [51] analyze the cooccurrence statistics of words to cope with the drawbacks of the Porter stemmer [43]. For instance, in the Porter stemmer the words policy and
police are conflated although they have different meanings but the words index and indices' are not conflated although they have the same root.

Goldsmith (2001) [52] proposes an information theoretic morphological segmentation system based on MDL. The best segmentation of the word is the one that minimizes the total compressed length of the corpus. For example, laughing, laughs, walked, walking, walks, jumped, jumping, jumps are grouped as $\{$ laugh, walk, jump $\}$ and suffixes are grouped as $\{e d$, ing, $s\}$ that is called a signature. This method is implemented as Linguistica [53].

Bacchin et al. (2002) [54] propose a graph-based algorithm for stemming. In the first step, the method splits the words at every possible split points to form a set of substrings. Then, the sets of substrings are used to build a directed graph to determine the prefix and suffix scores based on frequencies of substrings. The best split point is determined by the maximum probability of a suffix-prefix pair.

Melucci and Orio (2003) [55] present an HMM based stemmer. The letters are represented as the states in the HMM. The states correspond to either prefixes or suffixes. Rules are defined for transitions. The parameters are estimated by EM algorithm. Once the parameters are estimated, the path that has the maximum probability generates a segmentation of a word, where the first part is considered as the stem.

McNamee and Mayfield (2004) [56] propose an alternative stemming algorithm that uses letter $n$-grams. Digrams or trigrams are generated for each word. For example, following bigrams and trigrams are generated from the word kalemler:

* $k, k a, a l, l e, e m, m l, l e, e r, r^{*}$
**k, *ka, kal, ale, lem, eml, mle, ler, er*, $r^{* *}$
The basic intuition of this approach is that similar words share common $n$-grams, and $n$-gram frequencies of an inflected form of a word are less than its stem. In other words, similar words will share a high proportion of $n$-grams.

Bacchin et al. (2005) [57] extend the graph-based stemmer introduced in [54] to discover stems and derivations using mutual reinforcement relationship between stems and suffixes. Initially, a set of probable substrings are generated by splitting each word at all positions. Then, a directed graph is built where nodes represent substrings and a directed edge is inserted between node x and node y if there is a word z such that $z=x y$. The estimation of affix scores are calculated by HITS algorithm [58]. Once the prefix and suffix scores are
estimated, the algorithm finds the most probable split point by maximizing the likelihood of prefix and suffix pairs of each word in the word list.

Peng et al. (2007) [59] suggest context sensitive stemming using distributional similarity of words for the information retrieval task. Each query is expanded with the morphological variants of the query term. Additionally, bigrams are used for contextual features. For example, when stemming is applied on developing, developed, develops, development, they are all reduced to develop. Using bigrams may lead to selecting develops.

Majumder et al. (2007) [49] develop a statistical stemmer called YASS (Yet Another Suffix Striper) that adopts a complete linkage clustering algorithm by using a string distance measure. After the calculation of string similarity based on the string distance measure, the clusters (presumably morphologically related) are created using a graph-based complete linkage clustering algorithm.

Paik and Parui (2011) [60] present an unsupervised algorithm that collects the potential suffixes based on their cooccurrence frequency and then groups each word based on common prefix based on given length. Strength of the common prefix of each class is measured by integrating the potential suffix information. If strength measure is good enough, then it is considered as the root of the class. Otherwise, another root from the class is found iteratively.

Paik et al. (2011) [47] introduce GRAph-based Stemmer (GRAS) that is a statistical stemmer that groups words to find suffix pairs. The algorithm searches common prefixes among word pairs. For example, let two words $W 1=P+S 1$ and $W 2=P+S 2$ where $p$ is the longest common prefix between $w 1$ and $w 2$. The suffix pair $s 1$ and $s 2$ is a valid suffix pair if there is a common prefix followed by these suffixes in other word pairs. A weighted graph $G=(V, E)$ is built by using these suffix pairs. Each vertex of G represents a word in the lexicon and each weighted edge $w(u, v)$ represents the frequency of the suffix pair between the vertices u and v . Then the graph is decomposed to generate classes of related words.

Paik et al. (2011) [46] propose a stemming algorithm that is also based on cooccurrence statistics of words in the corpus. A graph is built where the word variants are vertices and two word variants forms and edge weighted by frequency of word variant pairs. Thus, this is a neighbor-based algorithm that can to find morphologically related words.

Paik (2013) [48] presents another stemming algorithm. Morphologically related words are clustered by using cooccurrence information that enables query independent search in the information retrieval task.

Brychcin and Konopik (2015) [45] present High Precision Stemmer (HPS) that is a statistical approach that uses orthographic and semantic information. This method works in two steps. In the first step, Maximum Mutual Information (MMI) clustering is used to cluster orthographically and semantically similar words. The word similarity is based on the longest common prefix. The second step uses a maximum entropy classifier on the clusters obtained from the first step. The classifier uses orthographic and semantic features of words to split word into their stems and suffixes. Brychchin and Konopik evaluate the performance of their stemmer on different size of data size and report that better results could be achieved with only 50.000 words. HPS, as reported in the paper, outperforms YASS [49], GRASS [47], and Linguistica [52]. Moreover, the authors train HPS in four major language families and six languages (i.e. Spanish, Polish, Hungarian, Czech, and Slovak). The results show that,HPS performs both well on seen and unseen data. The weakness of the HPS is the computational complexity especially on large datasets.

### 3.4.3. Hybrid Stemmers

Hybrid stemmers combine the rule-based and statistical approaches. This combination generally helps in increasing the performance of the stemmer.

Some of the hybrid stemmers are [61], [62], [63], [64], [65], [66].

### 3.4.4. Previous Work on Turkish Stemming

In this section, we summarize the stemming methods proposed for the Turkish language.
Köksal (1979) [67] proposes an early stemming algorithm that takes a fixed length of the initial part of the word as the stem. 5-6 letters gives the best results. However, a fixed length performance well in information retrieval task, whereas another length performs better on a different task. This shows that there is no common fixed length for different tasks. It is a simple approach but the results show that taking a fixed length improves the IR performance for Turkish.

Oflazer's (1994) morphological analyzer [68] uses a stem list and structural analysis to yield all possible analyses a given word.

Solak et al. (1994) [69] present AF algorithm. It is an adaptation of the morphological analysis system developed by Oflazer [68].

FindStem is another stemming algorithm developed by Sever and Bitirim (2003) [70]. The algorithm consists of three steps: identifying the root, doing morphological analysis and identifying the stem. The method relies on a lexicon that contains the morphological and PoS features of words, and syntactic rules.

Dinçer and Karaoğlan (2003) [71] introduce a probabilistic stemmer for a Turkish information retrieval system.

Eryiğit and Adalı (2004) [72] propose a rule-based suffix stripping algorithm for Turkish similar to Porter stemmer.

Akın and Akın (2007) [73] introduce zemberek as a morphological anaylzer and Çilden [74] introduces Snowball as a stemmer.

Özgür et al. [75] analyze the effects of stemming based on fixed-length word truncation and morphological analysis for multi-document summarization on Turkish. LexRank [76] summarization algorithm is used for the comparison. Results show that fixed-length word truncation methods improve the summarization scores, whereas morphological analysis does not improve summarization.

Özgür et al. [77] presents a language independent unsupervised stemmer for agglutinative languages. In the presence of a large enough training set, the algorithm performs stemming for an unseen word without a rule set or a separate lexicon.

Kışla and Karaoğlan (2016) [66] present a hybrid method that is based on a simple idea that nouns and verbs have different suffix patterns. A statistical method is used to strip off the suffixes and based on the suffix pattern PoS tagging is determined which then enables the decision for the stem boundary.

### 3.5. Conclusion

In this chapter, we reviewed the previous work on unsupervised PoS tagging and stemming. We also presented the PoS tagging and stemming methods applied to Turkish as an agglutinative language. This background will serve as reference point for developing a joint PoS tagging and stemming presented in the next chapter.

## 4. MODEL

This chapter presents the proposed joint unsupervised PoS tagging and stemming models in this thesis.

### 4.1. Introduction

PoS tagging and stemming are closely interconnected tasks, which is already addressed in Chapter 1. There have been many studies that perform the two tasks in an unsupervised framework. Most of these previous works have either presented pipeline approaches or hybrid approaches. We propose joint learning of PoS tagging and stemming in this thesis.

In this chapter, we describe our joint PoS tagging and stemming models. In order to learn both stems and PoS tags, we adopt the Bayesian HMM model of Goldwater and Griffiths [7], which is accepted as the baseline model. After the description of the baseline Bayesian PoS tagging model in Section 4.2., we will explain our models in Section 4.3.

### 4.2. Baseline Bayesian HMM Model

The Baseline Bayesian HMM model by Goldwater and Griffiths [7] extends the standard HMM model by adding prior distributions to the model parameters (i.e. transition and emission probability distributions). In this approach, for the prior distributions conjugate symmetric Dirichlet priors over Multinomial parameters are placed. The plate diagram of the model is given in Figure 4.1.


Figure 4.1. The plate diagram of the Bayesian HMM with symmetric Dirichlet priors.

The mathematical model is given as follows:

$$
\begin{align*}
t_{i} \mid t_{i-1}, t_{i-2}=t^{\prime}, \tau^{\left(t, t^{\prime}\right)} & \propto \operatorname{Mult}\left(\tau^{\left(t, t^{\prime}\right)}\right)  \tag{17}\\
w_{i} \mid t_{i}=t, \omega^{(t)} & \propto \operatorname{Mult}\left(\omega^{(t)}\right) \\
\tau^{\left(t, t^{\prime}\right)} \mid \alpha & \propto \operatorname{Dirichlet}(\alpha) \\
\omega^{(t)} \mid \beta & \propto \operatorname{Dirichlet}(\beta)
\end{align*}
$$

where $w_{i}$ denotes the $i$ th word and $t_{i}$ is its tag. $\operatorname{Mult}\left(\omega^{t}\right)$ is the emission distribution in the form of a Multinomial distribution with parameters $\omega^{(t)}$ that is generated by $\operatorname{Dirichlet}(\beta)$ with hyperparameter $\beta$. Analogously, $\operatorname{Mult}\left(\tau^{\left(t, t^{\prime}\right)}\right)$ is the transition distribution with parameters $\tau^{\left(t, t^{\prime}\right)}$ that is generated by $\operatorname{Dirichlet}(\alpha)$ with hyperparameter $\alpha$.

Based on the mathematical model, the conditional probability of a tag and a word are defined as follows:

$$
\begin{align*}
P\left(t_{i} \mid \mathbf{t}_{-\mathbf{i}}, \alpha\right) & =\frac{n_{\left(t_{i-2}, t_{i-1}, t_{i}\right)}+\alpha}{n_{\left(t_{i-2}, t_{i-1}\right)}+T \alpha}  \tag{18}\\
P\left(w_{i} \mid \mathbf{t}_{-\mathbf{i}}, \mathbf{w}_{-\mathbf{i}}, \beta\right) & =\frac{n_{\left(t_{i}, w_{i}\right)}+\beta}{n_{\left(t_{i}\right)}+W_{t_{i}} \beta} \tag{19}
\end{align*}
$$

where $\mathbf{t}_{-\mathbf{i}}$ is the current values of all tags except $t_{i}, \mathbf{w}_{-\mathbf{i}}$ represents the complete word list excluding $w_{i}, W_{t_{i}}$ is the number of word types in the corpus, $T$ is the size of the tag set, $n_{t_{i}}$ is the number of words tagged with $t_{i}, n_{\left(t_{i}, w_{i}\right)}$ is the number of tag-word pair $\left(t_{i}, w_{i}\right), n_{\left(t_{i-2}, t_{i-1}\right)}$
is the frequency of the tag bigram $<t_{i-2}, t_{i-1}>$ and $n_{\left(t_{i-2}, t_{i-1}, t_{i}\right)}$ is the frequency of the tag trigram $<t_{i-2}, t_{i-1}, t_{i}>$.

Goldwater and Griffiths [7] use Gibbs sampling [25] to perform the inference. The inference involves estimating the posterior distribution:

$$
\begin{equation*}
P(\mathbf{t} \mid \mathbf{w}, \alpha, \beta) \propto P(\mathbf{w} \mid \mathbf{t}, \beta) P(\mathbf{t} \mid \alpha) \tag{20}
\end{equation*}
$$

The sampling distribution of $t_{i}$ under this model is:

$$
\begin{align*}
P\left(t_{i} \mid \mathbf{t}_{-\mathbf{i}}, \mathbf{w}_{-\mathbf{i}}, \alpha, \beta\right)= & \frac{n_{\left(t_{i}, w_{i}\right)}+\beta}{n_{t_{i}}+W_{t_{i}} \beta} \cdot \frac{n_{\left(t_{i-2}, t_{i-1}, t_{i}\right)}+\alpha}{n_{\left(t_{i-2}, t_{i-1}\right)}+T \alpha}  \tag{21}\\
\cdot & \frac{n_{\left(t_{i-1}, t_{i}, t_{i+1}\right)+I\left(t_{i-2}=t_{i-1}=t_{i}=t_{i+1}\right)}+\alpha}{n_{\left(t_{i-1}, t_{i}\right)}+I\left(t_{i-2}=t_{i-1}=t_{i}\right)+T \alpha} \\
\cdot & \frac{n_{\left(t_{i}, t_{i+1}, t_{i+2}\right)+I\left(t_{i-2}=t_{i}=t_{i+2}, t_{i-1}=t_{i+1}\right)+I\left(t_{i-1}=t_{i}=t_{i+1}=t_{i+2}\right)}+\alpha}{n_{\left(t_{i}, t_{i+1}\right)}+I\left(t_{i-2}=t_{i}, t_{i-1}=t_{i+1}\right)+I\left(t_{i-1}=t_{i}=t_{i+1}\right)+T \alpha}
\end{align*}
$$

where $n_{\left(t_{i-1}, t_{i}\right)}$ is the frequency of the tag bigram $\left.<t_{i-1}, t_{i}\right\rangle, n_{\left(t_{i}, t_{i+1}\right)}$ is the frequency of the tag bigram $<t_{i}, t_{i+1}>, n_{\left(t_{i-1}, t_{i}, t_{i+1}\right)}$ is the frequency of the tag trigrams $<t_{i-1}, t_{i}, t_{i+1}>$ , $n_{\left(t_{i}, t_{i+1}, t_{i+2}\right)}$ is the frequency of tag trigram $<t_{i}, t_{i+1}, t_{i+2}>$ and $I($.$) is an identity function$ that gives 1 if its argument is true, and otherwise 0 . Sampling a tag affects three trigrams. Therefore, those changes are taken into account with the identity functions.

All tags are randomly initialized at the beginning of the inference. Then each word's tag is sampled from the tags's posterior distribution given in Equation 21. This process is repeated until the system converges.

### 4.3. Joint Models for PoS Tagging and Stemming

We extend the baseline model that is explained in the previous section to perform joint $\operatorname{PoS}$ tagging and stemming in a joint model. To this end, we propose different extensions to the same model.

### 4.3.1. Stem-based Bayesian HMM (Bayesian S-HMM)

Most of the statistical stemming algorithms use the method of stripping suffixes from the word end of the without considering the syntactic similarity of the word and its stem. Inflectional affixation retains the $\operatorname{PoS}$ tag of the word, whereas derivational affixation may not. For instance, if playing is a noun, then stripping of suffix -ing is a stemming error, if playing is a verb, then removing suffix -ing will be correct. Using stem emissions instead of word emissions will reduce the emission sparsity, thereby will mitigate the number of the OOV words. Thus, we propose to emit stems rather than words in the baseline model. The plate diagram of the model is given in Figure 4.2.


Figure 4.2. The plate diagram of the stem based Bayesian HMM.

The mathematical model is given as follows:

$$
\begin{align*}
t_{i} \mid t_{i-1}, t_{i-2}=t^{\prime}, \tau^{\left(t, t^{\prime}\right)} & \propto \operatorname{Mult}\left(\tau^{\left(t, t^{\prime}\right)}\right)  \tag{22}\\
s_{i} \mid t_{i}=t, \omega^{(t)} & \propto \operatorname{Mult}\left(\omega^{(t)}\right) \\
\tau^{\left(t, t^{\prime}\right)} \mid \alpha & \propto \operatorname{Dirichlet}(\alpha) \\
\omega^{(t)} \mid \beta & \propto \operatorname{Dirichlet}(\beta)
\end{align*}
$$

Here, $t_{i}$ and $s_{i}$ are the ith tag and stem, where $w_{i}=s_{i}+m_{i}, m_{i}$ being the suffix of $w_{i}$. Mult( $\omega^{t}$ ) is the emission distribution in the form of a Multinomial distribution with parameters $\omega^{(t)}$ that is generated by $\operatorname{Dirichlet}(\beta)$ with hyperparameter $\beta$. Analogously,
$\operatorname{Mult}\left(\tau^{\left(t, t^{\prime}\right)}\right)$ is the transition distribution with parameters $\tau^{\left(t, t^{\prime}\right)}$ that is generated by $\operatorname{Dirichlet}(\alpha)$ with hyperparameter $\alpha$.

Based on the mathematical model, the conditional probability of a tag and a stem are defined as follows:

$$
\begin{align*}
P\left(t_{i} \mid \mathbf{t}_{-\mathbf{i}}, \alpha\right) & =\frac{n_{\left(t_{i-2}, t_{i-1}, t_{i}\right)}+\alpha}{n_{\left(t_{i-2}, t_{i-1}\right)}+T \alpha}  \tag{23}\\
P\left(s_{i} \mid \mathbf{t}_{-\mathbf{i}}, \mathbf{s}_{-\mathbf{i}}, \beta\right) & =\frac{n_{\left(t_{i}, s_{i}\right)}+\beta}{n_{\left(t_{i}\right)}+S_{t_{i}} \beta} \tag{24}
\end{align*}
$$

where $\mathbf{s}_{-\mathbf{i}}$ refers to stem set excluding the current stem $s_{i}, S_{t_{i}}$ is the number of stem types in the corpus, $T$ is the size of the tag set, $n_{t_{i}}$ is the number of stems tagged with $t_{i}, n_{\left(t_{i}, s_{i}\right)}$ is the number of tag-stem pair $\left(t_{i}, s_{i}\right)$.

The inference involves estimating the following posterior distribution:

$$
\begin{equation*}
P(\mathbf{t}, \mathbf{s} \mid \alpha, \beta) \propto P(\mathbf{s} \mid \mathbf{t}, \beta) P(\mathbf{t} \mid \alpha) \tag{25}
\end{equation*}
$$

The sampling distribution for $t_{i}$ and $s_{i}$ under this model is:

$$
\begin{align*}
P\left(t_{i}, s_{i} \mid \mathbf{t}_{-\mathbf{i}}, \mathbf{s}_{-\mathbf{i}}, \alpha, \beta\right)= & \frac{n_{\left(t_{i}, s_{i}\right)}+\beta}{n_{t_{i}}+S_{t_{i}} \beta} \cdot \frac{n_{\left(t_{i-2}, t_{i-1}, t_{i}\right)}+\alpha}{n_{\left(t_{i-2}, t_{i-1}\right)}+T \alpha}  \tag{26}\\
\cdot & \frac{n_{\left(t_{i-1}, t_{i}, t_{i+1}\right)+I\left(t_{i-2}=t_{i-1}=t_{i}=t_{i+1}\right)}+\alpha}{n_{\left(t_{i-1}, t_{i}\right)}+I\left(t_{i-2}=t_{i-1}=t_{i}\right)+T \alpha} \\
\cdot & \frac{n_{\left(t_{i}, t_{i+1}, t_{i+2}\right)+I\left(t_{i-2}=t_{i}=t_{i+2}, t_{i-1}=t_{i+1}\right)+I\left(t_{i-1}=t_{i}=t_{i+1}=t_{i+2}\right)}+\alpha}{n_{\left(t_{i}, t_{i+1}\right)}+I\left(t_{i-2}=t_{i}, t_{i-1}=t_{i+1}\right)+I\left(t_{i-1}=t_{i}=t_{i+1}\right)+T \alpha}
\end{align*}
$$

Algorithm of inference is given in Algorithm 1. All tags are randomly initialized and all words are split into two segments randomly as a stem and a suffix at the beginning of the inference. In each iteration of the algorithm, a tag and a stem are sampled for each word from the posterior distribution given in Equation 26 by using Gibbs sampling. This process is repeated until the system converges.

```
Algorithm 1: Stem-based Bayesian HMM
Input: \(W, \alpha, \beta, \gamma, \delta, T\), iterasyon
Output: Tagged and stemmed corpus
for \(w\) in \(W\) do
    \(i \sim \operatorname{uniform}(1\), length \((w)) s \leftarrow w[1: i]\)
    \(t \sim \operatorname{uniform}(1, T)\)
for \(k \leftarrow 1\) to iterasyon do
    for \(w\) in \(W\) do
        \(t_{i}, s_{i} \leftarrow P\left(t_{i}, s_{i} \mid \mathbf{t}_{-\mathbf{i}}, \mathbf{s}_{-\mathbf{i}}, \alpha, \beta\right)\) choose new label and stem
return \(W\)
```


### 4.3.2. Stem \& Suffix-based Bayesian HMM (Bayesian SM-HMM)

In this model, we are inspired by the morphological similarity of words having the same PoS tag. Words belonging to the same syntactic category usually take similar suffixes. For example, words ending with $l y$ are usually adverbs, whereas words ending with ness are usually nouns. We include suffixes in the emissions in addition to the stems as seen in the plate diagram of the model given in Figure 4.3.


Figure 4.3. The plate diagram of the stem and suffix-based Bayesian HMM.

The extended mathematical model becomes as follows:

$$
\begin{align*}
t_{i} \mid t_{i-1}, t_{i-2}=t^{\prime}, \tau^{\left(t, t^{\prime}\right)} & \propto \operatorname{Mult}\left(\tau^{\left(t, t^{\prime}\right)}\right)  \tag{27}\\
s_{i} \mid t_{i}=t, \omega^{(t)} & \propto \operatorname{Mult}\left(\omega^{(t)}\right) \\
m_{i} \mid t_{i}=t, \psi^{(t)} & \propto \operatorname{Mult}\left(\psi^{(t)}\right) \\
\tau^{\left(t, t^{\prime}\right)} \mid \alpha & \propto \operatorname{Dirichlet}(\alpha) \\
\omega^{t} \mid \beta & \propto \operatorname{Dirichlet}(\beta) \\
\psi^{(t)} \mid \gamma & \propto \operatorname{Dirichlet}(\gamma)
\end{align*}
$$

Here, $t_{i}, s_{i}$ an $m_{i}$ are the ith tag, the stem and the suffix where $w_{i}=s_{i}+m_{i} . \operatorname{Mult}\left(\omega^{t}\right)$ is the stem emission distribution in the form of a Multinomial distribution with parameters $\omega^{(t)}$ that is generated by $\operatorname{Dirichlet}(\beta)$ with hyperparameter $\beta$ and $\operatorname{Mult}\left(\psi^{(t)}\right)$ is the suffix emission distribution in the form of a Multinomial distribution with parameters $\psi^{(t)}$ that is generated by $\operatorname{Dirichlet}(\gamma)$ with hyperparameter $\gamma$. Analogously, $\operatorname{Mult}\left(\tau^{\left(t, t^{\prime}\right)}\right)$ is the transition distribution with parameters $\tau^{\left(t, t^{\prime}\right)}$ that is generated by $\operatorname{Dirichlet}(\alpha)$ with hyperparameter $\alpha$.

Based on the mathematical model, the conditional probability of a tag, a stem and a suffix are defined respectively as follows:

$$
\begin{align*}
P\left(t_{i} \mid \mathbf{t}_{-\mathbf{i}}, \alpha\right) & =\frac{n_{\left(t_{i-2}, t_{i-1}, t_{i}\right)}+\alpha}{n_{\left(t_{i-2}, t_{i-1}\right)}+T \alpha}  \tag{28}\\
P\left(s_{i} \mid \mathbf{t}_{-\mathbf{i}}, \mathbf{s}_{-\mathbf{i}}, \beta\right) & =\frac{n_{\left(t_{i}, s_{i}\right)}+\beta}{n_{\left(t_{i}\right)}+S_{t_{i}} \beta}  \tag{29}\\
P\left(m_{i} \mid \mathbf{t}_{-\mathbf{i}}, \mathbf{m}_{-\mathbf{i}}, \gamma\right) & =\frac{n_{\left(t_{i}, m_{i}\right)}+\gamma}{n_{\left(t_{i}\right)}+M_{t_{i}} \gamma} \tag{30}
\end{align*}
$$

where $\mathbf{m}_{-\mathbf{i}}$ denotes the suffix of all suffixes except $m_{i}, M_{t_{i}}$ is the number of suffix types in the corpus, $n_{t_{i}}$ is the number of stems tagged with $t_{i}, n_{\left(t_{i}, s_{i}\right)}$ is the number of tag-stem pairs $\left(t_{i}, s_{i}\right), n_{\left(t_{i}, m_{i}\right)}$ is the number of tag-suffix pairs.

The inference involves estimating the following posterior distribution:

$$
\begin{equation*}
P(\mathbf{t}, \mathbf{s}, \mathbf{m} \mid \alpha, \beta, \gamma) \propto P(\mathbf{s} \mid \mathbf{t}, \beta) P(\mathbf{m} \mid \mathbf{t}, \gamma) P(\mathbf{t} \mid \alpha) \tag{31}
\end{equation*}
$$

The new posterior distribution of $t_{i}, s_{i}$ and $m_{i}$ under this model is given as follows:

$$
\begin{align*}
P\left(t_{i}, s_{i}, m_{i} \mid \mathbf{t}_{-\mathbf{i}}, \mathbf{s}_{-\mathbf{i}}, \mathbf{m}_{-\mathbf{i}}, \alpha, \beta, \gamma\right)= & \frac{n_{\left(t_{i}, s_{i}\right)} \beta}{n_{t_{i}}+S_{t_{i}} \beta} \cdot \frac{n_{\left(t_{i-2}, t_{i-1}, t_{i}\right)}+\alpha}{n_{\left(t_{i-2}, t_{i-1}\right)}+T \alpha}  \tag{32}\\
& \cdot \frac{n_{\left(t_{i-1}, t_{i}, t_{i+1}\right)+I\left(t_{i-2}=t_{i-1}=t_{i}=t_{i+1}\right)}+\alpha}{n_{\left(t_{i-1}, t_{i}\right)}+I\left(t_{i-2}=t_{i-1}=t_{i}\right)+T \alpha} \\
& \cdot \frac{n_{\left(t_{i}, t_{i+1}, t_{i+2}\right)+I\left(t_{i-2}=t_{i}=t_{i+2}, t_{i-1}=t_{i+1}\right)+I\left(t_{i-1}=t_{i}=t_{i+1}=t_{i+2}\right)+\alpha}}{n_{\left(t_{i}, t_{i+1}\right)}+I\left(t_{i-2}=t_{i}, t_{i-1}=t_{i+1}\right)+I\left(t_{i-1}=t_{i}=t_{i+1}\right)+T \alpha} \\
& \cdot \frac{n_{\left(t_{i}, m_{i}\right)}+\gamma}{n_{t_{i}}+M_{t_{i}} \gamma}
\end{align*}
$$

Here, we assume that stems and suffixes are independent from each other. For the inference, all tags are randomly initialized and all words are split into two segments randomly. In each iteration of the algorithm, a tag, a stem and a suffix are sampled for each word from the posterior distribution given in Equation 32 .

### 4.3.3. Stem-based Bayesian HMM using Neural Word Embeddings (Bayesian CSHMM)

Inflectional affixation preserves the meaning of the word in addition to its syntactic category. Thus, we add semantic features to the model as prior information and we use neural word embeddings obtained from word2vec [78].

The mathematical model is the same as the stem-based Bayesian HMM model given in Section 4.3.1.

The posterior distribution of $t_{i}$ and $s_{i}$ under this model is:

$$
\begin{align*}
P\left(t_{i}, s_{i} \mid \mathbf{t}_{-\mathbf{i}}, \mathbf{s}_{-\mathbf{i}}, \alpha, \beta\right)= & \frac{n_{\left(t_{i}, s_{i}\right)}+\beta}{n_{t_{i}}+S_{t_{i}} \beta} \cdot \frac{n_{\left(t_{i-2}, t_{i-1}, t_{i}\right)}+\alpha}{n_{\left(t_{i-2}, t_{i-1}\right)}+T \alpha}  \tag{33}\\
\cdot & \frac{n_{\left(t_{i-1}, t_{i}, t_{i+1}\right)+I\left(t_{i-2}=t_{i-1}=t_{i}=t_{i+1}\right)}+\alpha}{n_{\left(t_{i-1}, t_{i}\right)}+I\left(t_{i-2}=t_{i-1}=t_{i}\right)+T \alpha} \\
& \frac{n_{\left(t_{i}, t_{i+1}, t_{i+2}\right)+I\left(t_{i-2}=t_{i}=t_{i+2}, t_{i-1}=t_{i+1}\right)+I\left(t_{i-1}=t_{i}=t_{i+1}=t_{i+2}\right)}+\alpha}{n_{\left(t_{i}, t_{i+1}\right)}+I\left(t_{i-2}=t_{i}, t_{i-1}=t_{i+1}\right)+I\left(t_{i-1}=t_{i}=t_{i+1}\right)+T \alpha} \\
\cdot & \cos \left(s_{i}, w_{i}\right)
\end{align*}
$$

where $\cos \left(s_{i}, w_{i}\right)$ is the cosine similarity of the word vectors of $s_{i}$ and $w_{i}$. The higher the cosine similarity is, semantically closer to the words are.

### 4.3.4. Stem \& Suffix-based Bayesian HMM using Neural Word Embeddings (Bayesian CSM-HMM)

In this model, a stem-suffix pair is emitted from each HMM state analogously to the stem-suffix-based Bayesian HMM model. Additionally, we use the semantic information obtained from neural word embeddings. Therefore, the mathematical model is the same as the stem-suffix-based Bayesian HMM model given in Section 4.3.2.

The new conditional distribution of $t_{i}, s_{i}$ and $m_{i}$ becomes:

$$
\begin{align*}
P\left(t_{i}, s_{i}, m_{i} \mid \mathbf{t}_{-\mathbf{i}}, \mathbf{s}_{-\mathbf{i}}, \mathbf{m}_{-\mathbf{i}}, \alpha, \beta, \gamma\right) & =\frac{n_{\left(t_{i}, s_{i}\right)}+\beta}{n_{t_{i}}+S_{t_{i}} \beta} \cdot \frac{n_{\left(t_{i-2}, t_{i-1}, t_{i}\right)}+\alpha}{n_{\left(t_{i-2}, t_{i-1}\right)}+T \alpha}  \tag{34}\\
& \cdot \frac{n_{\left(t_{i-1}, t_{i}, t_{i+1}\right)+I\left(t_{i-2}=t_{i-1}=t_{i}=t_{i+1}\right)}+\alpha}{n_{\left(t_{i-1}, t_{i}\right)}+I\left(t_{i-2}=t_{i-1}=t_{i}\right)+T \alpha} \\
& \cdot \frac{n_{\left(t_{i}, t_{i+1}, t_{i+2}\right)+I\left(t_{i-2}=t_{i}=t_{i+2}, t_{i-1}=t_{i+1}\right)+I\left(t_{i-1}=t_{i}=t_{i+1}=t_{i+2}\right)+\alpha}^{n_{\left(t_{i}, t_{i+1}\right)}+I\left(t_{i-2}=t_{i}, t_{i-1}=t_{i+1}\right)+I\left(t_{i-1}=t_{i}=t_{i+1}\right)+T \alpha}}{} \\
& \cdot \frac{n_{\left(t_{i}, m_{i}\right)}+\gamma}{n_{t_{i}}+M_{t_{i}} \gamma} \cdot \cos \left(s_{i}, w_{i}\right)
\end{align*}
$$

Again each stem and suffix are assumed to be independent from each other.

### 4.3.5. Affix Transition-based Bayesian HMM Model (Bayesian A-HMM)

In the previous models, all suffixes are assumed to be independent. However, there is a dependency between the suffixes of each word in the same sentence, especially in agglutinative languages [79]. For example, we see dependency of suffixes of each word in a sentence in Figure 4.4.


Bu masadaki kitapların en kalını yırtılmıştır. (The thickest of books on this table is torn.)

Figure 4.4. Dependency of suffixes in an example Turkish sentence.

The plate diagram of the model is given in Figure 4.5.


Figure 4.5. The plate diagram of the affix transition-based Bayesian HMM.

We adopt a trigram model for the final suffixes of each successive triples of words in each sentence.The mathematical model is given as follows:

$$
\begin{align*}
t_{i} \mid t_{i-1}, t_{i-2}=t^{\prime}, \tau^{\left(t, t^{\prime}\right)} & \propto \operatorname{Mult}\left(\tau^{\left(t, t^{\prime}\right)}\right)  \tag{35}\\
s_{i} \mid t_{i}=t, \omega^{(t)} & \propto \operatorname{Mult}\left(\omega^{(t)}\right) \\
m_{i} \mid m_{i-1}, m_{i-2}=m^{\prime}, \psi^{\left(m, m^{\prime}\right)} & \propto \operatorname{Mult}\left(\psi^{\left(m, m^{\prime}\right)}\right) \\
\tau^{\left(t, t^{\prime}\right)} \mid \alpha & \propto \operatorname{Dirichlet}(\alpha) \\
\omega^{t} \mid \beta & \propto \operatorname{Dirichlet}(\beta) \\
\psi^{\left(m, m^{\prime}\right)} \mid \gamma & \propto \operatorname{Dirichlet}(\gamma)
\end{align*}
$$

Here, $\operatorname{Mult}\left(\psi^{\left(m, m^{\prime}\right)}\right)$ defines the trigram model for the final suffixes of words with parameters $\psi^{\left(m, m^{\prime}\right)}$ that is generated by $\operatorname{Dirichlet}(\gamma)$ with hyperparameter $\gamma$.

Based on the mathematical model, the conditional probability of a tag, a stem and a suffix are defined as follows:

$$
\begin{align*}
P\left(t_{i} \mid \mathbf{t}_{-\mathbf{i}}, \alpha\right) & =\frac{n_{\left(t_{i-2}, t_{i-1}, t_{i}\right)}+\alpha}{n_{\left(t_{i-2}, t_{i-1}\right)}+T \alpha}  \tag{36}\\
P\left(m_{i} \mid \mathbf{m}_{-\mathbf{i}}, \gamma\right) & =\frac{n_{\left(m_{i-2}, m_{i-1}, t_{i}\right)}+\gamma}{n_{\left(m_{i-2}, m_{i-1}\right)}+A \gamma}  \tag{37}\\
P\left(s_{i} \mid \mathbf{t}_{-\mathbf{i}}, \mathbf{s}_{-\mathbf{i}}, \beta\right) & =\frac{n_{\left(t_{i}, s_{i}\right)}+\beta}{n_{\left(t_{i}\right)}+S_{t_{i}} \beta} \tag{38}
\end{align*}
$$

where $A$ is the number of unique suffix types in the corpus, $n_{\left(m_{i-2}, m_{i-1}\right)}$ is the frequency of the suffix bigram $<m_{i-2}, m_{i-1}>$ and $n_{\left(m_{i-2}, m_{i-1}, m_{i}\right)}$ is the frequency of the suffix trigram $<m_{i-2}, m_{i-1}, m_{i}>$.

The inference involves estimating the following posterior distribution:

$$
\begin{equation*}
P(\mathbf{t}, \mathbf{s}, \mathbf{m} \mid \alpha, \beta, \gamma) \propto P(\mathbf{s} \mid \mathbf{t}, \beta) P(\mathbf{m} \mid \gamma) P(\mathbf{t} \mid \alpha) \tag{39}
\end{equation*}
$$

Here we again assume that each stem and suffix of a word are independent from each other. We generate the suffixes independently from the tags.
The new posterior distribution of $t_{i}, s_{i}$ and $m_{i}$ becomes:

$$
\begin{aligned}
& P\left(t_{i}, s_{i}, m_{i} \mid \mathbf{t}_{-\mathbf{i}}, \mathbf{s}_{-\mathbf{i}}, \mathbf{m}_{-\mathbf{i}}, \alpha, \beta, \gamma\right)=\frac{n_{\left(t_{i}, s_{i}\right)}+\beta}{n_{t_{i}}+S_{t_{i}} \beta} \cdot \frac{n_{\left(t_{i-2}, t_{i-1}, t_{i}\right)}+\alpha}{n_{\left(t_{i-2}, t_{i-1}\right)}+T \alpha} \\
& \frac{n_{\left(t_{i-1}, t_{i}, t_{i+1}\right)+I\left(t_{i-2}=t_{i-1}=t_{i}=t_{i+1}\right)}+\alpha}{n_{\left(t_{i-1}, t_{i}\right)}+I\left(t_{i-2}=t_{i-1}=t_{i}\right)+T \alpha} \\
& \frac{n_{\left(t_{i}, t_{i+1}, t_{i+2}\right)+I\left(t_{i-2}=t_{i}=t_{i+2}, t_{i-1}=t_{i+1}\right)+I\left(t_{i-1}=t_{i}=t_{i+1}=t_{i+2}\right)+\alpha}^{n_{\left(t_{i}, t_{i+1}\right)}+I\left(t_{i-2}=t_{i}, t_{i-1}=t_{i+1}\right)+I\left(t_{i-1}=t_{i}=t_{i+1}\right)+T \alpha}}{n} \\
& \frac{n_{\left(m_{i-2}, m_{i-1}, m_{i}\right)}+\gamma}{n_{\left(m_{i-2}, m_{i-1}\right)}+A \gamma} \\
& \frac{n_{\left(m_{i-1}, m_{i}, m_{i+1}\right)+I\left(m_{i-2}=m_{i-1}=m_{i}=m_{i+1}\right)+\gamma}^{n_{\left(m_{i-1}, m_{i}\right)}+I\left(m_{i-2}=m_{i-1}=m_{i}\right)+A \gamma}}{\text { 有 }} \\
& \frac{n_{\left(m_{i}, m_{i+1}, m_{i+2}\right)+I\left(m_{i-2}=m_{i}=m_{i+2}, m_{i-1}=m_{i+1}\right)+I\left(m_{i-1}=m_{i}=m_{i+1}=m_{i+2}\right)+\gamma}^{n_{\left.m_{i}, m_{i+1}\right)}+I\left(m_{i-2}=m_{i}, m_{i-1}=m_{i+1}\right)+I\left(m_{i-1}=m_{i}=m_{i+1}\right)+A \gamma}}{1}
\end{aligned}
$$

where $n_{\left(m_{i-1}, m_{i}\right)}$ is the frequency of the suffix bigram $<m_{i-1}, m_{i}>, n_{\left(m_{i}, m_{i+1}\right)}$ is the frequency of the suffix bigram $<m_{i}, m_{i+1}>, n_{\left(m_{i-1}, m_{i}, m_{i+1}\right)}$ is the frequency of the suffix trigram $<m_{i-1}, m_{i}, m_{i+1}>$ and $n_{\left(m_{i}, m_{i+1}, m_{i+2}\right)}$ is the frequency of the suffix trigram $<m_{i}, m_{i+1}, m_{i+2}>$. Sampling each suffix affects three trigrams since each suffix exists in three suffix trigrams. Therefore, we consider the three affected trigrams in sampling using identity function analogously to the tags.

### 4.3.6. $\quad$ Stem \& Affix Transition-based Bayesian HMM Model (Bayesian AS-HMM)

In this model, only suffixes are emitted from each HMM state and stems are independent. The plate diagram of the model is given in Figure 4.6.


Figure 4.6. Stem and Transition based Bayesian HMM.

The mathematical model is given as follows:

$$
\begin{align*}
t_{i} \mid t_{i-1}, t_{i-2}=t^{\prime}, \tau^{\left(t, t^{\prime}\right)} & \propto \operatorname{Mult}\left(\tau^{\left(t, t^{\prime}\right)}\right)  \tag{41}\\
s_{i}, \rho & \propto \operatorname{Mult}(\rho) \\
m_{i} \mid t_{i}=t, \phi^{(t)} & \propto \operatorname{Mult}\left(\phi^{(t)}\right) \\
m_{i} \mid m_{i-1}, m_{i-2}=m^{\prime}, \psi^{\left(m, m^{\prime}\right)} & \propto \operatorname{Mult}\left(\psi^{\left(m, m^{\prime}\right)}\right) \\
\tau^{\left(t, t^{\prime}\right)} \mid \alpha & \propto \operatorname{Dirichlet}(\alpha) \\
\rho \mid \beta & \propto \operatorname{Dirichlet}(\beta) \\
\phi^{t} \mid \delta & \propto \operatorname{Dirichlet}(\delta) \\
\psi^{\left(m, m^{\prime}\right)} \mid \gamma & \propto \operatorname{Dirichlet}(\gamma)
\end{align*}
$$

where $\operatorname{Mult}\left(\phi^{t}\right)$ is the emission distribution in the form of a Multinomial distribution with parameter $\phi^{(t)}$ that is generated by Dirichlet $(\delta)$ with hyperparameter $\delta$ and $\operatorname{Mult}(\rho)$ defines the model for stems of words with parameters $\rho$ that is generated by $\operatorname{Dirichlet}(\beta)$ with hyperparameters $\beta$.

Based on the mathematical model, the conditional probability of a tag, a stem and a suffix are defined as follows:

$$
\begin{align*}
P\left(s_{i} \mid \beta\right) & =\frac{n\left(s_{i}\right)+\beta}{S+S_{c} \beta}  \tag{4}\\
P\left(t_{i} \mid \mathbf{t}_{-\mathbf{i}}, \alpha\right) & =\frac{n_{\left(t_{i-2}, t_{i-1}, t_{i}\right)}+\alpha}{n_{\left(t_{i-2}, t_{i-1}\right)}+T \alpha}  \tag{43}\\
P\left(m_{i} \mid \mathbf{m}_{-\mathbf{i}}, \gamma\right) & =\frac{n_{\left(m_{i-2}, m_{i-1}, t_{i}\right)}+\gamma}{n_{\left(m_{i-2}, m_{i-1}\right)}+A \gamma}  \tag{44}\\
P\left(m_{i} \mid \mathbf{t}_{-\mathbf{i}}, \mathbf{m}_{-\mathbf{i}}, \delta\right) & =\frac{n_{\left(t_{i}, m_{i}\right)}+\delta}{n_{\left(t_{i}\right)}+M_{t_{i}} \delta} \tag{45}
\end{align*}
$$

where $n\left(s_{i}\right)$ defines the number of words stemmed as $s_{i}, \mathrm{~S}$ is the number of stem in the corpus, and $S_{c}$ is the number of unique stem types in the corpus.

Inference involves estimating the posterior distribution:

$$
\begin{equation*}
P(\mathbf{t}, \mathbf{s}, \mathbf{m} \mid \alpha, \beta, \gamma, \delta) \propto P(\mathbf{s} \mid \beta) P(\mathbf{m} \mid \mathbf{t}, \delta) P(\mathbf{t} \mid \alpha) P(\mathbf{m} \mid \gamma) \tag{46}
\end{equation*}
$$

The posterior distribution of $t_{i}, s_{i}$ and $m_{i}$ under this model is:

$$
\begin{align*}
& P\left(t_{i}, s_{i}, m_{i} \mid \mathbf{t}_{-\mathbf{i}}, \mathbf{s}_{-\mathbf{i}}, \mathbf{m}_{-\mathbf{i}}, \alpha, \beta, \gamma, \delta\right)=\frac{n_{\left(t_{i}, m_{i}\right)}+\delta}{n_{t_{i}}+M_{t_{i}} \delta} \cdot \frac{n_{\left(s_{i}\right)} \beta}{S+S_{c} \beta}  \tag{47}\\
& \frac{n_{\left(t_{i-2}, t_{i-1}, t_{i}\right)}+\alpha}{n_{\left(t_{i-2}, t_{i-1}\right)}+T \alpha} \\
& \frac{n_{\left(t_{i-1}, t_{i}, t_{i+1}\right)+I\left(t_{i-2}=t_{i-1}=t_{i}=t_{i+1}\right)}+\alpha}{n_{\left(t_{i-1}, t_{i}\right)}+I\left(t_{i-2}=t_{i-1}=t_{i}\right)+T \alpha} \\
& \frac{n_{\left(t_{i}, t_{i+1}, t_{i+2}\right)+I\left(t_{i-2}=t_{i}=t_{i+2}, t_{i-1}=t_{i+1}\right)+I\left(t_{i-1}=t_{i}=t_{i+1}=t_{i+2}\right)+\alpha}^{n_{\left(t_{i}, t_{i+1}\right)}+I\left(t_{i-2}=t_{i}, t_{i-1}=t_{i+1}\right)+I\left(t_{i-1}=t_{i}=t_{i+1}\right)+T \alpha}}{n} \\
& \frac{n_{\left(m_{i-2}, m_{i-1}, m_{i}\right)}+\gamma}{n_{\left(m_{i-2}, m_{i-1}\right)}+A \gamma} \\
& \frac{n_{\left(m_{i-1}, m_{i}, m_{i+1}\right)+I\left(m_{i-2}=m_{i-1}=m_{i}=m_{i+1}\right)+\gamma}^{n_{\left(m_{i-1}, m_{i}\right)}+I\left(m_{i-2}=m_{i-1}=m_{i}\right)+A \gamma}}{n} \\
& \frac{n_{\left(m_{i}, m_{i+1}, m_{i+2}\right)+I\left(m_{i-2}=m_{i}=m_{i+2}, m_{i-1}=m_{i+1}\right)+I\left(m_{i-1}=m_{i}=m_{i+1}=m_{i+2}\right)}+\gamma}{n_{\left.m_{i}, m_{i+1}\right)}+I\left(m_{i-2}=m_{i}, m_{i-1}=m_{i+1}\right)+I\left(m_{i-1}=m_{i}=m_{i+1}\right)+A \gamma}
\end{align*}
$$

## 5. EXPERIMENTS AND RESULTS

In this chapter, we describe the datasets used in our experiments in Section 5.1. and evaluation metrics used in experiments in Section 5.2. In Section 5.3., we present the results and compare our model's performance for the PoS tagging and the stemming tasks to the other PoS tagging and stemming models.

### 5.1. Datasets

We ran experiments on several languages. The datasets used in the experiments are:

METU-Treebank [80] is a Turkish treebank built from newspapers, journal issues and books. The treebank involves 5620 sentences and 53,798 tokens.

Penn Treebank [81] is an English treebank collected from the Air Traffic Information System, the Wall Street Journal (WSJ), the Brown Corpus, Switchboard, and a variety of other sources. We used the first 12 K and 24 K words from the corpus for the experiments.

Finn Treebank [82] is a Finnish dataset annotated manually.
UD Dependency Treebank [83] is a cross-lingual treebank built especially for multilingual parsing and cross-lingual learning. We used only Basque, English and Hungarian portions.

Table 5.1. Datasets used in the experiments

| Language | Source | \# Tags |
| :--- | :--- | :--- |
| Basque | UD Dependency Treebank [83] | 16 |
| English | Penn Treebank [81] | 45 |
| English | UD Dependency Treebank [83] | 17 |
| Finnish | FinnTreeBank [82] | 14 |
| Hungarian | UD Dependency Treebank [83] | 16 |
| Turkish | METU Treebank [80] | 31 |

All datasets contain different tagsets and this variety aggravates evaluating the results of PoS tagging. We use universal PoS tagset defined by Petrov et al. (2011) [2] in our experiments.

This set consists of 12 coarse-grained tags. Therefore, we reduce the size of the tagset to 12 based on the universal PoS tagset (see Appendix A).

Figure 5.1. gives an example of mapping for a sentence taken from Penn Treebank [81]. Original PoS tagset is Penn Treebank tagset [81] and universal PoS tagset is taken from universal PoS tagset defined by Petrov et al. (2011) [2].

## Example

| Sentence: | It | has | ho | hearing | on | our | work | force | today | . |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Original: | It/PRP | has/VBZ | no/DT | bearing/NN | on/IN | our/PRP | work/NN | force/NN | today/NN | ./. |
| Universal: | It/PRON | has/VERB | no/DET | bearing/NOUN | on/ADP | our/PRON | work/NOUN | force/NOUN | today/NOUN | ./. |

Figure 5.1. Example sentence with its specific and corresponding universal POS tags.

### 5.2. Evaluation Metrics

In this section, we briefly explain the evaluation metrics that we used for PoS taging and stemming.

### 5.2.1. PoS Tagging

## Many-to-one

Many-to-one [23] accuracy maps each result tag to the most frequent gold standard tag. In this method, more than one cluster can be mapped to the same gold tag. It is one of the commonly used metrics in the literature.

## One-to-one

One-to-one [31] accuracy maps each result tag to a single gold standard tag. This method uses a greedy algorithm to obtain the best relevant mapping in terms of accuracy.

## Variation of Information (VI)

VI [84] is one of the most common approaches to evaluate PoS tagging. VI uses two parameters; homogeneity and completeness to measure the amount of information that changes from clustering C to clustering G. The expression of VI is given as follows:

$$
\begin{align*}
V I\left(C_{r}, C_{g}\right) & =H\left(C_{r}\right)+H\left(C_{g}\right)-2 I\left(C_{r}, C_{g}\right)  \tag{48}\\
& =H\left(C_{r} \mid C_{g}\right)+H\left(C_{g} \mid C_{r}\right)
\end{align*}
$$

where $I\left(C_{r}, C_{g}\right)$ measures the mutual dependence between two clusterings, $H\left(C_{r}\right)$ is the entropy associated with the result clustering $C_{r}$ (result clustering) and $H\left(C_{g}\right)$ is the entropy associated with the gold clustering $C_{g}$ (the gold clustering).

## Normalized Mutual Information (NMI)

NMI [85] normalizes the symmetric measure of statistical information between two distributions [86]. The formula of NMI is given as follows:

$$
\begin{equation*}
\operatorname{NMI}\left(C_{r}, C_{g}\right)=\frac{I\left(C_{r}, C_{g}\right)}{\sqrt{H\left(C_{r}\right) H\left(C_{g}\right)}} \tag{49}
\end{equation*}
$$

where $I\left(C_{r}, C_{g}\right)$ measures the mutual dependence between two clusterings, $H\left(C_{r}\right)$ is the entropy associated with the result clustering $C_{r}, H\left(C_{g}\right)$ is the entropy associated with the gold clustering $C_{g}$.

### 5.2.2. Stemming

## Stemmer Strength Metrics

Strength of a stemmer is important due to the prediction of Recall and Precision of index compression in the character removal case. A strong stemmer indicates a higher Recall, index compression and a lower Precision.

We used five metrics to compare the strength of our models:

1. The mean number of words per conflation class (MWC) : It is the average number of words that correspond to the same stem. Stronger stemmers tend to have a higher

MWC. It is computed as given below:

$$
\begin{equation*}
M W C=\frac{N}{S} \tag{50}
\end{equation*}
$$

where $S$ is the number of unique stems once the stemming is performed and $N$ is total number of unique words in the corpus.
2. Index compression factor (ICF) : It measures the decrease of the size of the corpus as a result of stemming. This can be calculated by;

$$
\begin{equation*}
I C F=\frac{N-S}{N} \tag{51}
\end{equation*}
$$

where $N$ is the number of unique words before stemming and $N$ is the number of unique words after stemming. Stronger stemmers tend to have a higher ICF.
3. The number of words and stems that differ (NWSF) : It is the difference between the number of words before and after stemming. It indicates the strength of stemming because stronger stemmers tend to transform words more than weaker stemmers.
4. The mean number of characters removed (MCRS) : It counts the number of characters that are removed by the stemmer. Stronger stemmers tend to remove more characters from words to obtain stems compared to weaker stemmers.
5. The mean and median Modified Hamming distance (MHD) : It measures the distance between words and their stems. The modified Hamming distance is calculated by adding the Hamming distance to the difference in the length between the word and its stem.

## Accuracy

Accuracy is used to measure the correctness of stems obtained at the end of stemming.

## Frakes and Fox Similarity Metric (FSM)

This metric is proposed by Frakes and Fox [87] to evaluate the strength and similarity based on the Hamming distance measure. It is calculated by;

$$
\begin{equation*}
N_{a}=\frac{N_{w}}{N_{s}} \tag{52}
\end{equation*}
$$

$N_{a}$ is the average number of words per conflation class, $N_{w}$ refers to the number of unique words before stemming, and $N_{s}$ is the number of unique stems after stemming.

### 5.3. Experiments

We ran experiments for Turkish, English, Finnish, Hungarian and Basque. As defined in Chapter 4., our models have four hyperparameters: $\alpha, \beta, \gamma$ and $\delta$. We manually set these hyperparameters for each experiment. We defined six sets for the values of the hyperparameters.

1. set $\alpha=0.003 \beta=1 \gamma=0.003 \delta=0.003$
2. set $\alpha=0.003 \beta=0.1 \gamma=0.003 \delta=0.003$
3. set $\alpha=0.001 \beta=1 \gamma=0.001 \delta=0.001$
4. set $\alpha=0.001 \beta=0.1 \gamma=0.001 \quad \delta=0.001$
5. set $\alpha=0.03 \beta=1 \gamma=0.03 \quad \delta=0.03$
6. set $\alpha=0.03 \beta=0.1 \gamma=0.03 \delta=0.03$

The evaluation scores for each set will be given separately in order to understand the efforts of hyperparameters better. For each experiment, we performed 5000 iterations in Gibbs sampling.

We implemented our models on Python 3.5, and tested it on a server with Express x 3650 M5, Xeon 6C E5-2620v3 2.4GHz/1866MHz/15MB Intel Xeon 2.40GHz processor. Training Bayesian S-HMM and Bayesian SM-HMM models on 53K dataset takes about 15h, 24 K datasets about 8h, and 12K datasets about 6h. Bayesian SM-HMM. Training Bayesian CSHMM and Bayesian CSM-HMM models takes longer about 2-3h on datasets due to access neural word embeddings obtained from word2vec [78] and finally Bayesian A-HMM and Bayesian AS-HMM models on 53 K dataset takes about 24 h , 24 K datasets about 18 h , and and 12 K datasets about 12 h .

We compare our PoS tagging results with Brown Clustering ${ }^{1}$ [14] and Anchor $\mathrm{HMM}^{2}$ [29] and our stemming results with HPS $^{3}$ [45], Morfessor FlatCat ${ }^{4}$ [88], and Linguistica ${ }^{5}$ [53].

[^0]Table 5.2. shows the PoS tagging results for Turkish for six hyperparameter sets. For PoS tagging task, in Many-to-one accuracy, Bayesian S-HMM gives better results and in other metrics, Bayesian CSM-HMM model gives better results than the other models. When we look at the results, generally results of Bayesian CSM-HMM are better for PoS tagging. This shows that using suffixes and semantic features helps in PoS tagging. The overall PoS tagging results show that Bayesian CSM-HMM outperforms both Brown Clustering [14], wordbased Bayesian HMM [7](baseline model), and Anchor HMM [29] for Turkish according to both Many-to-one, One-to-one, NMI and VI measure.

Since Anchor HMM [29] evaluation is restricted, One-to-one, NMI and VI accuracy couldn't be computed.

In terms of the hyperparameter values, the results show that the sixth hyperparameter set gives better results than the others (see Figure 5.2.).


Figure 5.2. Sensitivity of hyperparameter sets for PoS tagging performance in Turkish

The stemming results for Turkish are given in Table 5.3. The results show that Bayesian CS-HMM model generally gives better results in among the six hyperparameter sets. Our results are far better than HPS [45], Morfessor FlatCat [88], and Linguistica [53] for Turkish. Adding neural word embbedings to the model made a significant improvement. This may lead this conclusion:semantic information about stem and word has an important impact on stemming.

Table 5.2. Turkish PoS tagging results for different hyperparameter sets

|  |  | Metu-Sabancı Treebank |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Many-to-one | One-to-one | NMI | VI |
|  | Bayesian HMM | 54.92 | 25.32 | 19.99 | 5.00 |
|  | Bayesian S-HMM | 53.36 | 26.15 | 17.84 | 5.16 |
|  | Bayesian SM-HMM | 58.07 | 27.80 | 29.35 | 4.34 |
| 1 | Bayesian CS-HMM | 52.27 | 23.81 | 17.67 | 5.17 |
|  | Bayesian CSM-HMM | 60.09 | 27.73 | 30.43 | 4.28 |
|  | Bayesian A-HMM | 43.26 | 18.38 | 6.99 | 5.83 |
|  | Bayesian AS-HMM | 37.03 | 9.64 | 0.13 | 6.30 |
|  | Bayesian HMM | 55.44 | 26.40 | 20.83 | 4.94 |
|  | Bayesian S-HMM | 52.04 | 24.17 | 21.41 | 4.94 |
|  | Bayesian SM-HMM | 56.46 | 27.02 | 28.55 | 4.41 |
| 2 | Bayesian CS-HMM | 50.97 | 24.75 | 17.09 | 5.21 |
|  | Bayesian CSM-HMM | 59.36 | 30.53 | 30.49 | 4.30 |
|  | Bayesian A-HMM | 42.05 | 19.26 | 7.23 | 5.78 |
|  | Bayesian AS-HMM | 37.03 | 9.06 | 0.09 | 6.30 |
|  | Bayesian HMM | 55.81 | 24.32 | 20.46 | 4.95 |
|  | Bayesian S-HMM | 51.58 | 23.77 | 16.41 | 5.26 |
|  | Bayesian SM-HMM | 56.05 | 27.83 | 28.33 | 4.47 |
| 3 | Bayesian CS-HMM | 51.81 | 24.55 | 17.17 | 5.86 |
|  | Bayesian CSM-HMM | 60.53 | 31.28 | 30.97 | 4.30 |
|  | Bayesian A-HMM | 42.73 | 17.48 | 6.54 | 5.78 |
|  | Bayesian AS-HMM | 37.03 | 9.60 | 0.16 | 6.30 |
|  | Bayesian HMM | 55.31 | 27.18 | 20.30 | 4.99 |
|  | Bayesian S-HMM | 53.64 | 26.20 | 19.93 | 5.01 |
|  | Bayesian SM-HMM | 56.70 | 26.68 | 29.16 | 4.34 |
| 4 | Bayesian CS-HMM | 53.15 | 25.43 | 20.15 | 5.02 |
|  | Bayesian CSM-HMM | 59.79 | 29.51 | 30.13 | 4.30 |
|  | Bayesian A-HMM | 43.45 | 22.37 | 7.91 | 5.71 |
|  | Bayesian AS-HMM | 37.03 | 9.41 | 0.17 | 6.29 |
|  | Bayesian HMM | 55.51 | 25.16 | 20.13 | 5.00 |
|  | Bayesian S-HMM | 53.89 | 24.93 | 18.65 | 5.11 |
|  | Bayesian SM-HMM | 56.97 | 28.48 | 29.11 | 4.43 |
| 5 | Bayesian CS-HMM | 54.95 | 25.07 | 19.94 | 5.02 |
|  | Bayesian CSM-HMM | 60.10 | 30.48 | 30.90 | 4.31 |
|  | Bayesian A-HMM | 44.60 | 19.39 | 8.39 | 5.75 |
|  | Bayesian AS-HMM | 37.03 | 9.48 | 0.15 | 6.30 |
|  | Bayesian HMM | 56.79 | 27.31 | 23.25 | 4.79 |
|  | Bayesian S-HMM | 64.43 | 26.33 | 29.22 | 5.54 |
|  | Bayesian SM-HMM | 56.43 | 28.65 | 29.39 | 4.40 |
| 6 | Bayesian CS-HMM | 57.38 | 28.87 | 24.64 | 4.72 |
|  | Bayesian CSM-HMM | 59.32 | 30.93 | 30.95 | 4.30 |
|  | Bayesian A-HMM | 46.24 | 30.01 | 11.36 | 5.34 |
|  | Bayesian AS-HMM | 37483 | 9.13 | 0.12 | 6.30 |
|  | Brown Clustering | 54.91 | 30.70 | 26.78 | 4.47 |
|  | Anchor HMM | 58.82 | - | - | - |

Table 5.3. Turkish stemming results for different hyperparameter sets

|  |  | Metu-Sabancı Treebank |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Accuracy | ICF | MWC | NWSF | MCRS | MHD | FSM |
|  | Bayesian S-HMM | 47.55 | -0.97 | 4.24 | 28048 | 1.24 | 1.21 | 0.77 |
|  | Bayesian SM-HMM | 34.97 | -1.17 | 3.16 | 34685 | 1.56 | 1.37 | 0.60 |
| 1 | Bayesian CS-HMM | 57.31 | -1.41 | 3.61 | 2284 | 1.32 | 1.18 | 0.72 |
| 1 | Bayesian CSM-HMM | 39.51 | -1.15 | 3.45 | 32180 | 1.42 | 1.27 | 0.66 |
|  | Bayesian A-HMM | 37.49 | -1.53 | 3.46 | 33366 | 1.43 | 1.31 | 0.66 |
|  | Bayesian AS-HMM | 43.57 | -0.72 | 5.03 | 30211 | 1.09 | 1.11 | 0.87 |
|  | Bayesian S-HMM | 47.51 | -0.02 | 8.52 | 28124 | 1.27 | 1.28 | 0.76 |
|  | Bayesian SM-HMM | 34.97 | -1.78 | 3.16 | 34684 | 1.56 | 1.37 | 0.60 |
| 2 | Bayesian CS-HMM | 57.76 | -1.40 | 3.63 | 22627 | 1.30 | 1.17 | 0.73 |
| 2 | Bayesian CSM-HMM | 40.55 | -1.43 | 3.62 | 31605 | 1.38 | 1.24 | 0.68 |
|  | Bayesian A-HMM | 39.15 | -0.97 | 4.45 | 32495 | 1.39 | 1.31 | 0.68 |
|  | Bayesian AS-HMM | 43.43 | -. 072 | 5.04 | 30279 | 1.09 | 1.10 | 0.87 |
|  | Bayesian S-HMM | 47.30 | -0.97 | 4.42 | 28185 | 1.24 | 1.22 | 0.77 |
|  | Bayesian SM-HMM | 34.97 | -1.78 | 3.16 | 34684 | 1.56 | 1.37 | 0.60 |
| 3 | Bayesian CS-HMM | 57.47 | -1.43 | 3.59 | 22771 | 1.31 | 1.17 | 0.72 |
| 3 | Bayesian CSM-HMM | 39.50 | -1.56 | 3.43 | 32184 | 1.42 | 1.27 | 0.66 |
|  | Bayesian A-HMM | 37.30 | -1.57 | 3.41 | 33457 | 1.45 | 1.32 | 0.65 |
|  | Bayesian AS-HMM | 43.22 | -0.77 | 4.89 | 30377 | 1.11 | 0.86 |  |
|  | Bayesian S-HMM | 47.46 | -0.02 | 8.54 | 28119 | 1.27 | 1.28 | 0.76 |
|  | Bayesian SM-HMM | 34.97 | -1.78 | 3.16 | 34682 | 1.56 | 1.37 | 0.60 |
| 4 | Bayesian CS-HMM | 63.71 | -0.50 | 5.80 | 19431 | 1.07 | 1.03 | 0.88 |
| 4 | Bayesian CSM-HMM | 40.22 | -1.44 | 3.60 | 31771 | 1.39 | 1.25 | 0.67 |
|  | Bayesian A-HMM | 39.04 | -1.01 | 4.35 | 32549 | 1.40 | 1.32 | 0.68 |
|  | Bayesian AS-HMM | 43.22 | -0.78 | 4.87 | 30380 | 1.10 | 1.11 | 0.86 |
|  | Bayesian S-HMM | 47.45 | -0.95 | 4.47 | 28139 | 1.23 | 1.21 | 0.77 |
|  | Bayesian SM-HMM | 34.97 | -1.78 | 3.16 | 34682 | 1.56 | 1.37 | 0.60 |
| 5 | Bayesian CS-HMM | 57.85 | -1.42 | 3.60 | 22563 | 1.30 | 1.16 | 0.73 |
| 5 | Bayesian CSM-HMM | 39.62 | -1.53 | 3.47 | 32116 | 1.41 | 1.26 | 0.66 |
|  | Bayesian A-HMM | 38.00 | -1.45 | 3.58 | 33040 | 1.41 | 1.31 | 0.67 |
|  | Bayesian AS-HMM | 44.19 | -0.60 | 5.41 | 29869 | 1.08 | 1.10 | 0.88 |
|  | Bayesian S-HMM | 47.29 | -0.02 | 8.51 | 28225 | 1.28 | 1.29 | 0.75 |
|  | Bayesian SM-HMM | 34.96 | -1.78 | 3.17 | 34687 | 1.56 | 1.37 | 0.60 |
| 6 | Bayesian CS-HMM | 63.83 | -0.50 | 5.83 | 19401 | 1.07 | 1.02 | 0.89 |
| 6 | Bayesian CSM-HMM | 41.08 | -1.37 | 3.71 | 31312 | 1.37 | 1.23 | 0.69 |
|  | Bayesian A-HMM | 40.89 | -0.60 | 5.46 | 31567 | 1.34 | 1.30 | 0.71 |
|  | Bayesian AS-HMM | 44.40 | -0.59 | 5.43 | 29756 | 1.08 | 1.10 | 0.88 |
|  | HPS | 53.79 | -0.80 | 4.82 | 24521 | 1.18 | 1.08 | 0.81 |
|  | Morfessor | 52.06 | -0.85 | 5.10 | 23311 | 1.10 | 1.23 | 0.77 |
|  | Linguistica | 52.33 | -0.90 | 5.02 | 24021 | 1.07 | 0.81 | 0.76 |

We give also a summary of the stemming results of Turkish in Figure 5.3.


Figure 5.3. Sensitivity of parameter set for stemming performance of Turkish

The Figure 5.4. shows the relation of metrics. We can see that there is a reverse relationship between ICF, MWC, FSM and NWSF, MCRS, MHD. It can be concluded that the Bayesian CS-HMM model is acting stronger than the other models as a stemmer.

- Bayesian SM-HMM
- Bayesian A-HMM
- Bayesian CSM-HMM
- Bayesian AS-HMM
- Bayesian S-HMM
- Bayesian CS-HMM


Figure 5.4. Features summary of proposed model for Turkish

The PoS tagging results for Hungarian are presented in Table 5.4. (see 12 K results in Appendix C in Table 3.1.). The results show that Bayesian SM-HMM gives the highest scores for both Hungarian datasets. Bayesian CSM-HMM results are also close to Bayesian SM-HMM. We used a small dataset to train word2vec [78] in Hungarian. When we compare the Bayesian CSM-HMM results with the Turkish results, the small training set for word2vec [78] can be the reason of comparably low results of Bayesian-CSM HMM. This shows that using semantic features has a high impact on PoS tagging.

The overall PoS tagging results show that Bayesian-SM model outperform Brown Clustering [14], word-based Bayesian HMM [7], and Anchor HMM [29] for Hungarian according to Many-to-one, One-to-one, NMI, and VI measure.

When we compare the results of 12 K and 24 K datasets, it is seen that PoS tagging scores increase, as the dataset size increases.

Figure 5.5. shows the correlation of the dataset size and PoS tagging performance for Hungarian. The best PoS tagging results are obtained from Bayesian SM-HMM. Thus, we choose this model to analyze the affect of the size of the dataset.


Figure 5.5. Sensitivity of dataset for PoS performance of Hungarian

Table 5.5. shows stemming results for 24 K for six hyperparameter sets (see 12 K results in Appendix C]in Table 3.2.). Linguistica [53] results increase with the dataset size, whereas

Table 5.4. Hungarian 24 k PoS tagging results for different hyperparameter sets

|  |  | UD Hungarian24k Treebank |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Many-to-one | One-to-one | NMI | VI |
| 1 | Bayesian HMM | 37.03 | 16.37 | 8.66 | 5.91 |
|  | Bayesian S-HMM | 36.02 | 17.62 | 6.62 | 6.06 |
|  | Bayesian SM-HMM | 46.61 | 28.67 | 25.80 | 4.61 |
|  | Bayesian CS-HMM | 50.07 | 30.81 | 24.93 | 4.80 |
|  | Bayesian CSM-HMM | 48.66 | 27.94 | 25.12 | 4.78 |
|  | Bayesian A-HMM | 31.54 | 13.90 | 2.66 | 6.32 |
|  | Bayesian AS-HMM | 29.07 | 9.70 | 0.19 | 6.50 |
| 2 | Bayesian HMM | 33.47 | 15.36 | 9.02 | 6.17 |
|  | Bayesian S-HMM | 34.81 | 16.67 | 6.08 | 6.11 |
|  | Bayesian SM-HMM | 44.70 | 26.52 | 23.58 | 4.72 |
|  | Bayesian CS-HMM | 34.47 | 15.72 | 5.67 | 6.13 |
|  | Bayesian CSM-HMM | 47.92 | 31.60 | 28.17 | 4.73 |
|  | Bayesian A-HMM | 30.04 | 12.15 | 16.30 | 6.41 |
|  | Bayesian AS-HMM | 29.07 | 9.79 | 0.21 | 6.50 |
| 3 | Bayesian HMM | 34.29 | 15.92 | 6.82 | 6.04 |
|  | Bayesian S-HMM | 38.37 | 19.57 | 11.01 | 5.78 |
|  | Bayesian SM-HMM | 52.07 | 30.86 | 27.10 | 4.64 |
|  | Bayesian CS-HMM | 36.93 | 19.90 | 9.78 | 5.85 |
|  | Bayesian CSM-HMM | 49.95 | 29.65 | 26.20 | 4.72 |
|  | Bayesian A-HMM | 30.86 | 13.18 | 2.49 | 6.34 |
|  | Bayesian AS-HMM | 29.07 | 9.25 | 0.18 | 6.50 |
| 4 | Bayesian HMM | 37.17 | 18.02 | 8.76 | 5.90 |
|  | Bayesian S-HMM | 36.08 | 17.97 | 8.50 | 5.94 |
|  | Bayesian SM-HMM | 46.59 | 27.12 | 25.51 | 4.63 |
|  | Bayesian CS-HMM | 38.24 | 19.18 | 10.09 | 5.82 |
|  | Bayesian CSM-HMM | 50.59 | 28.98 | 24.33 | 4.84 |
|  | Bayesian A-HMM | 31.93 | 14.90 | 3.56 | 6.27 |
|  | Bayesian AS-HMM | 29.07 | 9.40 | 0.18 | 6.51 |
| 5 | Bayesian HMM | 43.92 | 22.41 | 14.75 | 5.48 |
|  | Bayesian S-HMM | 39.38 | 18.74 | 11.25 | 5.76 |
|  | Bayesian SM-HMM | 54.38 | 33.33 | 29.46 | 4.50 |
|  | Bayesian CS-HMM | 44.12 | 23.79 | 14.56 | 5.51 |
|  | Bayesian CSM-HMM | 51.20 | 29.95 | 26.17 | 4.71 |
|  | Bayesian A-HMM | 34.98 | 19.57 | 6.67 | 6.06 |
|  | Bayesian AS-HMM | 29.07 | 9.68 | 0.21 | 6.50 |
| 6 | Bayesian HMM | 40.32 | 19.04 | 13.78 | 5.58 |
|  | Bayesian S-HMM | 47.55 | 27.19 | 19.75 | 5.19 |
|  | Bayesian SM-HMM | 47.00 | 30.08 | 26.65 | 4.50 |
|  | Bayesian CS-HMM | 49.91 | 27.42 | 22.12 | 5.04 |
|  | Bayesian CSM-HMM | 47.56 | 29.51 | 27.11 | 4.47 |
|  | Bayesian A-HMM | 43.91 | 27.38 | 13.64 | 5.56 |
|  | Bayesian AS-HMM | 29597 | 9.54 | 0.22 | 6.50 |
|  | Brown Clustering | 50.89 | 33.25 | 28.65 | 4.57 |
|  | Anchor HMM | 48.86 | - | - | - |

our models' results and HPS [45], Morfessor FlatCat [88] results are not. The best results are obtained from Linguistica [53]. We get the best results from the Bayesian CS-HMM model for stemming. This was the same for Turkish. Our results obtained from the Bayesian CS-HMM model are close to HPS [45] and far better than Morfessor FlatCat [88].

Table 5.6. shows PoS tagging results for Finnish 24K datasets for six hyperparameter sets (see 12 K results in Appendix C in Table 3.3.). We get the highest scores in Many-to-one, NMI, and VI scores from the Bayesian CSM-HMM model. The highest One-to-one accuracy is obtained from Brown Clustering [14]. The results show that Bayesian SM-HMM and Bayesian CSM-HMM results are very close. This may be because of the small training set for word2vec [78] used for Bayesian CSM-HMM model.

Table 5.7. shows stemming results for Finnish 24 K datasets for six hyperparameter sets (see 12 K results in Appendix Cin Table 3.4.). The best results are obtained from Linguistica [53]. Among our models, the highest scores are obtained from Bayesian CS-HMM model like the other two agglutinative languages: Turkish and Hungarian. Our results are far better than the results of the HPS [45] and Morfessor FlatCat [88].

Table 5.8. shows PoS tagging results for Basque 24 K datasets for six hyperparameter sets (see 12 K results in Appendix C in Table 3.5.). The best results are obtained from Brown Clustering [14]. The results obtained from 24k dataset shows that we get better result with larger dataset. The scores obtained from Bayesian SM-HMM and Bayesian CSM-HMM are very close to Brown Clustering [14] and Anchor HMM [29] for 24K dataset.

Table 5.9. shows stemming results for Basque 24 K datasets for six hyperparameter sets (see 12 K results in Appendix Cin Table 3.6.). For 12K dataset, the best results are obtained from Morfessor FlatCat [88]. However, results of HPS [45], Morfessor FlatCat [88], Linguistica [53] and Bayesian CS-HMM are very close. In 24 K dataset, the best results are obtained from Linguistica [53]. It is seen that, our stemming results are not affected by the dataset size.

Table 5.10. shows PoS tagging results for Penn 24K datasets for six hyperparameter sets (see 12 K results in Appendix C in Table 3.7.). The best results are obtained from Anchor HMM [29] for Many-to-one accuracy. Brown Clustering [14] gives the highest for One-toone, NMI, VI scores. However, it is seen that Bayesian HMM [7] model is far more behind the joint models.

Table 5.5. Hungarian 24 k stemming results for different hyperparameter sets

|  |  | UD Hungarian24k Treebank |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Accuracy | ICF | MWC | NWSF | MCRS | MHD | FSM |
|  | Bayesian S-HMM | 48.26 | -0.23 | 3.17 | 12400 | 1.46 | 1.50 | 0.62 |
|  | Bayesian SM-HMM | 41.18 | -0.39 | 2.83 | 14047 | 0.77 | 0.83 | 1.15 |
| 1 | Bayesian CS-HMM | 57.03 | 0.72 | 13.00 | 13994 | 2.29 | 2.32 | 0.42 |
| 1 | Bayesian CSM-HMM | 41.99 | 0.16 | 4.69 | 12036 | 0.92 | 0.96 | 1.02 |
|  | Bayesian A-HMM | 41.37 | -0.33 | 2.93 | 14008 | 1.16 | 1.22 | 0.80 |
|  | Bayesian AS-HMM | 42.19 | -0.11 | 3.49 | 13744 | 1.54 | 1.59 | 0.62 |
|  | Bayesian S-HMM | 48.00 | -0.21 | 3.20 | 12451 | 1.48 | 1.52 | 0.64 |
|  | Bayesian SM-HMM | 41.18 | -0.39 | 2.83 | 14047 | 0.77 | 0.83 | 1.15 |
| 2 | Bayesian CS-HMM | 56.95 | -0.20 | 3.23 | 10314 | 1.25 | 1.28 | 0.76 |
| 2 | Bayesian CSM-HMM | 42.12 | -0.38 | 2.85 | 13826 | 0.80 | 0.86 | 1.11 |
|  | Bayesian A-HMM | 41.42 | -0.34 | 2.93 | 14000 | 1.17 | 1.22 | 0.80 |
|  | Bayesian AS-HMM | 42.13 | -0.13 | 3.42 | 13796 | 1.51 | 1.56 | 0.63 |
|  | Bayesian S-HMM | 46.31 | 0.20 | 4.86 | 12876 | 1.82 | 1.86 | 0.53 |
|  | Bayesian SM-HMM | 41.18 | -0.39 | 2.83 | 14048 | 0.77 | 0.83 | 1.15 |
| 3 | Bayesian CS-HMM | 56.17 | 0.17 | 4.75 | 10503 | 1.51 | 1.54 | 0.63 |
| 3 | Bayesian CSM-HMM | 42.19 | -0.39 | 2.83 | 13861 | 0.79 | 0.85 | 1.12 |
|  | Bayesian A-HMM | 41.07 | -0.09 | 3.56 | 14100 | 1.42 | 1.46 | 0.67 |
|  | Bayesian AS-HMM | 42.18 | -0.10 | 3.51 | 13804 | 1.55 | 1.60 | 0.62 |
|  | Bayesian S-HMM | 45.50 | 0.20 | 4.89 | 13059 | 1.83 | 1.86 | 0.53 |
|  | Bayesian SM-HMM | 41.18 | -0.39 | 2.83 | 14047 | 0.77 | 0.83 | 1.115 |
| 4 | Bayesian CS-HMM | 56.01 | 0.16 | 4.68 | 10552 | 1.51 | 1.54 | 0.63 |
| 4 | Bayesian CSM-HMM | 41.99 | -0.38 | 2.85 | 13814 | 0.79 | 0.85 | 1.12 |
|  | Bayesian A-HMM | 41.16 | -0.12 | 3.48 | 14074 | 1.38 | 1.43 | 0.68 |
|  | Bayesian AS-HMM | 41.98 | -0.13 | 3.43 | 13842 | 1.53 | 1.57 | 0.63 |
|  | Bayesian S-HMM | 48.17 | -0.21 | 3.21 | 12420 | 1.48 | 1.51 | 0.65 |
|  | Bayesian SM-HMM | 41.20 | -0.39 | 2.83 | 14052 | 0.78 | 0.84 | 1.14 |
| 5 | Bayesian CS-HMM | 57.17 | -0.20 | 3.26 | 10254 | 1.24 | 1.28 | 0.76 |
| 5 | Bayesian CSM-HMM | 42.13 | -0.39 | 2.84 | 13828 | 0.80 | 0.86 | 1.12 |
|  | Bayesian A-HMM | 41.40 | -0.32 | 2.97 | 14005 | 1.19 | 1.24 | 0.79 |
|  | Bayesian AS-HMM | 42.45 | -0.05 | 3.67 | 13715 | 1.57 | 1.62 | 0.61 |
|  | Bayesian S-HMM | 45.87 | 0.22 | 5.01 | 12976 | 1.83 | 1.87 | 0.53 |
|  | Bayesian SM-HMM | 41.18 | -0.39 | 2.83 | 14048 | 0.77 | 0.83 | 1.15 |
| 6 | Bayesian CS-HMM | 56.36 | 0.18 | 4.78 | 10469 | 1.50 | 1.53 | 0.64 |
| 6 | Bayesian CSM-HMM | 42.25 | -0.38 | 2.86 | 13800 | 0.80 | 0.86 | 1.11 |
|  | Bayesian A-HMM | 41.27 | -0.02 | 3.80 | 14045 | 1.50 | 1.55 | 0.63 |
|  | Bayesian AS-HMM | 42.45 | -0.06 | 3.62 | 13709 | 1.57 | 1.62 | 0.61 |
|  | HPS | 58.98 | 0.09 | 3.87 | 9784 | 0.93 | 0.98 | 1.00 |
|  | Morfessor | 45.89 | -3.20 | 3.87 | 12907 | 2.36 | 0.99 | 0.41 |
|  | Linguistica | 70.12 | 0.32 | 3.87 | 7154 | 0.73 | 0.82 | 1.21 |

Table 5.6. Finnish24k PoS tagging results for different hyperparameter sets

|  |  | Finnish24k Treebank |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Many-to-one | One-to-one | NMI | VI |
| 1 | Bayesian HMM | 41.81 | 20.37 | 9.90 | 5.59 |
|  | Bayesian S-HMM | 42.02 | 20.33 | 10.88 | 5.54 |
|  | Bayesian SM-HMM | 46.98 | 22.54 | 18.86 | 5.03 |
|  | Bayesian CS-HMM | 41.77 | 20.70 | 10.92 | 5.53 |
|  | Bayesian CSM-HMM | 46.23 | 21.92 | 18.49 | 5.05 |
|  | Bayesian A-HMM | 33.77 | 13.44 | 1.55 | 6.13 |
|  | Bayesian AS-HMM | 32.10 | 9.92 | 0.18 | 6.22 |
| 2 | Bayesian HMM | 42.66 | 21.66 | 11.47 | 5.49 |
|  | Bayesian S-HMM | 42.67 | 21.12 | 11.11 | 5.53 |
|  | Bayesian SM-HMM | 47.25 | 23.25 | 19.79 | 4.95 |
|  | Bayesian CS-HMM | 42.05 | 22.07 | 11.14 | 5.51 |
|  | Bayesian CSM-HMM | 47.42 | 23.90 | 19.93 | 4.94 |
|  | Bayesian A-HMM | 33.74 | 12.79 | 1.26 | 6.10 |
|  | Bayesian AS-HMM | 32.10 | 9.80 | 0.22 | 6.21 |
| 3 | Bayesian HMM | 41.13 | 20.27 | 9.92 | 5.60 |
|  | Bayesian S-HMM | 41.75 | 22.00 | 10.01 | 5.59 |
|  | Bayesian SM-HMM | 46.78 | 22.42 | 17.58 | 5.11 |
|  | Bayesian CS-HMM | 41.42 | 21.22 | 10.39 | 5.56 |
|  | Bayesian CSM-HMM | 46.82 | 23.75 | 18.35 | 5.09 |
|  | Bayesian A-HMM | 33.17 | 12.94 | 1.33 | 6.14 |
|  | Bayesian AS-HMM | 32.10 | 9.37 | 0.15 | 6.22 |
| 4 | Bayesian HMM | 42.06 | 21.53 | 10.84 | 5.53 |
|  | Bayesian S-HMM | 42.24 | 20.95 | 12.00 | 5.46 |
|  | Bayesian SM-HMM | 46.34 | 22.82 | 18.92 | 5.02 |
|  | Bayesian CS-HMM | 42.64 | 21.40 | 11.35 | 5.50 |
|  | Bayesian CSM-HMM | 46.71 | 23.67 | 18.72 | 5.02 |
|  | Bayesian A-HMM | 33.80 | 12.15 | 1.62 | 6.12 |
|  | Bayesian AS-HMM | 32.10 | 9.40 | 0.16 | 6.22 |
| 5 | Bayesian HMM | 43.21 | 23.39 | 13.14 | 5.39 |
|  | Bayesian S-HMM | 42.70 | 21.78 | 11.64 | 5.49 |
|  | Bayesian SM-HMM | 48.46 | 23.45 | 20.24 | 4.94 |
|  | Bayesian CS-HMM | 42.61 | 22.42 | 12.62 | 5.43 |
|  | Bayesian CSM-HMM | 47.78 | 22.79 | 20.19 | 4.93 |
|  | Bayesian A-HMM | 35.05 | 15.58 | 2.62 | 6.05 |
|  | Bayesian AS-HMM | 32.10 | 9.47 | 0.17 | 6.22 |
| 6 | Bayesian HMM | 43.18 | 23.10 | 13.63 | 5.35 |
|  | Bayesian S-HMM | 46.41 | 25.67 | 15.46 | 5.24 |
|  | Bayesian SM-HMM | 47.65 | 22.98 | 20.33 | 4.92 |
|  | Bayesian CS-HMM | 44.95 | 24.51 | 14.58 | 5.31 |
|  | Bayesian CSM-HMM | 47.58 | 24.16 | 20.70 | 4.89 |
|  | Bayesian A-HMM | 35.23 | 17.71 | 3.67 | 5.96 |
|  | Bayesian AS-HMM | 32.10 | 9.42 | 0.21 | 6.22 |
|  | Brown Clustering | 47.95 | 30.13 | 17.62 | 4.92 |
|  | Anchor HMM | 43.73 | - | - | - |

Table 5.7. Finnish 24 k stemming results for different hyperparameter sets


Table 5.8. Basque 24 k PoS tagging results for different hyperparameter sets

|  |  | Basque24k Treebank |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Many-to-one | One-to-one | NMI | VI |
|  | Bayesian HMM | 44.37 | 20.91 | 12.17 | 5.41 |
|  | Bayesian S-HMM | 45.53 | 20.92 | 11.21 | 5.47 |
|  | Bayesian SM-HMM | 53.98 | 24.58 | 24.02 | 4.58 |
| 1 | Bayesian CS-HMM | 44.26 | 21.34 | 11.02 | 5.48 |
|  | Bayesian CSM-HMM | 55.01 | 26.25 | 25.03 | 4.52 |
|  | Bayesian A-HMM | 35.17 | 12.58 | 2.07 | 6.04 |
|  | Bayesian AS-HMM | 31.02 | 10.16 | 0.19 | 6.15 |
|  | Bayesian HMM | 47.45 | 23.36 | 14.05 | 5.27 |
|  | Bayesian S-HMM | 48.32 | 19.41 | 14.34 | 5.23 |
|  | Bayesian SM-HMM | 56.29 | 28.80 | 26.28 | 4.42 |
| 2 | Bayesian CS-HMM | 49.00 | 23.42 | 13.57 | 5.30 |
|  | Bayesian CSM-HMM | 54.90 | 24.55 | 25.68 | 4.43 |
|  | Bayesian A-HMM | 37.76 | 14.37 | 3.86 | 5.93 |
|  | Bayesian AS-HMM | 31.05 | 9.67 | 0.17 | 6.16 |
|  | Bayesian HMM | 44.42 | 22.03 | 11.19 | 5.49 |
|  | Bayesian S-HMM | 45.05 | 19.84 | 10.92 | 5.39 |
|  | Bayesian SM-HMM | 54.92 | 26.56 | 24.04 | 4.52 |
| 3 | Bayesian CS-HMM | 44.68 | 20.05 | 10.69 | 5.38 |
|  | Bayesian CSM-HMM | 54.24 | 25.87 | 24.05 | 4.55 |
|  | Bayesian A-HMM | 35.48 | 12.61 | 2.33 | 5.95 |
|  | Bayesian AS-HMM | 30.88 | 9.78 | 0.17 | 6.15 |
|  | Bayesian HMM | 43.60 | 20.75 | 11.00 | 5.49 |
|  | Bayesian S-HMM | 46.65 | 20.80 | 12.10 | 5.39 |
|  | Bayesian SM-HMM | 53.63 | 23.48 | 24.72 | 4.52 |
| 4 | Bayesian CS-HMM | 47.60 | 20.46 | 12.22 | 5.38 |
|  | Bayesian CSM-HMM | 54.31 | 20.81 | 24.22 | 4.55 |
|  | Bayesian A-HMM | 38.16 | 14.52 | 3.23 | 5.95 |
|  | Bayesian AS-HMM | 31.33 | 9.63 | 0.25 | 6.15 |
|  | Bayesian HMM | 49.90 | 24.50 | 15.49 | 5.20 |
|  | Bayesian S-HMM | 47.73 | 23.75 | 13.79 | 5.31 |
|  | Bayesian SM-HMM | 56.49 | 23.83 | 26.24 | 4.44 |
| 5 | Bayesian CS-HMM | 51.44 | 25.14 | 16.83 | 5.13 |
|  | Bayesian CSM-HMM | 58.68 | 28.25 | 27.05 | 4.45 |
|  | Bayesian A-HMM | 41.17 | 18.63 | 6.27 | 5.76 |
|  | Bayesian AS-HMM | 30.82 | 9.70 | 0.13 | 6.16 |
|  | Bayesian HMM | 57.07 | 29.54 | 22.47 | 4.75 |
|  | Bayesian S-HMM | 57.38 | 29.95 | 23.63 | 4.66 |
|  | Bayesian SM-HMM | 57.31 | 28.49 | 26.64 | 4.45 |
| 6 | Bayesian CS-HMM | 58.13 | 30.41 | 23.90 | 4.66 |
|  | Bayesian CSM-HMM | 58.37 | 29.48 | 27.65 | 4.36 |
|  | Bayesian A-HMM | 44.82 | 18.75 | 9.22 | 5.52 |
|  | Bayesian AS-HMM | 31573 | 10.36 | 0.23 | 6.16 |
|  | Brown Clustering | 60.63 | 30.37 | 28.71 | 4.31 |
|  | Anchor HMM | 58.20 | - | - | - |

Table 5.9. Basque 24 k stemming results for different hyperparameter sets

|  |  | Basque24k Treebank |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Accuracy | ICF | MWC | NWSF | MCRS | MHD | FSM |
|  | Bayesian S-HMM | 35.55 | -0.45 | 3.62 | 15460 | 1.39 | 1.80 | 0.54 |
|  | Bayesian SM-HMM | 33.59 | -0.69 | 3.11 | 15910 | 0.88 | 1.30 | 0.71 |
| 1 | Bayesian CS-HMM | 49.12 | -0.44 | 3.64 | 12197 | 1.09 | 1.52 | 0.62 |
| 1 | Bayesian CSM-HMM | 36.97 | -0.65 | 3.19 | 15098 | 0.89 | 1.31 | 0.71 |
|  | Bayesian A-HMM | 33.25 | -0.67 | 3.15 | 16000 | 0.99 | 1.42 | 0.66 |
|  | Bayesian AS-HMM | 31.85 | -0.28 | 4.09 | 16341 | 1.43 | 1.84 | 0.53 |
|  | Bayesian S-HMM | 31.85 | 0.10 | 5.89 | 16357 | 1.72 | 2.12 | 0.46 |
|  | Bayesian SM-HMM | 33.55 | -0.69 | 3.12 | 15923 | 0.88 | 1.30 | 0.71 |
| 2 | Bayesian CS-HMM | 48.48 | -0.03 | 5.07 | 12351 | 1.25 | 1.67 | 0.57 |
| 2 | Bayesian CSM-HMM | 37.18 | -0.62 | 3.25 | 15048 | 0.89 | 1.32 | 0.71 |
|  | Bayesian A-HMM | 32.77 | -0.49 | 3.51 | 16112 | 1.12 | 1.55 | 0.62 |
|  | Bayesian AS-HMM | 31.75 | -0.27 | 4.13 | 16364 | 1.42 | 1.83 | 0.53 |
|  | Bayesian S-HMM | 35.93 | -0.46 | 3.60 | 15367 | 1.36 | 1.78 | 0.55 |
|  | Bayesian SM-HMM | 33.59 | -0.69 | 3.11 | 15910 | 0.88 | 1.30 | 0.71 |
| 3 | Bayesian CS-HMM | 49.54 | -0.43 | 3.68 | 12098 | 1.09 | 1.51 | 0.63 |
| 3 | Bayesian CSM-HMM | 36.95 | -0.66 | 3.18 | 15103 | 0.89 | 1.31 | 0.72 |
|  | Bayesian A-HMM | 33.32 | -0.68 | 3.12 | 15979 | 0.98 | 1.40 | 0.67 |
|  | Bayesian AS-HMM | 32.07 | -0.31 | 4.00 | 16294 | 1.40 | 1.81 | 0.54 |
|  | Bayesian S-HMM | 32.41 | 0.09 | 5.78 | 16216 | 1.71 | 2.11 | 0.47 |
|  | Bayesian SM-HMM | 33.59 | -0.69 | 3.12 | 15911 | 0.88 | 1.30 | 0.71 |
| 4 | Bayesian CS-HMM | 48.85 | -0.03 | 5.09 | 12267 | 1.24 | 1.66 | 0.57 |
| 4 | Bayesian CSM-HMM | 37.26 | -0.62 | 3.25 | 15029 | 0.89 | 1.31 | 0.72 |
|  | Bayesian A-HMM | 32.82 | -0.51 | 3.47 | 16109 | 1.11 | 1.54 | 0.62 |
|  | Bayesian AS-HMM | 32.04 | -0.31 | 3.98 | 16300 | 1.40 | 1.81 | 0.54 |
|  | Bayesian S-HMM | 36.18 | -0.47 | 3.58 | 15305 | 1.35 | 1.76 | 0.55 |
|  | Bayesian SM-HMM | 33.59 | -0.69 | 3.11 | 15911 | 0.88 | 1.30 | 0.71 |
| 5 | Bayesian CS-HMM | 49.10 | -0.43 | 3.69 | 12199 | 1.09 | 1.51 | 0.63 |
| 5 | Bayesian CSM-HMM | 36.97 | -0.64 | 3.20 | 15099 | 0.90 | 1.32 | 0.71 |
|  | Bayesian A-HMM | 33.32 | -0.66 | 3.17 | 15980 | 1.01 | 1.44 | 0.66 |
|  | Bayesian AS-HMM | 31.49 | -0.19 | 4.04 | 16433 | 1.47 | 1.88 | 0.52 |
|  | Bayesian S-HMM | 31.92 | 0.09 | 5.78 | 16334 | 1.69 | 2.10 | 0.47 |
|  | Bayesian SM-HMM | 33.54 | -0.69 | 3.12 | 15922 | 0.88 | 1.30 | 0.71 |
| 6 | Bayesian CS-HMM | 48.72 | -0.01 | 5.16 | 12299 | 1.24 | 1.67 | 0.57 |
| 6 | Bayesian CSM-HMM | 37.27 | -0.60 | 3.28 | 15029 | 0.90 | 1.32 | 0.71 |
|  | Bayesian A-HMM | 32.28 | -0.38 | 3.81 | 16237 | 1.23 | 1.65 | 0.58 |
|  | Bayesian AS-HMM | 31.53 | -0.19 | 4.38 | 16417 | 1.48 | 1.89 | 0.52 |
|  | HPS | 50.06 | 0.24 | 5.24 | 11579 | 0.77 | 1.21 | 0.77 |
|  | Morfessor | 55.50 | -0.64 | 5.24 | 10723 | 1.06 | 1.16 | 0.66 |
|  | Linguistica | 53.17 | 0.43 | 5.24 | 11211 | 0.92 | 1.39 | 0.68 |

Since the English stems are not covered in Penn Treebank [81], we were not able to evaluate the English stemming results for this dataset.

Table 5.11. shows PoS tagging results for udEnglish 24 K datasets for six hyperparameter sets (see 12 K results in Appendix C in Table 3.8.). It is seen that the results of these datasets are very similar to the results on Penn Treebank [81].

Table5.12. shows stemming results for udEnglish 24 K datasets for six hyperparameter sets (see 12 K results in Appendix C in Table 3.9.). The best results are obtained from Linguistica [53]. However, Bayesian CS-HMM model is much better than HPS [45] and Morfessor FlatCat [88].

Examples to correct and incorrect stems in all languages are given in Tables 5.13. 5.14. 5.15. 5.16. and 5.17. respectively. The results show that our joint model can find common endings, such as sl, a, mıştım in Turkish.

Table 5.13. Examples to correct and incorrect stems of Turkish

| Turkish |  |
| :--- | :--- |
| Correct | Incorrect |
| koca-sı | hiç-bir |
| tuhaf-\# | operasy-onunda |
| bil-miyor | Grossm-an |
| duvar-a | eşleri-ni |
| anla-mıştım | yirm-i |

Table 5.14. Examples to correct and incorrect stems of Hungarian

| Hungarian |  |
| :--- | :--- |
| Correct | Incorrect |
| tanár-ok | pedi-g |
| fizetés-ének | ide-i |
| bértábla-bér | befagyasz-tott |
| az-\# | pedag-ógus |
| felada-ként | emelle-t |

Table 5.10. Penn 24 K PoS tagging results for different hyperparameter sets

|  |  | Penn 24K Treebank |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Many-to-one | One-to-one | NMI | VI |
| 1 | Bayesian HMM | 32.83 | 17.52 | 7.84 | 6.15 |
|  | Bayesian S-HMM | 32.32 | 16.88 | 6.63 | 6.27 |
|  | Bayesian SM-HMM | 43.95 | 29.19 | 26.94 | 4.70 |
|  | Bayesian CS-HMM | 32.52 | 16.41 | 5.65 | 6.34 |
|  | Bayesian CSM-HMM | 46.16 | 31.63 | 27.85 | 4.73 |
|  | Bayesian A-HMM | 28.98 | 12.27 | 2.24 | 6.57 |
|  | Bayesian AS-HMM | 28.98 | 10.08 | 0.19 | 6.69 |
| 2 | Bayesian HMM | 35.82 | 19.59 | 11.42 | 5.90 |
|  | Bayesian S-HMM | 33.04 | 17.48 | 8.74 | 6.12 |
|  | Bayesian SM-HMM | 47.24 | 32.84 | 28.56 | 4.61 |
|  | Bayesian CS-HMM | 35.97 | 21.04 | 11.73 | 5.91 |
|  | Bayesian CSM-HMM | 45.84 | 30.55 | 28.67 | 4.56 |
|  | Bayesian A-HMM | 29.69 | 15.01 | 4.92 | 6.37 |
|  | Bayesian AS-HMM | 28.98 | 9.47 | 0.17 | 6.72 |
| 3 | Bayesian HMM | 31.46 | 15.29 | 5.39 | 6.34 |
|  | Bayesian S-HMM | 32.45 | 15.92 | 5.90 | 6.32 |
|  | Bayesian SM-HMM | 45.77 | 28.81 | 25.96 | 4.81 |
|  | Bayesian CS-HMM | 32.23 | 16.54 | 6.13 | 6.30 |
|  | Bayesian CSM-HMM | 39.78 | 22.16 | 22.30 | 5.07 |
|  | Bayesian A-HMM | 29.98 | 11.44 | 11.90 | 6.62 |
|  | Bayesian AS-HMM | 28.98 | 9.76 | 0.14 | 6.70 |
| 4 | Bayesian HMM | 32.95 | 19.27 | 8.56 | 6.09 |
|  | Bayesian S-HMM | 33.10 | 19.12 | 8.70 | 6.11 |
|  | Bayesian SM-HMM | 48.10 | 33.02 | 28.26 | 4.65 |
|  | Bayesian CS-HMM | 33.49 | 17.07 | 8.35 | 6.13 |
|  | Bayesian CSM-HMM | 43.10 | 29.43 | 26.22 | 4.67 |
|  | Bayesian A-HMM | 29.23 | 13.23 | 3.07 | 6.51 |
|  | Bayesian AS-HMM | 28.98 | 10.51 | . 14 | 6.69 |
| 5 | Bayesian HMM | 36.86 | 22.07 | 13.81 | 5.74 |
|  | Bayesian S-HMM | 33.82 | 19.17 | 9.08 | 6.10 |
|  | Bayesian SM-HMM | 48.61 | 32.16 | 29.85 | 4.55 |
|  | Bayesian CS-HMM | 36.60 | 24.98 | 14.41 | 5.73 |
|  | Bayesian CSM-HMM | 52.28 | 37.27 | 33.64 | 4.36 |
|  | Bayesian A-HMM | 30.19 | 16.73 | 6.04 | 6.30 |
|  | Bayesian AS-HMM | 28.98 | 9.93 | 0.17 | 6.70 |
| 6 | Bayesian HMM | 48.14 | 32.19 | 25.56 | 4.97 |
|  | Bayesian S-HMM | 43.91 | 28.22 | 23.38 | 5.09 |
|  | Bayesian SM-HMM | 48.39 | 34.79 | 31.26 | 4.47 |
|  | Bayesian CS-HMM | 46.75 | 32.65 | 26.22 | 4.91 |
|  | Bayesian CSM-HMM | 45.60 | 31.92 | 28.71 | 4.58 |
|  | Bayesian A-HMM | 36.11 | 22.35 | 15.19 | 5.67 |
|  | Bayesian AS-HMM | 28.98 | 9.93 | 0.18 | 6.70 |
|  | Brown Clustering | 50.49 | 45.71 | 38.23 | 4.02 |
|  | Anchor HMM | 55.39 | - | - | - |

Table 5.11. udEnglish 24 K PoS tagging results for different hyperparameter sets

|  |  | udEnglish 24K Treebank |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Many-to-one | One-to-one | NMI | VI |
| 1 | Bayesian HMM | 22.87 | 16.20 | 6.62 | 6.60 |
|  | Bayesian S-HMM | 20.40 | 15.48 | 4.83 | 6.77 |
|  | Bayesian SM-HMM | 36.69 | 30.98 | 24.34 | 5.22 |
|  | Bayesian CS-HMM | 21.07 | 15.80 | 5.37 | 6.73 |
|  | Bayesian CSM-HMM | 36.11 | 29.75 | 24.43 | 5.24 |
|  | Bayesian A-HMM | 18.76 | 11.51 | 2.44 | 6.93 |
|  | Bayesian AS-HMM | 16.04 | 9.25 | 0.26 | 7.07 |
| 2 | Bayesian HMM | 22.49 | 15.76 | 6.97 | 6.58 |
|  | Bayesian S-HMM | 21.54 | 15.37 | 6.81 | 6.58 |
|  | Bayesian SM-HMM | 35.77 | 29.39 | 23.75 | 5.19 |
|  | Bayesian CS-HMM | 22.85 | 16.97 | 7.57 | 6.55 |
|  | Bayesian CSM-HMM | 34.54 | 29.88 | 24.37 | 5.16 |
|  | Bayesian A-HMM | 17.18 | 11.52 | 2.25 | 6.96 |
|  | Bayesian AS-HMM | 15.97 | 9.46 | 0.26 | 7.07 |
| 3 | Bayesian HMM | 22.18 | 16.55 | 6.02 | 6.64 |
|  | Bayesian S-HMM | 20.52 | 14.65 | 4.71 | 6.78 |
|  | Bayesian SM-HMM | 33.61 | 27.47 | 21.68 | 5.36 |
|  | Bayesian CS-HMM | 20.18 | 14.77 | 4.89 | 6.77 |
|  | Bayesian CSM-HMM | 34.98 | 29.43 | 23.74 | 5.23 |
|  | Bayesian A-HMM | 16.60 | 10.79 | 1.19 | 7.03 |
|  | Bayesian AS-HMM | 15.97 | 9.25 | 0.26 | 7.09 |
| 4 | Bayesian HMM | 24.93 | 18.69 | 7.94 | 6.49 |
|  | Bayesian S-HMM | 21.46 | 15.86 | 6.85 | 6.62 |
|  | Bayesian SM-HMM | 37.21 | 33.49 | 24.57 | 5.18 |
|  | Bayesian CS-HMM | 21.00 | 14.78 | 5.77 | 6.70 |
|  | Bayesian CSM-HMM | 35.64 | 29.85 | 24.96 | 5.06 |
|  | Bayesian A-HMM | 17.28 | 11.16 | 2.02 | 6.97 |
|  | Bayesian AS-HMM | 15.97 | 9.16 | 0.20 | 7.10 |
| 5 | Bayesian HMM | 31.39 | 24.43 | 15.33 | 5.94 |
|  | Bayesian S-HMM | 25.65 | 19.80 | 8.86 | 6.47 |
|  | Bayesian SM-HMM | 38.96 | 34.06 | 27.20 | 5.02 |
|  | Bayesian CS-HMM | 24.07 | 18.02 | 8.01 | 6.54 |
|  | Bayesian CSM-HMM | 38.90 | 33.27 | 27.18 | 5.03 |
|  | Bayesian A-HMM | 25.98 | 20.08 | 8.76 | 6.45 |
|  | Bayesian AS-HMM | 15.97 | 9.21 | 0.28 | 7.09 |
| 6 | Bayesian HMM | 36.19 | 27.89 | 19.96 | 5.65 |
|  | Bayesian S-HMM | 30.43 | 23.34 | 15.00 | 6.01 |
|  | Bayesian SM-HMM | 39.69 | 32.55 | 28.17 | 4.95 |
|  | Bayesian CS-HMM | 37.71 | 31.30 | 22.99 | 5.40 |
|  | Bayesian CSM-HMM | 39.06 | 32.95 | 28.55 | 4.95 |
|  | Bayesian A-HMM | 22.77 | 16.80 | 7.76 | 6.51 |
|  | Bayesian AS-HMM | 15.97 | 9.16 | 0.26 | 7.09 |
|  | Brown Clustering | 51.97 | 47.32 | 40.25 | 4.14 |
|  | Anchor HMM | 48.79 | - | - | - |

Table 5.12. udEnglish 24 K stemming results for different hyperparameter sets

|  |  | udEnglish 24K Treebank |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Accuracy | ICF | MWC | NWSF | MCRS | MHD | FSM |
|  | Bayesian S-HMM | 54.70 | -0.31 | 4.64 | 11199 | 0.97 | 1.05 | 0.93 |
|  | Bayesian SM-HMM | 47.82 | -0.12 | 5.42 | 12648 | 0.52 | 0.61 | 1.59 |
|  | Bayesian CS-HMM | 79.95 | -0.18 | 5.17 | 5134 | 0.34 | 0.43 | 2.20 |
|  | Bayesian CSM-HMM | 50.07 | -0.07 | 5.70 | 12109 | 0.63 | 0.72 | 1.35 |
|  | Bayesian A-HMM | 47.07 | -0.19 | 5.10 | 12833 | 0.66 | 0.75 | 1.30 |
|  | Bayesian AS-HMM | 46.07 | -0.10 | 5.52 | 13071 | 1.07 | 1.16 | 0.85 |
|  | Bayesian S-HMM | 49.49 | 0.09 | 6.76 | 12272 | 1.24 | 1.32 | 0.74 |
|  | Bayesian SM-HMM | 47.82 | -0.12 | 5.42 | 12648 | 0.52 | 0.61 | 1.59 |
|  | Bayesian CS-HMM | 78.94 | -0.01 | 6.01 | 5368 | 0.43 | 0.52 | 1.85 |
| 2 | Bayesian CSM-HMM | 50.10 | -0.03 | 5.89 | 12102 | 0.66 | 0.75 | 1.30 |
|  | Bayesian A-HMM | 47.00 | -0.13 | 5.38 | 12854 | 0.68 | 0.77 | 1.26 |
|  | Bayesian AS-HMM | 46.03 | -0.10 | 5.50 | 13083 | 1.07 | 1.16 | 0.85 |
|  | Bayesian S-HMM | 53.67 | -0.30 | 4.68 | 11303 | 0.97 | 1.06 | 0.92 |
|  | Bayesian SM-HMM | 47.82 | -0.12 | 5.42 | 12647 | 0.51 | 0.61 | 1.59 |
| 3 | Bayesian CS-HMM | 79.82 | -0.18 | 5.17 | 5172 | 0.35 | 0.44 | 2.16 |
| 3 | Bayesian CSM-HMM | 50.08 | -0.08 | 5.66 | 12105 | 0.63 | 0.71 | 1.36 |
|  | Bayesian A-HMM | 47.13 | -0.20 | 5.07 | 12819 | 0.66 | 0.75 | 1.30 |
|  | Bayesian AS-HMM | 46.16 | -0.11 | 5.46 | 13050 | 1.04 | 1.13 | 0.87 |
|  | Bayesian S-HMM | 49.72 | 0.10 | 6.81 | 12217 | 1.23 | 1.31 | 0.75 |
|  | Bayesian SM-HMM | 47.83 | -0.12 | 5.42 | 12647 | 0.52 | 0.61 | 1.59 |
| 4 | Bayesian CS-HMM | 78.79 | -0.009 | 6.04 | 5404 | 0.44 | 0.52 | 1.83 |
| 4 | Bayesian CSM-HMM | 50.10 | -0.04 | 5.84 | 12100 | 0.64 | 0.73 | 1.33 |
|  | Bayesian A-HMM | 47.00 | -0.14 | 5.35 | 12851 | 0.68 | 0.77 | 1.26 |
|  | Bayesian AS-HMM | 46.37 | -0.13 | 5.40 | 13000 | 1.02 | 1.11 | 0.88 |
|  | Bayesian S-HMM | 53.41 | -0.31 | 4.65 | 11372 | 0.98 | 1.07 | 0.92 |
|  | Bayesian SM-HMM | 47.82 | -0.12 | 5.42 | 12648 | 0.52 | 0.61 | 1.59 |
| 5 | Bayesian CS-HMM | 80.01 | -0.17 | 5.19 | 5125 | 0.34 | 0.43 | 2.21 |
| 5 | Bayesian CSM-HMM | 50.14 | -0.05 | 5.79 | 12092 | 0.65 | 0.73 | 1.33 |
|  | Bayesian A-HMM | 47.02 | -0.20 | 5.07 | 12845 | 0.66 | 0.75 | 1.29 |
|  | Bayesian AS-HMM | 45.54 | -0.04 | 5.82 | 13201 | 1.16 | 1.24 | 0.79 |
|  | Bayesian S-HMM | 49.30 | 0.11 | 6.86 | 12324 | 1.24 | 1.32 | 0.74 |
|  | Bayesian SM-HMM | 47.82 | -0.12 | 5.43 | 12650 | 0.52 | 0.61 | 1.58 |
| 6 | Bayesian CS-HMM | 78.99 | -0.01 | 6.04 | 5350 | 0.43 | 0.52 | 1.84 |
| 6 | Bayesian CSM-HMM | 50.13 | -0.006 | 6.07 | 12095 | 0.69 | 0.78 | 1.25 |
|  | Bayesian A-HMM | 46.85 | -0.11 | 5.47 | 12886 | 0.71 | 0.80 | 1.22 |
|  | Bayesian AS-HMM | 45.54 | -0.04 | 5.84 | 13198 | 1.16 | 1.24 | 0.79 |
|  | HPS | 75.21 | -0.02 | 6.00 | 6012 | 0.81 | 0.55 | 0.79 |
|  | Morfessor | 63.05 | -0.9 | 5.96 | 7048 | 0.72 | 0.78 | 1.02 |
|  | Linguistica | 83.84 | 0.16 | 5.86 | 5040 | 0.69 | 0.83 | 1.17 |

Table 5.15. Examples to correct and incorrect stems of Finnish

| Finnish |  |
| :--- | :--- |
| Correct | Incorrect |
| niska+an | sai+si |
| suomenmaa+\# | tänn+e |
| pappila+ssa | tul+ee |
| piste+ttä | kotii+n |
| valinta+nsa | oll+a |

Table 5.16. Examples to correct and incorrect stems of Basque

| Basque |  |
| :--- | :--- |
| Correct | Incorrect |
| lortu-tako | mas-a |
| gero-\# | mol-de |
| palestinar-rak | ematen |
| lan-ean | nahas-mendu |
| etxe-ra | baldin-tzak |

Table 5.17. Examples to correct and incorrect stems of English

| English |  |
| :--- | :--- |
| Correct | Incorrect |
| respect-ed | caus-ing |
| year-s | troubl-e |
| of-\# | thir-d |
| rumour-s | investme-nt |
| kill-ed | opera-ting |

### 5.4. Conclusion

We proposed six different models that learn PoS tags and stems jointly for agglutinative languages. We did experiments Turkish, Finnish, Hungarian as agglutinative languages and
also Basque and English. We compared our PoS tagging and stemming results with other models. We showed that especially Bayesian CSM-HMM outperforms other models for POS tagging task and Bayesian CS-HMM outperforms other models for the stemming task.

## 6. CONCLUSION

### 6.1. Conclusion

In this thesis, we described the joint task of stemming and PoS tagging and presented six different unsupervised Bayesian joint PoS tagging and stemming models for agglutinative languages which extended the word-based Bayesian HMM model [7]. In agglutinative languages like Turkish, Finnish or Hungarian stemming and PoS tagging are crucial and connected processes. Joint models reveals effect of stemming and PoS tagging on each other. We did experiments on Turkish, Finnish, Hungarian, Basque and English. Results showed that the models can be applicable on other languages as well, although they are proposed for agglutinative languages.

The research questions are concluded accordingly:

- We showed joint learning of PoS tagging and stemming helps in both tasks in terms of their performance.
- We compared our PoS tagging with the Baseline model which is word-based.The results show that using stems and affixes rather than words improve PoS tagging results. Stemming results also improve in the joint task.
- Semantic information play an important role in this thesis as Schone and Jurafsky (2000) [89], Brychcin and Konopik (2015) [45], and Narasimhan et al. (2015) [90] demonstrated the value of semantic information on PoS tagging and morphology.

Our study makes a valuable contribution to the joint learning in the PoS tagging and stemming literature. Our experiments provides two major additions. First, we show that using stems instead of words for PoS tagging task is more suitable for agglutinative languages. Learning stems reduces sparsity in PoS tagging task. Second, using semantic information for PoS tagging and stemming helps improve the scores of both tasks (We hypothesize that morhologically related words - stem and word - have semantic similarity. The similarity can be calculated by embedding vectors of words [78].).

### 6.2. Future Research Directions

The proposed joint $\operatorname{PoS}$ tagging and stemming model is a fully unsupervised model and can be applicable to any language. However, there are many problems left unsolved by the proposed models in this thesis. Experiments prove that stemming is effective but that is limited to only regular words. In other words, model cannot handle stemming irregular words. For instance, if a suffix starts with a vowel in some disyllables, haplology can be seen in Turkish $(a \breve{g} l z+l \leftarrow a \breve{g} z l)$. This can be overcome by adding operations as features that describe the transformation of a word to another word to capture irregular words. Adding mechanism to find stems of irregular words may bring higher accuracy than current models. Applying the model for a high order NLP task such as Text Classification for an extrinsic evaluation remains as another future work.

## A APPENDIX : PoS TAGSET REDUCTION

In this appendix, we present PoS tagset reduction for used datasets based on universal PoS tagset of Petrov et al. (2011) [2]. The reduced tagset for the Penn Treebank is given in Table 1.1. for the Finn Treebank in Table 1.2., for the UD Treebank for Basque, Hungarian and English in Table 1.3. 1.4., 1.5. respectievly, and for the Metu-Sabancı Turkish Treebank in Table 1.6.

Table 1.1. The mapping of the Universal tagset to the Penn Treebank tagset

| Universal tagset | Penn Treebank tagset |
| :--- | :--- |
| VERB | VBP,VBD,VBG,VBN,VB,VBZ,MD |
| PRON | WP,PRP, PRP, $W P$ |
| PUNCT | $("),(),$,- PRB-,-NONE-,-RRB-,(.),(:),("),\$ |
| PRT | RP,TO |
| DET | WDT,EX,PDT,DT |
| NOUN | NN,NNP,NNPS,NNS |
| ADV | RB,RBR,WRB,RBS |
| ADJ | JJ,JJS |
| UNKNOWN | FW,UH |
| ADP | IN |
| NUM | CD |
| CONJ | CC |

Table 1.2. The mapping of the Universal tagset to the FinnTreeBank tagset

| Universal tagset | FinnTreeBank tagset |
| :--- | :--- |
| VERB | V |
| PRON | Pron |
| PUNCT | Punct |
| PRT | Pcle |
| DET | Det |
| NOUN | N |
| ADV | Adv |
| ADJ | A |
| UNKNOWN | Symb, Foreign, Interj |
| ADP | Adp |
| NUM | Num |
| CONJ | C |

Table 1.3. The mapping of the Universal tagset to UD Basque TreeBank tagset

| Universal tagset | UD Basque TreeBank tagset |
| :--- | :--- |
| VERB | VERB, AUX |
| PRON | PRON |
| PUNCT | PUNCT |
| PRT | PART |
| DET | DET |
| NOUN | NOUN, PROPN |
| ADV | ADV |
| ADJ | ADJ |
| UNKNOWN | SYM, INTJ, X |
| ADP | ADP |
| NUM | NUM |
| CONJ | CONJ |

Table 1.4. The mapping of the Universal tagset to UD Hungarian TreeBank tagset

| Universal tagset | UD Hungarian TreeBank tagset |
| :--- | :--- |
| VERB | VERB, AUX |
| PRON | PRON |
| PUNCT | PUNCT |
| PRT | PART |
| DET | DET |
| NOUN | NOUN, PROPN |
| ADV | ADV |
| ADJ | ADJ |
| UNKNOWN | X, INTJ |
| ADP | ADP |
| NUM | NUM |
| CONJ | CONJ, SCONJ |

Table 1.5. The mapping of the Universal tagset to UD English TreeBank tagset

| Universal tagset | UD English TreeBank tagset |
| :--- | :--- |
| VERB | VERB, AUX |
| PRON | PRON |
| PUNCT | PUNCT |
| PRT | PART |
| DET | DET |
| NOUN | NOUN, PROPN |
| ADV | ADV |
| ADJ | ADJ |
| UNKNOWN | X, INTJ, SYM |
| ADP | ADP |
| NUM | NUM |
| CONJ | CONJ, SCONJ |

Table 1.6. The mapping of the Universal tagset to the Metu-Sabancı Turkish Treebank tagset

| Universal tagset | Metu-Sabancı Turkish Treebank tagset |
| :--- | :--- |
|  | Noun_Pron,Noun_Ins,Noun_Nom,Noun_Verb,Noun_Loc, |
| Noun | Noun_Acc,Noun_Abl,Noun_Gen, Noun_Dat,Noun_Adj, |
|  | Noun_Num,Noun_Pnon,Noun_Postp,Noun_Equ |
| Adj | Adj_Noun,Adj_Verb,Adj,Adj_Pron,Adj_Postp,Adj_Num |
| Adv | Adv_Verb,Adv_Adj,Adv_Noun,Adv |
| Conj | Conj |
| Det | Det |
| Interj | Interj |
| Ques | Ques |
| Verb | Verb,Negp,Verb_Noun,Verb_Postp,Verb_Adj,Verb_Adv,Verb_Verb |
| Postp | Postp |
| Num | Num |
| Pron | Pron,Pron_Noun |
| Punc | Punc |

## B APPENDIX : Word2vec DATA

## Word2vec data

In this appendix, we present datasets used to learn distributred representations of words by word2vec [78].

English : The corpus with first one billion characters from Wikipedia. (http://mattmahoney . net/dc/text8.zip)

Finn Treebank [82]: It is a treebank that has approximately 19000 sentences or sentence fragments, and 162000 word forms.

The Basque UD Treebank [83]: It is part of the Basque Dependency Treebank(BDT) [91]. The treebank consists of 8.993 sentences and 121.443 tokens.

The Hungarian UD Treebank [83]: It is derived from the Szeged Dependency Treebank [92]. It contains 1299 sentences and 42.032 words.

Turkish Boun Corpus [93]: A web corpus for Turkish is composed of four subcorpora. It has 423M words and 491M tokens.

## C APPENDIX : RESULTS FOR 12K DATASETS

In this appendix, we present PoS tagging and stemming results for 12 K datasets for six hyperparameter sets.

Table 3.1. Hungarian12K PoS tagging results for different hyperparameter sets

|  |  | UD Hungarian 12K Treebank |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Many-to-one | One-to-one | NMI | VI |
| 1 | Bayesian HMM | 32.22 | 15.12 | 4.47 | 6.21 |
|  | Bayesian S-HMM | 33.35 | 16.37 | 4.90 | 6.21 |
|  | Bayesian SM-HMM | 43.25 | 24.85 | 17.34 | 5.37 |
|  | Bayesian CS-HMM | 33.53 | 16.39 | 5.90 | 6.14 |
|  | Bayesian CSM-HMM | 44.54 | 25.78 | 21.68 | 5.03 |
|  | Bayesian A-HMM | 27.74 | 10.82 | 1.01 | 6.47 |
|  | Bayesian AS-HMM | 27.74 | 10.15 | 0.27 | 6.52 |
| 2 | Bayesian HMM | 33.33 | 15.56 | 5.60 | 6.16 |
|  | Bayesian S-HMM | 34.86 | 17.15 | 6.20 | 6.06 |
|  | Bayesian SM-HMM | 47.61 | 28.12 | 23.94 | 4.87 |
|  | Bayesian CS-HMM | 32.86 | 15.50 | 6.18 | 6.17 |
|  | Bayesian CSM-HMM | 48.00 | 28.04 | 25.22 | 4.77 |
|  | Bayesian A-HMM | 29.05 | 13.23 | 1.84 | 6.40 |
|  | Bayesian AS-HMM | 2.74 | 10.25 | 0.36 | 6.15 |
| 3 | Bayesian HMM | 32.18 | 14.87 | 4.26 | 6.24 |
|  | Bayesian S-HMM | 31.79 | 15.47 | 3.96 | 6.27 |
|  | Bayesian SM-HMM | 42.44 | 22.92 | 18.50 | 5.30 |
|  | Bayesian CS-HMM | 33.29 | 16.43 | 5.75 | 6.15 |
|  | Bayesian CSM-HMM | 44.22 | 21.30 | 19.10 | 5.25 |
|  | Bayesian A-HMM | 27.81 | 10.80 | 0.86 | 6.48 |
|  | Bayesian AS-HMM | 27.74 | 9.84 | 0.28 | 6.52 |
| 4 | Bayesian HMM | 31.51 | 14.60 | 4.31 | 6.21 |
|  | Bayesian S-HMM | 33.32 | 16.16 | 5.62 | 6.13 |
|  | Bayesian SM-HMM | 43.80 | 26.74 | 20.84 | 5.02 |
|  | Bayesian CS-HMM | 31.54 | 14.86 | 4.95 | 6.19 |
|  | Bayesian CSM-HMM | 44.52 | 24.57 | 20.57 | 5.13 |
|  | Bayesian A-HMM | 29.42 | 12.00 | 1.64 | 6.42 |
|  | Bayesian AS-HMM | 27.74 | 9.60 | 0.29 | 6.52 |
| 5 | Bayesian HMM | 34.46 | 16.81 | 9.36 | 5.89 |
|  | Bayesian S-HMM | 34.31 | 17.46 | 7.32 | 6.04 |
|  | Bayesian SM-HMM | 44.60 | 28.60 | 25.21 | 4.62 |
|  | Bayesian CS-HMM | 35.67 | 19.15 | 8.91 | 5.94 |
|  | Bayesian CSM-HMM | 52.58 | 32.53 | 28.20 | 4.60 |
|  | Bayesian A-HMM | 31.84 | 16.16 | 4.53 | 6.22 |
|  | Bayesian AS-HMM | 27.74 | 9.99 | 0.28 | 6.51 |
| 6 | Bayesian HMM | 37.93 | 19.29 | 11.94 | 5.73 |
|  | Bayesian S-HMM | 41.39 | 21.49 | 15.37 | 5.49 |
|  | Bayesian SM-HMM | 52.96 | 32.66 | 29.04 | 4.54 |
|  | Bayesian CS-HMM | 39.20 | 22.02 | 12.92 | 5.65 |
|  | Bayesian CSM-HMM | 50.81 | 29.53 | 28.15 | 4.58 |
|  | Bayesian A-HMM | 35.75 | 19.45 | 7.99 | 5.99 |
|  | Bayesian AS-HMM | 27.74 | 10.08 | 0.31 | 6.52 |
|  | Brown Clustering | 50.98 | 33.83 | 28.42 | 4.62 |
|  | Anchor HMM | 48.56 | - | - | - |

Table 3.2. Hungarian12k stemming results for different hyperparameter sets


Table 3.3. Finnish 12 K PoS tagging results for different hyperparameter sets

|  |  | Finnish 12K Treebank |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Many-to-one | One-to-one | NMI | VI |
| 1 | Bayesian HMM | 39.76 | 19.80 | 9.67 | 5.63 |
|  | Bayesian S-HMM | 39.81 | 20.83 | 9.50 | 5.64 |
|  | Bayesian SM-HMM | 45.61 | 22.51 | 16.33 | 5.23 |
|  | Bayesian CS-HMM | 40.81 | 20.80 | 9.38 | 5.65 |
|  | Bayesian CSM-HMM | 44.46 | 22.07 | 16.15 | 5.23 |
|  | Bayesian A-HMM | 31.89 | 10.65 | 0.79 | 6.20 |
|  | Bayesian AS-HMM | 31.69 | 9.82 | 0.35 | 6.23 |
| 2 | Bayesian HMM | 40.83 | 20.58 | 10.18 | 5.59 |
|  | Bayesian S-HMM | 39.97 | 17.87 | 9.92 | 5.62 |
|  | Bayesian SM-HMM | 46.28 | 22.61 | 18.06 | 5.10 |
|  | Bayesian CS-HMM | 39.45 | 16.91 | 9.72 | 5.63 |
|  | Bayesian CSM-HMM | 47.52 | 24.35 | 18.10 | 5.11 |
|  | Bayesian A-HMM | 32.20 | 11.41 | 1.18 | 6.17 |
|  | Bayesian AS-HMM | 31.69 | 10.08 | 0.44 | 6.22 |
| 3 | Bayesian HMM | 38.95 | 18.80 | 8.25 | 5.72 |
|  | Bayesian S-HMM | 39.40 | 19.25 | 8.51 | 5.71 |
|  | Bayesian SM-HMM | 44.79 | 22.41 | 14.79 | 5.31 |
|  | Bayesian CS-HMM | 38.35 | 19.47 | 8.46 | 5.70 |
|  | Bayesian CSM-HMM | 45.71 | 22.95 | 16.94 | 5.18 |
|  | Bayesian A-HMM | 31.69 | 10.01 | 0.49 | 6.22 |
|  | Bayesian AS-HMM | 31.69 | 10.21 | 0.32 | 6.22 |
| 4 | Bayesian HMM | 38.86 | 19.84 | 8.69 | 5.68 |
|  | Bayesian S-HMM | 38.40 | 17.26 | 8.95 | 5.67 |
|  | Bayesian SM-HMM | 45.70 | 22.56 | 16.13 | 5.22 |
|  | Bayesian CS-HMM | 41.09 | 20.85 | 9.33 | 5.65 |
|  | Bayesian CSM-HMM | 45.99 | 23.21 | 17.43 | 5.15 |
|  | Bayesian A-HMM | 31.83 | 10.60 | 0.64 | 6.21 |
|  | Bayesian AS-HMM | 31.69 | 9.70 | 0.31 | 6.23 |
| 5 | Bayesian HMM | 42.07 | 21.78 | 12.65 | 5.44 |
|  | Bayesian S-HMM | 41.68 | 21.74 | 12.21 | 5.47 |
|  | Bayesian SM-HMM | 48.23 | 23.68 | 20.80 | 4.92 |
|  | Bayesian CS-HMM | 41.68 | 22.39 | 11.52 | 5.52 |
|  | Bayesian CSM-HMM | 47.69 | 22.76 | 20.21 | 4.98 |
|  | Bayesian A-HMM | 32.61 | 13.22 | 1.89 | 6.13 |
|  | Bayesian AS-HMM | 31.69 | 9.89 | 0.36 | 6.32 |
| 6 | Bayesian HMM | 43.47 | 22.05 | 12.26 | 5.46 |
|  | Bayesian S-HMM | 42.87 | 23.94 | 13.06 | 5.41 |
|  | Bayesian SM-HMM | 47.60 | 23.35 | 21.36 | 4.87 |
|  | Bayesian CS-HMM | 42.16 | 22.68 | 12.68 | 5.43 |
|  | Bayesian CSM-HMM | 48.49 | 24.84 | 21.41 | 4.87 |
|  | Bayesian A-HMM | 33.26 | 13.51 | 2.91 | 6.03 |
|  | Bayesian AS-HMM | 31.69 | 9.88 | 0.32 | 6.22 |
|  | Brown Clustering | 44.33 | 28.21 | 17.58 | 4.96 |
|  | Anchor HMM | 45.23 | - | - | - |

Table 3.4. Finnish 12 K stemming results for different hyperparameter sets


Table 3.5. Basque 12 K PoS tagging results for different hyperparameter sets

|  |  | Basque 12K Treebank |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Many-to-one | One-to-one | NMI | VI |
| 1 | Bayesian HMM | 33.87 | 19.31 | 9.23 | 6.03 |
|  | Bayesian S-HMM | 43.11 | 18.62 | 9.62 | 5.58 |
|  | Bayesian SM-HMM | 48.49 | 24.96 | 17.07 | 5.10 |
|  | Bayesian CS-HMM | 41.99 | 18.00 | 8.45 | 5.64 |
|  | Bayesian CSM-HMM | 50.50 | 23.71 | 20.59 | 4.87 |
|  | Bayesian A-HMM | 32.63 | 10.92 | 1.10 | 6.11 |
|  | Bayesian AS-HMM | 31.63 | 10.56 | 0.44 | 6.14 |
| 2 | Bayesian HMM | 32.12 | 18.32 | 8.72 | 6.07 |
|  | Bayesian S-HMM | 44.38 | 22.07 | 10.89 | 5.46 |
|  | Bayesian SM-HMM | 49.68 | 22.32 | 20.98 | 4.86 |
|  | Bayesian CS-HMM | 44.87 | 20.72 | 10.60 | 5.49 |
|  | Bayesian CSM-HMM | 52.30 | 24.44 | 22.64 | 4.76 |
|  | Bayesian A-HMM | 34.49 | 12.11 | 1.71 | 6.06 |
|  | Bayesian AS-HMM | 31.57 | 11.11 | 0.32 | 6.14 |
| 3 | Bayesian HMM | 33.41 | 18.90 | 8.82 | 6.07 |
|  | Bayesian S-HMM | 39.48 | 15.05 | 5.95 | 5.80 |
|  | Bayesian SM-HMM | 46.37 | 22.87 | 16.12 | 5.17 |
|  | Bayesian CS-HMM | 43.52 | 19.26 | 9.43 | 5.59 |
|  | Bayesian CSM-HMM | 46.26 | 20.85 | 17.76 | 5.06 |
|  | Bayesian A-HMM | 33.75 | 11.02 | 0.99 | 6.11 |
|  | Bayesian AS-HMM | 31.29 | 10.23 | 0.31 | 6.15 |
| 4 | Bayesian HMM | 33.63 | 18.79 | 9.57 | 6.01 |
|  | Bayesian S-HMM | 44.24 | 21.29 | 10.50 | 5.52 |
|  | Bayesian SM-HMM | 50.96 | 25.79 | 18.84 | 4.98 |
|  | Bayesian CS-HMM | 43.47 | 20.15 | 10.09 | 5.54 |
|  | Bayesian CSM-HMM | 49.10 | 24.55 | 19.09 | 4.97 |
|  | Bayesian A-HMM | 33.82 | 12.07 | 1.57 | 6.08 |
|  | Bayesian AS-HMM | 31.67 | 11.09 | 0.36 | 6.14 |
| 5 | Bayesian HMM | 34.04 | 20.34 | 11.59 | 5.88 |
|  | Bayesian S-HMM | 44.95 | 21.16 | 11.34 | 5.47 |
|  | Bayesian SM-HMM | 53.98 | 26.37 | 23.70 | 4.64 |
|  | Bayesian CS-HMM | 45.63 | 21.65 | 12.02 | 5.43 |
|  | Bayesian CSM-HMM | 55.97 | 26.46 | 25.45 | 4.50 |
|  | Bayesian A-HMM | 34.70 | 13.95 | 2.60 | 6.01 |
|  | Bayesian AS-HMM | 31.37 | 11.09 | 0.45 | 6.14 |
| 6 | Bayesian HMM | 37.23 | 22.58 | 13.00 | 5.79 |
|  | Bayesian S-HMM | 39.84 | 25.34 | 15.54 | 5.61 |
|  | Bayesian SM-HMM | 46.27 | 25.49 | 24.68 | 4.92 |
|  | Bayesian CS-HMM | 36.95 | 22.91 | 15.24 | 5.62 |
|  | Bayesian CSM-HMM | 46.38 | 26.84 | 25.36 | 4.93 |
|  | Bayesian A-HMM | 27.57 | 16.20 | 5.27 | 6.28 |
|  | Bayesian AS-HMM | 24.35 | 10.01 | 0.31 | 6.64 |
|  | Brown Clustering | 588.33 | 27.50 | 25.67 | 4.53 |
|  | Anchor HMM | 56.37 | - | - | - |

Table 3.6. Basque 12 K stemming results for different hyperparameter sets

|  |  | Basque 12K Treebank |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Accuracy | ICF | MWC | NWSF | MCRS | MHD | FSM |
|  | Bayesian S-HMM | 36.49 | -0.41 | 2.83 | 7627 | 1.30 | 1.72 | 0.56 |
|  | Bayesian SM-HMM | 33.52 | -0.55 | 2.58 | 7974 | 0.88 | 1.31 | 0.71 |
| 1 | Bayesian CS-HMM | 49.28 | -0.36 | 2.94 | 6091 | 1.06 | 1.48 | 0.63 |
| 1 | Bayesian CSM-HMM | 36.62 | -0.52 | 2.63 | 7601 | 0.88 | 1.30 | 0.72 |
|  | Bayesian A-HMM | 33.00 | -0.54 | 2.60 | 8039 | 1.02 | 1.45 | 0.65 |
|  | Bayesian AS-HMM | 32.01 | -0.20 | 3.32 | 8159 | 1.40 | 1.82 | 0.54 |
|  | Bayesian S-HMM | 32.95 | -0.001 | 4.00 | 8055 | 1.59 | 2.00 | 0.49 |
|  | Bayesian SM-HMM | 33.52 | -0.55 | 2.58 | 7973 | 0.88 | 1.30 | 0.71 |
| 2 | Bayesian CS-HMM | 49.16 | -0.10 | 3.63 | 6106 | 1.16 | 1.58 | 0.60 |
| 2 | Bayesian CSM-HMM | 36.95 | -0.48 | 2.70 | 7562 | 0.89 | 1.31 | 0.72 |
|  | Bayesian A-HMM | 32.30 | -0.39 | 2.89 | 8125 | 1.14 | 1.57 | 0.61 |
|  | Bayesian AS-HMM | 31.63 | -0.22 | 3.26 | 8211 | 1.40 | 1.81 | 0.54 |
|  | Bayesian S-HMM | 36.64 | -0.42 | 2.82 | 7613 | 1.30 | 1.73 | 0.56 |
|  | Bayesian SM-HMM | 33.52 | -0.55 | 2.58 | 7973 | 0.88 | 1.30 | 0.71 |
| 3 | Bayesian CS-HMM | 48.63 | -0.37 | 2.92 | 6167 | 1.08 | 1.51 | 0.62 |
| 3 | Bayesian CSM-HMM | 36.68 | -0.53 | 2.62 | 7594 | 0.87 | 1.29 | 0.72 |
|  | Bayesian A-HMM | 33.10 | -0.52 | 2.63 | 8030 | 1.03 | 1.46 | 0.65 |
|  | Bayesian AS-HMM | 32.06 | -0.25 | 3.19 | 8157 | 1.38 | 1.79 | 0.54 |
|  | Bayesian S-HMM | 33.28 | -0.02 | 3.92 | 8017 | 1.58 | 1.98 | 0.49 |
|  | Bayesian SM-HMM | 33.55 | -0.55 | 2.58 | 7969 | 0.88 | 1.30 | 0.71 |
| 4 | Bayesian CS-HMM | 48.96 | -0.09 | 3.68 | 6131 | 1.17 | 1.60 | 0.60 |
| 4 | Bayesian CSM-HMM | 37.22 | -0.49 | 2.69 | 7528 | 0.88 | 1.30 | 0.72 |
|  | Bayesian A-HMM | 32.48 | -0.40 | 2.86 | 8106 | 1.14 | 1.56 | 0.61 |
|  | Bayesian AS-HMM | 31.92 | -0.26 | 3.17 | 8174 | 1.38 | 1.79 | 0.54 |
|  | Bayesian S-HMM | 36.16 | -0.42 | 2.83 | 7669 | 1.33 | 1.74 | 0.55 |
|  | Bayesian SM-HMM | 33.55 | -0.55 | 2.58 | 7969 | 0.88 | 1.31 | 0.71 |
| 5 | Bayesian CS-HMM | 49.27 | -0.35 | 2.97 | 6093 | 1.08 | 1.50 | 0.63 |
| 5 | Bayesian CSM-HMM | 36.80 | -0.50 | 2.66 | 7579 | 0.90 | 1.32 | 0.71 |
|  | Bayesian A-HMM | 33.21 | -0.52 | 2.64 | 8016 | 1.05 | 1.47 | 0.64 |
|  | Bayesian AS-HMM | 31.55 | -0.16 | 3.43 | 8216 | 1.45 | 1.86 | 0.53 |
|  | Bayesian S-HMM | 32.95 | 0.003 | 4.03 | 8056 | 1.60 | 2.00 | 0.49 |
|  | Bayesian SM-HMM | 33.49 | -0.55 | 2.59 | 7977 | 0.88 | 1.31 | 0.71 |
| 6 | Bayesian CS-HMM | 49.04 | -0.08 | 3.68 | 6124 | 1.17 | 1.59 | 0.60 |
| 6 | Bayesian CSM-HMM | 37.36 | -0.47 | 2.73 | 7512 | 0.90 | 1.32 | 0.71 |
|  | Bayesian A-HMM | 32.43 | -0.29 | 3.10 | 8111 | 1.23 | 1.65 | 0.58 |
|  | Bayesian AS-HMM | 31.36 | -0.16 | 3.44 | 8238 | 1.45 | 1.87 | 0.53 |
|  | HPS | 48.95 | 0.26 | 4.00 | 6153 | 0.81 | 1.26 | 0.74 |
|  | Morfessor | 51.70 | -0.50 | 4.00 | 5829 | 1.18 | 1.24 | 0.61 |
|  | Linguistica | 52.75 | 0.38 | 4.00 | 5668 | 0.93 | 1.40 | 0.67 |

Table 3.7. Penn 12 K PoS tagging results for different hyperparameter sets

|  |  | Penn 12K Treebank |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Many-to-one | One-to-one | NMI | VI |
| 1 | Bayesian HMM | 32.85 | 14.47 | 4.50 | 6.39 |
|  | Bayesian S-HMM | 32.94 | 15.13 | 4.52 | 6.40 |
|  | Bayesian SM-HMM | 41.86 | 27.58 | 19.34 | 5.34 |
|  | Bayesian CS-HMM | 33.01 | 14.80 | 4.49 | 6.40 |
|  | Bayesian CSM-HMM | 42.54 | 24.70 | 20.48 | 5.15 |
|  | Bayesian A-HMM | 29.86 | 10.76 | 1.25 | 6.63 |
|  | Bayesian AS-HMM | 29.86 | 10.19 | 0.36 | 6.68 |
| 2 | Bayesian HMM | 32.96 | 16.60 | 5.49 | 6.28 |
|  | Bayesian S-HMM | 33.41 | 15.56 | 5.37 | 6.29 |
|  | Bayesian SM-HMM | 48.12 | 32.80 | 28.11 | 4.62 |
|  | Bayesian CS-HMM | 33.21 | 16.13 | 5.27 | 6.33 |
|  | Bayesian CSM-HMM | 45.70 | 28.25 | 25.62 | 4.80 |
|  | Bayesian A-HMM | 29.86 | 14.16 | 2.86 | 6.50 |
|  | Bayesian AS-HMM | 29.86 | 10.30 | 0.33 | 6.67 |
| 3 | Bayesian HMM | 32.15 | 13.75 | 3.18 | 6.48 |
|  | Bayesian S-HMM | 32.20 | 14.46 | 3.86 | 6.44 |
|  | Bayesian SM-HMM | 38.90 | 21.28 | 17.42 | 5.48 |
|  | Bayesian CS-HMM | 33.14 | 14.77 | 4.34 | 6.41 |
|  | Bayesian CSM-HMM | 39.93 | 23.34 | 17.55 | 5.45 |
|  | Bayesian A-HMM | 29.86 | 10.64 | 1.08 | 6.64 |
|  | Bayesian AS-HMM | 29.86 | 10.43 | 0.30 | 6.67 |
| 4 | Bayesian HMM | 32.11 | 15.21 | 4.22 | 6.39 |
|  | Bayesian S-HMM | 33.21 | 14.98 | 5.55 | 6.29 |
|  | Bayesian SM-HMM | 45.28 | 28.24 | 25.96 | 4.77 |
|  | Bayesian CS-HMM | 32.78 | 14.67 | 4.10 | 6.42 |
|  | Bayesian CSM-HMM | 44.29 | 29.75 | 24.71 | 4.79 |
|  | Bayesian A-HMM | 29.86 | 11.24 | 1.49 | 6.60 |
|  | Bayesian AS-HMM | 29.86 | 10.07 | 0.28 | 6.68 |
| 5 | Bayesian HMM | 33.30 | 18.25 | 8.35 | 6.12 |
|  | Bayesian S-HMM | 33.18 | 16.92 | 7.14 | 6.21 |
|  | Bayesian SM-HMM | 50.67 | 35.23 | 31.55 | 4.48 |
|  | Bayesian CS-HMM | 33.28 | 16.79 | 6.79 | 6.24 |
|  | Bayesian CSM-HMM | 48.01 | 31.24 | 28.43 | 4.63 |
|  | Bayesian A-HMM | 29.86 | 13.52 | 3.09 | 6.49 |
|  | Bayesian AS-HMM | 29.86 | 9.79 | 0.44 | 6.66 |
| 6 | Bayesian HMM | 35.04 | 21.91 | 11.58 | 5.88 |
|  | Bayesian S-HMM | 39.02 | 23.73 | 14.89 | 5.66 |
|  | Bayesian SM-HMM | 51.52 | 36.78 | 32.33 | 4.38 |
|  | Bayesian CS-HMM | 38.64 | 23.18 | 15.11 | 5.67 |
|  | Bayesian CSM-HMM | 52.21 | 34.74 | 31.58 | 4.50 |
|  | Bayesian A-HMM | 34.46 | 19.54 | 11.04 | 5.90 |
|  | Bayesian AS-HMM | 29.86 | 10.20 | 0.33 | 6.67 |
|  | Brown Clustering | 467.88 | 43.15 | 36.60 | 4.15 |
|  | Anchor HMM | 52.36 | - | - | - |

Table 3.8. udEnglish 12 K PoS tagging results for different hyperparameter sets

|  |  | udEnglish 12K Treebank |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Many-to-one | One-to-one | NMI | VI |
| 1 | Bayesian HMM | 19.98 | 14.56 | 3.84 | 6.83 |
|  | Bayesian S-HMM | 19.23 | 13.44 | 3.67 | 6.85 |
|  | Bayesian SM-HMM | 32.75 | 29.93 | 19.81 | 5.55 |
|  | Bayesian CS-HMM | 19.25 | 13.48 | 3.79 | 6.83 |
|  | Bayesian CSM-HMM | 30.09 | 22.23 | 18.26 | 5.72 |
|  | Bayesian A-HMM | 16.74 | 10.84 | 1.56 | 7.01 |
|  | Bayesian AS-HMM | 15.58 | 9.69 | 0.44 | 7.07 |
| 2 | Bayesian HMM | 19.57 | 14.40 | 4.67 | 6.76 |
|  | Bayesian S-HMM | 19.48 | 13.88 | 4.73 | 6.75 |
|  | Bayesian SM-HMM | 35.06 | 27.06 | 21.96 | 5.44 |
|  | Bayesian CS-HMM | 19.43 | 14.78 | 4.38 | 6.80 |
|  | Bayesian CSM-HMM | 33.97 | 29.12 | 22.95 | 5.21 |
|  | Bayesian A-HMM | 16.06 | 10.66 | 1.42 | 7.02 |
|  | Bayesian AS-HMM | 15.54 | 9.32 | 0.35 | 7.09 |
| 3 | Bayesian HMM | 19.10 | 14.00 | 3.55 | 6.86 |
|  | Bayesian S-HMM | 18.73 | 13.11 | 3.29 | 6.88 |
|  | Bayesian SM-HMM | 28.91 | 22.44 | 16.24 | 5.83 |
|  | Bayesian CS-HMM | 19.58 | 13.96 | 3.86 | 6.84 |
|  | Bayesian CSM-HMM | 29.43 | 21.96 | 15.06 | 5.94 |
|  | Bayesian A-HMM | 16.26 | 10.48 | 1.21 | 7.03 |
|  | Bayesian AS-HMM | 15.51 | 9.64 | 0.37 | 7.09 |
| 4 | Bayesian HMM | 19.49 | 14.28 | 4.12 | 6.79 |
|  | Bayesian S-HMM | 19.82 | 14.89 | 4.87 | 6.75 |
|  | Bayesian SM-HMM | 28.78 | 21.35 | 18.08 | 5.71 |
|  | Bayesian CS-HMM | 21.02 | 14.48 | 4.82 | 6.76 |
|  | Bayesian CSM-HMM | 31.23 | 24.00 | 18.43 | 5.73 |
|  | Bayesian A-HMM | 16.32 | 11.41 | 1.68 | 6.98 |
|  | Bayesian AS-HMM | 15.67 | 9.36 | 0.38 | 7.09 |
| 5 | Bayesian HMM | 21.55 | 16.09 | 6.13 | 6.66 |
|  | Bayesian S-HMM | 19.87 | 14.68 | 5.23 | 6.75 |
|  | Bayesian SM-HMM | 37.26 | 30.92 | 25.11 | 5.71 |
|  | Bayesian CS-HMM | 19.97 | 14.57 | 4.90 | 6.76 |
|  | Bayesian CSM-HMM | 35.45 | 29.83 | 24.23 | 5.19 |
|  | Bayesian A-HMM | 17.11 | 11.58 | 1.89 | 6.98 |
|  | Bayesian AS-HMM | 15.55 | 9.82 | 0.41 | 7.06 |
| 6 | Bayesian HMM | 23.91 | 18.60 | 9.74 | 6.38 |
|  | Bayesian S-HMM | 23.42 | 16.32 | 7.74 | 6.54 |
|  | Bayesian SM-HMM | 38.86 | 32.89 | 27.21 | 5.01 |
|  | Bayesian CS-HMM | 23.66 | 17.72 | 9.08 | 6.45 |
|  | Bayesian CSM-HMM | 36.96 | 31.91 | 26.52 | 5.02 |
|  | Bayesian A-HMM | 18.61 | 14.28 | 4.39 | 6.78 |
|  | Bayesian AS-HMM | 15.53 | 9.35 | 0.37 | 7.04 |
|  | Brown Clustering | 47.82 | 42.37 | 37.23 | 4.36 |
|  | Anchor HMM | 48.72 | - | - | - |

Table 3.9. udEnglish 12 K stemming results for different hyperparameter sets


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## Project and Budgets

## Oral and Poster Presentations

## PUBLICATIONS

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Bölücü, Necva, Can, B. "Stem-based PoS Tagging for Agglutinative Languages." Signal Processing and Communication Application Conference (SIU), 2017 25th. IEEE. 2016.

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[^0]:    ${ }^{1}$ Brown Clustering: http://www.cs.berkeley.edu/~pliang/software/ brown-cluster-1.2.zip Percy Liang)
    ${ }^{2}$ Anchor HMM: https://github.com/karlstratos/anchor
    ${ }^{3}$ HPS: http://liks.fav.zcu.cz/HPS/
    ${ }^{4}$ Morfessor FlatCat: https://github.com/aalto-speech/flatcat
    ${ }^{5}$ Linguistica: http://linguistica.uchicago.edu/

